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KEY

TO THE

NATIONAL ARITHMETIC;

CONTAINING

full Solutions to nearly all the Problems,

DESIGNED FOR THE

USE OF TEACHERS AND PRIVATE STUDENTS.

BY JOHN HERBERT SANGSTER, M.A., M.D.,
MATHRMATICAL MASTER AND LECTURER IN CHEMISTRY AND NATURAL
PHILOSOPHY IV THE NORMAL SCHOOL FOR ONTARIO.

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MANAGER OF BUILDING THE SERVICE OF

PREFACE.

It was the original intention of the Author to give, in the Key, merely a series of brief hints upon the Solutions of the more difficult Problems. He was led to modify this plan, and to issue the work in its present form, chiefly from the consideration that as there are in the country many young persons who, from various causes, are unable to avail themselves of the advice and assistance of a teacher, it would be a great boon to these to have access to a book to which they might refer with the certainty of having every doubt removed as to the correctness of their work and methods of solution. He offers the work to his fellow-teachers with the hope that they will accord it the same favorable reception that they have so kindly given to the National Arithmetic.

TORONTO, May, 1861.

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(1) d 233

9331

1432

5729

PAGE 114 116 123 129 131 137 138 139 141 156 160 163 165 ... 171 175 ... 177 ... 182 ... 184 185 ... 186 ... 187 ... 192 ... 201 202 ... 210 ... 217 ... 231 235 237

... 238

KEY TO NATIONAL ARITHMETIC.

Exercise 5-Page 50.

(1) d 23328 4	(2) £ 348 20	(3) £ s. 38 10 20	(4) £ s 58 1:	124 - 124 PART - 184
93312 f.	6960 s.	770 s.	1173 s,	1173 s. 12
ata mila	we or t	9240 d.	14076 d.	14076 d.
1000		The second		56304 f.

. (6) £ s. d. 59 13 62	£ s. d. 63 0 9	(8) cwt. qrs. lbs. 16 2 16	(9) cwt. qrs. lbs. 14 3 16
20 1193 s. 12	20 1260 s.	66 qrs.	59 qrs. 25
14322 d	15129 d.	346 132 : 131	311
57291 f.	BEAST STORY	1666 lbs.	1491 lbs.

60

3)

40

60)3

60)

(10) lbs. oz. dw 3 5 12 12	t. grs. lbs. oz. o	lwt. grs. yrs.	(13) mile. 1 8	yrs. 46 365	(14) d. h. m. 21 8 56
41 oz. 20	95 20	7300	dys. 8 fur	276	, k
832 dwts. 24	1915 dwts	. 29200 14600	320 per	138 16811 de	ays.
3344 1664	7674 3830	1752001	160	67252	
19984 grs.	45974 grs.	ţ	1760 yds 8 5280 ft.	403472 h 60 1208375 m	
(15) sq. per. 74 301	(16) a. r. per. s 46 3 12	(1") q. miles. 767 640		cs. p	10) ks. 97
2220 181	187 r. 30 40 460		1534	4 gals. 15:	4 gals.
£238} sq. yds. 7	301	880 sq. a. 7	67 6136	qts. 63	6 qts.
2247 18	760. 73	18	25376 cub.		_ 2 pts.
2266	33 sq. yds.				11.

Exercise 6-Page 51.

(1) f. 4)32756	(2) grs. 24)28547	(3) yds. 51)397024
12)8189 d.	20)981 dwt. 3 grs.	2 2
20)6829 54	12\49 or 1 day 2 a	11)794048

£34 2s. 5d. 4 lbs. 1 oz. 1 dwt. 3 g. 8)1804 fur. 26 r. 1 yd.

²²⁵ m. 4 f. 26 r. 1 y.

KHY.

(14) yrs. d. h. m. 46 21 8 56 365 351 16

2 72 hrs.

80 75 min.

(20) pks. 797

. 1594 gals.

6376 qts.

12752 pts.

ds.=1 yd. 3 r. 1 yd.

26 r. 1 y.

(4) (6) lbs. 60)28635 25)1666 25)1491

60)477 m. 15 sec. 4)66 qrs. 16 lbs. 4)59 qrs. 16 lbs.

7 hrs. 57 m. 15 sec. 16 cwt. 2 q. 16 lbs. 14 cwt. 3q.16 lbs.

(7) (8) (9) (10) cub. in. OE. 24)115200 16)107520 1728)1674674 767 20)4800 dwt. 6720 lbs. 969 ft. 242 in. -4)2301 qrs. 12)240 oz. 575 yds.1 qr. 20 lbs.

(11) (12)(13)cub. in. cub. ft. 3)183810 1728)138297 128)67893

51)61270 yds. 27)80 ft. 57 in. 530 cords 53 c. ft. 2)

2 c. yds. 26 c. ft. 57 c. in.

11)122540

40)11140 per.

8)278 fur. 20 per.

3)34 m. 6 fur. 20 per.

11 lea. 1 m. 6 fur. 20 per.

(14) (15)sec. qts. 60)3561829 4)1597 8)1000

60)59363 m. 49 sec. 2)399 gals. 1 qt. 125 cords.

24)989 h. 23 m. 49 s. 4)199 pks. 1 gal. 1 qt.

7)41 d. 5 h. 23 m. 49 s. 49 bush. 3 pecks 7 gal. 1 qt.

5 wks. 6 days 5 hrs. 23 min. 49 sec.

(17)(18) (19) sq. links. secouds. grs. 60)10000 10000)70000 20)11621 60)166' 40" 7 sq. ch. 3)576 ser. 1 gr. 2º 46' 40" 8)192 dr. 1 gr. 12)24 oz. 1 gr.

2 lbs. 1 gr.

(20) sq. ft. 9)26025

301)2891 yds, 6 ft. 4.764

121)11564 quarter yards.

95 per. 69 quar! yds. 6 ft. = 40)95 per. 17 yds. 8 ft. 36 in.

2 r. 15 sq. p. 17 sq. y. 8 sq. ft. 36 sq. in.

Exencise 7-Page 53:

(1) £3×400=1200 cents. £29×400=\$116.00 $7s. \times 20 = 140$ " $18s. \times 20 = 3.60$ 14d.=5 far.×5÷12= $2\frac{1}{12}$ " $3\frac{1}{12}$ d.=14 far.×5÷12= 0.05£. 78. 11d.=13421 cts. £29 18s. 31d.=\$119.65%

> (3) WEEK ! 114d.=45 far. ×5-12=181 ctg.

£69×400=3276-00 18s.×20=\$3.60 15s. × 20= 3.00 8id.=34 far. × 5:12= .14i 6d.=24 far.×5+12= 10

£69 15s. 6d.=\$279·10

18s. 81d.=\$3.741

2d.

3d.=:

6=12 \$169

2037

66112

18 = £ B.

80 5

60 15

\$116.00 3.60 -058

\$119.658

=\$3·60 = ·14}

(NAT. AMITM.	EXERCISES 6-18.]	KEY.	1
,	(6) £17×400=	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	.(7) £87×400= \$ 348·00
eral gra	₹d.==23 far.×5+12=		(8) () (1) (1)
lr. 1 gr.	£17 16s. 5‡d.=	\$71·29 7 112d,=47	15s.×20=\$3·00 far.×5÷12= :197
z. 1 gr.	. ') 	15s. 112d.—\$3·19-7
os. 1 gr.	£16×400:	= 1.20	
	£16 6s. 2d.:	=\$65·23}	£2 9s. 11d.—\$9.98}
•			
	E	KERCISE 13—Page'S	00.
	- (1)	(3)	(4)
36 sq. in.	6=12 + 3 121=11 ; \$169 78 7963	× 11 144=12 × 42.3 \$3346	12 648=12 × 9 × 735

	(1)	(4)	(3)	(4)
	6=12 + 3 \$169.78	121=11 × 11 1 796342.3	\$33460 12	18=12 × 9 × 6 735 12
	2037-33	8759765-3 11	401520	8820
	6112.08	96357418:3	\$4818240	79380
	3 7 6	22 = 11 × 2 8	£ s. d. c	wt. qrs. lbs. oz.
2	0 5 0	62 19 111	32 5 10 1	07 0 15
60	9.15 0	125 19 11	290 12 6 6	42 1 4 10

2615 12:16

		[NAT. ARITH
bush. pks. gal. qt. pt. yds. 26 3 1 1 1 7	(10) 3 = 9 × 7 5. qrs. na. in. 2 2 2 9	(11) 288 = 12 × 12 × 2 dys. hrs. min. sec. 5 17 33 11 12
7	0 2 0	68 18 33 12
1319 0 1 1 1 168	3 2 0	825 7 38 24
	,	1650 15 16 48
EXERCISE	14-Page 9	. .
$83 = 3 \times 10 \times 8$		(2)
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	•	$\theta = 10 \times 10 \times 10 - 1$ £ s. d. 963 0 03
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		9630 0 71
1000 15 0		96300 6 3
		963003 2 6 963 0 0‡
		962040 2 51
$\begin{array}{c} (3) \\ 178 = 8 + 10 \times 7 + 10 \times 10 \times 1 + 10 \times 10 \times 1 \\ £ s. d. £ s. d. \\ 3 6 5 \ 1 \ \times 8 = 26 11 6 \end{array}$	16 3	(4)
33 4 41×7= 232 10 71	168 3	0×7= 1181 1 0
332 3 9 ×1= 332 3 9	1687 2	0×8=10125 0 0
21 17 6 ×3=9965 12 6		11441 1 0

10556 18 4

F 10		
PATE	A Districtor	
Fortant.	ARITH	×

[NAT. ARITE
(11) = 12 × 12 × 2 ys. hrs. min. sec. 5 17 33 11 12
8 18 33 12
7 38 24
15 16 48
(2) 0 × 10 × 10—1 £ s. d. 963 0 02 10
9630 0 71 10.
3300 6 3
963 0 0‡
040 2 5‡ 0) 17+10×10×6

bush. pk. gal. 135 0 0

= 1181 1 0

=10125 0 0

11441 1 0

				(5				
	2	47 =	7+	10×	4+10	×10;	×2.	
1111	ur	. ras.	yas	•	m.	fur.	rds.	yds.
23	6	33	10	×7 =	= 166	7	36	01
238	4	17	14 10	×4=	= 954	1	29	04
2385	4	12	4	×2=	4771	0	25	21
		٠.		(6)	5892	2	10	31
	7:	21 =	1+	10×2	-10°	× 10 ×	17	
8.	ueg.	min.	500	• '	8.	deg	main	. #80.
3	16	30	45 10	$\times 1 =$	3	16	30	45
35	15.	7	30	×2=	71	0	15	0
355	1	15	0	×7=	2485	8	45	0

2559 25 30

Exercise 15-Page 93.

7071 556	15607 3094	(8) 39948123 6007	(9) 2778588 9867
42426 35355 35355	62428 140463 468210	279636861 23968873800	19450116 16671528 22228704
3931476	48288058	239968374861	25007292
	A 44		27416327796

Exencisa 16-Page 95.

(4)	(5)	(6)	(7)	(8)
3.2517	64.001	482000	3782.4	87.96
.023	340	.87	.00917	220
97551	2560040	3374000	264768	175920
55034	192003	1446000	37824	17592
747891	21760.340	178340.00	340416	19361.20

Exercise 17-Page 100.

(1)	(2)	(3)	# (d)
216=6×6×6 \$83469	\$61135.37 229	258226 143	176=11×8×2
6	55021833 12227074	765678 1020904	2037 36
500814	12227074	255226	2241996
3004884	\$13999999.73	36497318	8
6	ET TOTAL SE EN	STOPPEN TO SERVICE THE	17928768
\$18029304			35857536
(5)	6 (6)	26 (7) 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	(8)
116700 235	3721 73	$297 = 11 \times 9 \times 3$	
583500 350100 233400	11163 26047	352000	65408000
	271633	9	5
27424500	<u>.</u>	3168000	327040000
		9504000	

(9)

749=9+10×4+10×10×7 999998=1000000-2

lbs. ox. drs. ser. gr. lbs. ox. drs. sers. grs.

123 4 7 2 17×9= 1110 8 7 1 13 1698732
10 1000000

1234 1 7 1 10×4= 4936 7 6 0 0 1698732000000
10 3397464

12341 7 3 0 0×7= 86391 3 5 0 0 1698728602536

EXERCISE 17.]

(4)	
6=11	×8×2

17

203736 11 2241996

17928768

35857536

(8)

327040000

7902

(10)

8=1000000-2

1698732 1000000

1698732000000 3397464

1698728602536

(1	1)	II.		₩.	64 Estate Library	(12)
640 = bush. 1 123	pk.	gal.	qt.	8 pt.		89
	-11			10		267
1234	0	1	3	0		623
				8		\$64.97
9873	3	0	0	8		
78990	Δ	0	^	_	7	

(13)

yds. qrs. na. in. yds. qrs. na. in. 7 3 2 1 × 3 = 23 2 3 02 79 0 $0 I \times 4 = 316 0$ 12 .10 $0.1 \times 1 = 790$ 790 10

> 9032 3 (15)

\$968.49 3.4 387396 290547

\$3292.866

(14) $1143=3+10\times4+10\times10\times1+10\times10\times10\times1$ 1634-5789 635000 81728945000 49037367 98074734 1037957601.5 $0 1 \times 1 = 7902 3 0 1$

> \$3292.866 3.7

23050062 9878598

3.12183-6042 12183.6042

3292.866 968.49

\$16444.9602

5)3'

Exercise 18-Page 110.

(9)	10 10 10 10 10 N
6423)798 9 65(124)	£ s. d. 12)176 14 6
15666 12846	14 14 76
28205 25692	
2513	
(11) 741)56789(76427 5187	(12) 7894)6785158(859 1811 63152
, 4919 , 4448	46995 39470
478	75258 71046
	4212
£ s. d. £ s. d.	(14)
1714700 30 000	397896·64(\$228·19313
1558 1268 6)970763 290 20 161793-8333+	858 1209 47600)977076(2025075 858 95200
5816 a 2013 to 10 15 1 2 3 3 17 17 17 17 17 17 17 17 17 17 17 17 17	3516 3432 25076
2646 2536 (16) 110 • 9)71234	84-6 42-9
7914	41·74 38·61
1268	3·13

Exercisms 18, 19.]

•	14	7	61
3	#. 14	7	d. 6
1	0		*

(12) 58(8591811 5 0 -58 66 -2

19<u>113</u> 7) 7076(20<u>14878</u> 200 076

	(18)		1	0	719\7	(20)	
lbs. 98)7289 498	or. drs.	or. grs 2 13	. lbs. oz. d 3(14 7	re. scr. grs. 5 0 124	37 -	9807	10 9414
2309 1992			19)	-0		9712	
317 12	487	£)157 20	s. d.s. 16 7(6	63489	i ilin	(21)	
3810 3486		3156 2922		37)	m. fur.	rds. m.	fur. rds. 3 14
324		234 12	n' Mi	e e e	15		
2596 2490		2815 2435	na gr		23		ı
.103		380			12 40		
320 20		520 461 .			18		
6413 5976	* 1.5. \$1.5° 7.5° \$1.5°	59			48 48		
437							

Exercise 19-Page 112.

25=5×5 5)3766	(2) 42=7×6 7)26406	(3) 96=12×8 12)25431	24=1 £ 12)24	B.	d.
5)753 1	6)3772 2	8)2119 3	2)2	1	51
150 3 3×5+1=16 15015	628 4 4×7+2=30 62829	2647 7×12+3=87 26483	1	0	81

54

7673

(5) 49=7×7 £ s. d. 7)740 12 4	(6) 56=8×7 £ s. d.	(7) 35=7×5 7)6789436
7)105 16 211	7)68 9 01	5)9699193
15 2 3\frac{1}{4}\frac{1}{48}	9 15 63	4×7+3=31 193983}}
147=7×7×3 7)753293 7)107613	. 9)	81=9×9 lbs. oz. dwt. grs. 1798 6 11 9
3)15373		9)199 10 1 63 22 2 9 06 6×9+3=57
1×7×7+2×7+2=65 5124,667	22 lbs.	2 oz. 9 dwt. 0{ grs.

Exercise 20—Page 114.

491 11 20	(1) 2. d. £ 2 01) 8968		m. fur. rd: 17 5 27	(2) m. fur.) 1027	rds. 1 6
9832	179373 12		141 40	8217	
117984	2152483	5	667	328686 28335	(58
471937		(18114884		45336 45336	
₩ o 1977K ages	3890564 3775496		•		
	115068		•		

	**************************************		KRY.		19
(7) 35=7×5 7)6789436 5)9699193 1939834 4×7+3=31 193983;; (9)	1140 12	£ 8.	d. dwt 10j 5 24	grs. (4) grs. lbs. oz. d 9 9 9 12 117 20 2343 24	wt. grs. 3 12
=9×9 dwt. grs. 11 9	54750) 1642 1642	150 (3 150	12	9384 4686 9)56244(436 516	
0 1 63		•		464 387	
2 9 06 ==57 dwt. 0{{ grs.				774	
		DAMROINE 5)	21-Page 11		
ı	91 0 6)		per. 4	(6) 17·655 : 4 ·5= (5)476·55(10·59	
(2) m. fur. rds.) 1027 1 6 8	364 40 14566) 3	9467 40 78716 (26 9132	A SECTION OF	26·5 22·5 4·05	
8217 40		87396 87396		4.05	
828686 (58 28335 45336	756·98 + 76·736 7673612)75698000 (69062508	12 = 9·864 +	• 47· 2617	(8) 5782975 ÷ 26·1 5)47578·2975(1 26175	75 = ·8177
45336	6635492·0 6138889·6	•	· .	21403·2 20940·0	
	496602·40 460416·72		•	463·29 261·75	*
	36185-68 30694-44	8		201-547 183-225	
	5491-23	2		8225	b

, , , ,	
(9)	(10)
$\begin{array}{c} 1 \div 7.6345 = \\ 76345)10000.0(0.1309 + 3829) \end{array}$	5·347÷0·3829 =)753470(196·7798 +
76345) 10000-0(0-1309-1 3829	3829
10010	
2365.50	37057 (11) 34461
2290.35	
The state of	20000
75.1500	22974 8)200000
68.7105	2986.0
•	2680.3
\$ 100 M	305.70
	268.03
	37.670
	34.461
	3.2090
	3.0632
	*1458
Exercise 27	Page 116.
(1)	(2)
95)\$3300000(\$34736.8421	126)\$3860000(\$30634.9206
285 (3)) dys. 378
28800)9527040	00(3308
450 86400	800
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(5)		(6) ···· (149) .	(7)
27475271)\$3764112127	(\$137 9)\$	972 108)	3972(\$9
27475271	asa ta Profit	100	973
101658502	Table that the	108	(10)
82425813	(9)	1728\1	(10) 000(-578 o
	792)340480(4	12912 oz.	864.0
192326897	3168	and the state of the	-
192326897	* * * * * * * * * * * * * * * * * * * *	The state of the	136.00
(8) Mp. 14. M	2368	Children of the last of the la	120.96
294)\$8526(\$29	1584	(12)	
588 (11)		9)4750(250 lbs.	15.040
— m. fur.	7840 7128	38	13.824
2646 8	1120	. 95 mm 38	1.216
_ 111	a 712	95	1 210
266 - 20-1	761=88		
. 40	*/	(14)	
		al. qt. pt. bush. p	k. gal. qt. p
	297)729 1	1 1 1 (2	1 1 2 1,
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5320	135		Santana 🕶
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	594		
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481738·10	175		
70565-700	- 1		
67443.334	351		
7122000	297	· · · ·	
3122-366			
	54 54	-2-	

ibe. cs. dr. cwt. qr. ll 9 7 8) 179 3	bs. os. dr.	1.	١
151 Variable 719 16 variable 25	m. fq1 93 4 8	(16) r. rds. m. 7 25000	
914 AAA 3599 151 A 41 1438	748 40	200000	
2424 . 4 534 17979	29927 2	9927) 8000000 (267 59854	hrs. 718884
107890 17979	' 10	201460 179562	
287680 16		218980 209489	
1726080 287680		9491 24	
2424)4602880(1898 3)	89	37964 18982	,
21788		227784 209469	
23968 21816		18295	
21520 19392	. *	, n	
2128 313	₹= 38 5.	`	

Exercise 23-Page 118.

(3)

DOGIX, MVOCCERRYI, MXCMXCIX, EXXXVMIV, MMMOMXLVMMDXCVI.

dys. hrs. 0(267 718384

```
(4)
                            17=7+10×1
72=8×9
 lbs. oz.
                          s. d. £ s. d.
 749 10
 5997 0
                       £2.6 51+1=2 6 81
                                3 18 112
53973 0
      (6)
  30)2850000000
            - days, hrs.
    24)95000000(3958333 8
      230 3654)3958333(10837
      140 1461)15833332
120 1461
                1461
               12233
       192
               11688
              5453
4383
        72
          80
                10702
          72 10227
           80 4)475 quarter days.
          72 days. hrs.
1182=118 18
           8 rem. Add
                        119
```

10837 yrs. 119 days, 2 hrs.

•		(8)
£729×400 17s.×20	=\$2916·00 = 3·40	\$10000
61d.=25 far.×5	÷12= 10-	9876-23
	\$2919-50-	\$128.77

XVMIV.

674

(10)	(11)
in.	\$729-43
12)7964327	16.70
	976-81
12)663693-11)	9987-17
} 119 in.	429.00
55307— 9) 9)55307 ft. 119 in.	129-19
301)6145 yds. 2 ft. 119 in.	\$12268.30
121)24580 203 p. 41 v.=	· · 203 p. 4 yds. 2 ft. 36 in.
11)24580 Add	2 ft. 119 in
$\frac{11)2234-6}{203-1}$ 17 qr. yds. 40)203 p. 4 yds, 5 ft. 11 in.
200-1	4)5 rd. 3 p. 4 yds. 5 ft. 11 in.
	1 a. 1 r. 3 p. 4 yds. 5 ft. 11 in.

(12)

wks.	dys. 4	brs.	9+10×2- min. 17×9= 10	wks. 59	dys.	hrġ.	min 33
65	6	8	50×2= 10	131	5	17	40
659	0	16	20×4=	2836	2	17	20
				2827	3	16	33

wks.

52)2827(54 yrs. 19 wks. 3 dys. 16 hrs. 33 min. 260

227 208

19 wks.

	al					
			(15)	•	(16)	
			tong.			100
			324	\$136×4=	44QK-	136
			20	A100 X ===		902
	7.		r. lbs. —		_	
		13 2	14 6480		2	487 275 39
		4	4.			
		54	25920	\$9237-\$2	347=\$675	0
		25	25		(1 m)	
					vds.grs.n	a. yds.qrs.na.
		284	129600			2)39 2 3
		108	51840		4	4
	1.0	1004			- c	
		1364)648000(475	1384=	13	158
		(14)	5456 475	Mathds.	4	4
		78-96	10240	\$	54)	628/1141
in.		.00042	9548		54)	635(1144
444.	10.			1		
		5792	6920			95
	31	584	6820			54
	033	31662	100			. ,
	,00	21002	100			41 . 6
,						
			•			
		(10)	(10)			
	'	(18)	(19)		(2	1)
	a.	8. 8.	T DAN		44	• .
	25	732 96	r. per. 3 17		108. 02	dwt. grs.
	197	674 4	• .,	(20)	12)36 8	14 16
	156			\$	3 0	14 13
	97	58 387		20 \$312		10,
	199	. 40		75 275		4
	674	15407	27764.06@0. FOI	97	(22	•
		10491)	\$7764·0(\$0·501 77 48 ·5	83 \$ 37		r. per.
			11200	275		3 12 2 0
			15.500	210		0 13
			15.497			2 36
			3		29	- 21

36 in. . 119 in

. 11 in.

. 5 ft. 11 in.

yds. 5 ft. 11 in.

. min. 33

40

20

33

min.

\$247.95

Ex

96 191 201

(23)	1	(24)			(25)	. '
5 7 9 —, N 0%	3 3.45.42.4	os. dwt. 9 8 2 16 6 17	0	11s.=45 far.)	2×400=3: 1×20= ×5+12=	3888·00 2:20 ·18‡
21)294() 21 84 84	14 1 15 15 15 16)		22 14 (27)			3890·38≹
	oz. drs. : 3 3	or. grs.	25 280 112 1400	100 100 100 100 100 100 100 100 100 100	0 7 1 17	lbs. = 24 01
3 51634 20 032694	scr.		2 2800 s 6 16800	l. ft. in ro	of.	12005 2401 360·15
	29 57 203 145 1653		\$ 139468 98573 \$238047	23	0129 8047 2082	
	8265 1653				. •	

. 3	
	888-00 2:20 ·18‡
\$3	890-38
	£
) ;	
. lbs. 11 16 7	
1=	lbs.
111	. 15

12005 2401 \$360.15

ELECTION A	10-1	n.n.r	• '			41
20	(31) 2 £ s 3 11 1694 1 20 1=12	#1=11	111d=	=47far	3) cwt. qr.	\$79-99-7
201579)34167190(1 201579	69-49	8 0	\$ 1 · 3	3 3	— ·lbs. 24=399 ·15
	1400929 1209474					1995
	1914550 1814211		•			\$59-85
•	100339·0 80631·6					
	19707·4 18142·1					
	1565-2	9				
cwt. c	(34) pr. lbs. 0 17 2 15	4s			,	•
5	1 20 3 17 1bs. 0 19=1419	•	,	43 ⁻ 76843 ⁻	(36) •2÷76·84 7)432000 384218	· 0(0· 562
	9933 4257	71			4778 4610	
	7091				1675 1536	
	\$532.12			*	138	406

1234000000000;-66 6)1234000000000	\$63·29 \\$2789·27 17 1075·93
11)20566666666666	44303 \$1713·34 6329
1869696969.69	\$1075.93
****	(39)
	0 11 11 16 417 16 91 11 27
117:8	2110·40 723·15 117·39 ₁ 7 ₅
	173) 3657·80 ₁ 7 ₄ 12 12
(40)	2076)43893·67(\$21·1433 4152
2076)491544(236 1 9 4152	2373 2076
7634 6228	297·6 207·6
14064 12466	90·07 83·04
1608 1898=193	7·030 6·228
	·8020 ·6228
	1792

38	3)			
3		52	78	
			_	

\$1713.34

78.43 17.16 11.27 10.40 3-15

17-397 7.807 12

3.67(\$21.1433

0.07 3.04

.030 228

.8020 6228

1792

Exercise 24-Page 127.

(1)	(2)	(3)	(4)
2)11368	2)2934	3)1011	2)1000
2)5684	3)1467	337	2)500
2)2842	3)489	3×337	2)250
7)1421			5)125
7)203	2×3³×163 (€		5)25
29 2 ³ ×7 ² ×29			2 ³ × ³ 5
(5)	(6)	(7)	(8)
2)1024	2)32320	7)707	2)1118
2)512	2)16160	101	13)559
2)256	2)8080	7×101	43
2)128	2)4040		2×13×43
2)64	2)2020		
2)32	2)1010		, '
2)16	5)505		
2)8	200 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		
2)4	26×5×101		
2 210			

Exercise 25-Page 128.

(1)

 $100=2^{9}\times5^{2}$

1..5..25

1..2..4..5..10..20..25..50..100

Ô.

(2)

810=34×2×5.

1..3..9..27..81

1..2

1..3..9..27..81..2..6..18..54..162

1..5

1..3..9..27..81..2..6..18..54..162..5..15..45..135..405.. 10..30..90..270..810 =

1..2..3..5..6..9..10..15..18..27..30..45..54..81..90..135.. 162..270..405..810.

(3)

920=23×5×23.

1..2..4..8

1..5

1..2..4..8..5..10..20..40

1..23

1..2..4..8..5..10..20..40..23..46..92..184..115..230..460..920= 1..2..4..5..8..10..20..23..40..46..92..115..184..230..460..920.

(4)

25000=55×22

1..5..25..125..625..3125

1..2..4..8

 $\begin{array}{c} 1..5..25..125..625..3125..2..10..50..250..1250..6250..4..20..100..\\ 500..2500..12500..8..40..200..1000..5000..25000 =\\ 1..2..4..5..8..10..20..25..40..50..100..125..200..250..500..625..\\ 1000..1250..2500..3125..5000..6250..12500..25000..\end{array}$

Exercise 26-Page 128.

(1)

(2)

88200=23×32×52×72 3+1=4

2+1=3

2+1=3

2+1=3

3500=2°×5°×7 2+1=3

3+1=4 1+1=2

3×4×2=24

4×3×3×3=108

.45..135..405,. 4..81..90..135..

.230..460..920= ..230..460..920.

50..4..20..100.. 0..25000 = .250..500..625.. 25000.

×5³×7 =3 =4 =2 2=24

(4) (3) 824=23×103 6336=26×38×11 3+1=4 6+1=7 1+1=2 2+1=3 1+1=2 4×2=9 7×3×2=42 (6) (5) 49000=23×53×75 81000=23×34×53 3+1=4 3+1=4 4+1=5 3+1=4 3+1=4 2+1=3 4×5×4=80 4×4×3=48 (8) (7) 25600=210×52 $75600=2^4\times3^3\times5^3\times7$ 10+1=11 4+1=5

Exercise 27-Page 129.

3+1=4

2+1=3 1+1=2 5×4×3×2=120

(3) (1) (2) 26= 2× 21= 7×3 21= 3× 7 $52 = 2 \times 2 \times 13$ $18=2\times3\times3$ 77=11× 42= 2×3×7 91= 7× 13 $27 = 3 \times 3 \times 3$ 143=11× $36=4\times3\times3$ 35= 5× 3 is common to all. 7 is common to all. 13 is common to all.

2+1= 8

11×3=33

(4) 82=41×2 118=59×2

146=73×2
2 is common to all.

Exercise 28-Page 130.

107(1 296	308)506(1 308	74)84(1
111)296(2 222	198)308(1 198	10)74(7
74)111(1	110)198(1	4)10
37)74	88)11	0(1 200 200 200 200 200 200 200 200 200 20
G. O. M. = 3	7,	12)88(4 G. O. M
		88 M, = 22.

1908\00000000000000000000000000000000000	(5) (5)
1825)2555(1	6)672(1
1825	556
730)1825(2	116)556(4
1460	464
365)730(2 730 G. C. M.=365.	92)11

24)92(3
72
20)24(1
20
4)20(5
G. O. M. = 4.

```
(3)
```

0.

74)84(1

10)74(7

4)10(2

(1 2)4

88(4 G. O. M.=2.

H. = 22.

2(1 | 8

3)556(4 464

92)116)1

24)92(3

20)24(1

4)20(5

G. C. M. = 4.

EXERCISE 29-Page 131.

(1) (2) 110)140(1 1326)3094(2 110 2652 30)110(3 442)1326(3 90 1326 20)30(1 Also 4420 is divisible by 442; 20 therefore it is their G. C.M. 10)680 10)20

68 2 Therefore 10 is their G. C. M.

(3) 468)922(1 (4) 204)1190(5 34)1445(42 468 1020 136 454)468(1 170)204(1 454 170 68 14)454(32 34)170(5 17)34(2 42 170 34 34 17)2006(118 28 17 6)14(2 30 12 17 2)6 136

375 is not divisible by 2, and therefore their G. C. M. is 1.

Exercise 30-Page 132.

(2) $56=2^3\times 7$

136 G. C. M.=17.

 $84=2^{2}\times3\times7$ $140=2^{2}\times5\times7$

 $168 = 2^3 \times 3 \times 7$

The greatest factors which are common are 2² and 7; therefore the G. O. M.=2²×7=28.

(3) $241920 = 2^{8} \times 3^{9} \times 5 \times 7$ $380160 = 2^{9} \times 3^{3} \times 5 \times 11$

 $69120 = 2^9 \times 3^3 \times 5$ $103680 = 2^8 \times 3^4 \times 5$

The greatest factors which are common are 2^8 , 3^3 and 5; therefore the G. C. M.= $2^8 \times 3^3 \times 5 = 34560$.

(4)

 $10800 = 2^4 \times 3^3 \times 5^2$ $28040 = 2^3 \times 5 \times 701$ $2160 = 2^4 \times 3^3 \times 5$

The greatest factors which are common are 2³ and 5; therefore the G. C. M.=2³×5=40.

Exercise 31-Page 133.

(2) (company (2))	(3)
6=2×3 4 / /	1=1 6=2×3
7=7	2=2 9=38
42=2×3×7	3=3 12=2°×3
. 9=3° is A W. M.	4=2° 15=3×5
10=2×5 600 (1)	5=5 18=2×3°
$630 = 2 \times 3^2 \times 5 \times 7$	6=2×3 21=3×7
	7=7 30=2×3×5
$2\times3^2\times5\times7=630.$	8=23
•	$9=3^{2} \times 3^{2} \times 5 \times 7 = 1260.$

 $3^{3} \times 2^{3} \times 5 \times 7 = 2520.$

(5) (6) $670=2\times5\times67$ $8=2^3$ $100=2\times5$ $335=5\times67$ $18=2\times3^2$

25=5° 27=3° 36=2°×3° 2°×5°×67=6700 44=2°×11

 $44=2^{2}\times11$ $396=2^{2}\times3^{2}\times11$ $2^{3}\times3^{3}\times5\times11=11880$ 28, 33 and 5;

re 2³ and 5 ;

(4) 6=2×3 9=3° 12=2°×3 15=3×5 18=2×3° 21=3×7 30=2×3×5

 $3^{\$}\times5\times7=1260.$

×5 ×3² ×3² ×11

 $\times 3^{2} \times 11$ $\times 11 = 11880$ Exercise 32-Page 134.

2)12..10..24 2)14..21..3..2 .63 2)18..12..39...

2) 6.. 5..12 3) 7..21..3..1..63 2) 9.. 6..39..

3) 3.. 5.. 6 7) 7.. 7..1..1..21 3) 9.. 3..39..

1.. 5.. 2 1.. 1..1..1.. 3 3) 3.. 1..13..

 $2\times2\times3\times5\times2=120$ $2\times3\times7\times3=126$ 13) 1.. 1..13..

(4) 2)8..18..15..20..70

2)4.. 9.. 15.. 10.. 35

3)2.. 9..15.. 5..35

5)2.. 3.. 5.. 5..35

2.. 3.. 1.. 1.. 7 2×2×3×5×2×3×7=2520

(6) 2)60..50..144..35..18

2)30..25.. 72..35.. 9

2)30...20... 12...30...

3)15..25.. 36..35.. 9

3) 5..25.. 12..35.. 3

5) 5..25.. 4..35.. 1

1.. 5.. 4.. 7.. 1 2×2×3×3×5×5×4×7=25200. 1.. 1.. 1.. 2×2×3×3×13+

2)24..16..18..20

2)12.. 8.. 9..10

2) 6.. 4.. 9.. 5

3) 3.. 2.. 9.. 5

1..2..3..5 $2\times2\times2\times3\times2\times3\times5=720.$

(7) 2)27..54..81..14..63

3)27..27..81.. 7..63

3) 9.. 9..27.. 7..21

3) 3.. 3.. 9.. 7.. 7

7) 1 2 7 7

7) 1.. 1.. 3.. 7.. 7

1...1...3...1...1 $2\times3\times3\times3\times7\times3=1134$,

Exercise 33-Page 136.

(1) 300 800...200...150...50...60...75...125 165 20...60...15...165...210...63...27 10 2 5 21 4... 4 14...21... 9 12 4... 4 14...21... 9 300×10=3000. 165×21×12=41580.

		(3)		
144	12	3214	460.	.96	1728
1.2	7/3	11	5	2	13
55	+ olympie t	11	5		
	144×	(12×55	=95040),	

	Express 34-	-Page 138.	
(1) 12)592835	(2) 5)3700	(3) 11)10000	6)1000000
12)49402	5)7400	11)3091	6)1666664
12)4116t	5)1480	11)827	6)277774
12)3430	5)293	75	6)46293
12)287	5)54	7571.	6)7713
24	10	The same of the same of	6)1283
2470te	104300.	The state of the s	6)212
(5) 8)10000	(6) 12)12345654321	9)10000	33233344 (8) 2)300
8)12500	12)1028804526	9 9)1111	1 2)1500
8)1562	12)85733710	6 9)123	.4 2)750
8)194	12)7144475	9)13.	2)371
23	12)595372	transferming	2)181
23420	12)49614.	.4 - 146	41 - 2 2)90
	12)4134.	.6 azje.,	2)41
	12)344.	.6	2)20
	12)28.	.8	10
	2. 24866	.4 4e/69	100101100

Exercise 35-Page 139.

(1)	(2)		(3)
118		Ý	17
8)37704	7)444	7)4321	9)1212201
8)43115	7)325	7)3135	9)231210
8)4801	23	7)216	9)11010
8)544		14 1465.	9)210
61 61415.		,	10000.
	-		

Exercise 36-Page 140.

(1)	(2)	(3)	(4)
IV .	m	IX	
20212331	101202220	1522365	33233344
4	3	9	6
8	3	14	21
. 4	3 3	9	6
_	••	CHANGE .	
34	10	128	128
4	3	9	· 6
-	-		
137	32	1154	771
4	3	9	. 6
			-
550 .	96 /	10389	4629
4	3	9	6
0000	-	00505	27777
2203	290	93507	6
4	3	9	•
8815	872	841568	166666
0010	512	941900	6
4	3		
35261	2618 3		1000000
	7854		

6)166666..4

6)27777..4

6)4629..3

6)771..3 6)128..3

6)21..2

33233344

(8) 2)300

.1 2)150..0

4 2)75..0

.6 2)37..1

4 ... 2)18..1

1

2)9..0

2)4..1

2)2..0

1..0

100101100

(6)

	(0)	y 1
1X	IX	13
3)132713	12)132713	8)132713
3)408340	12)102079	8)147571
3)132711	12)682t	8)16520
3)40831	12)518	8)1846
3)13270	3. t	8)215
3)4081		23
3)1322	· •	,
3)402		
3)130		
3)4.10		
11		,
TW 5.1	d	

ix 1000	. 111	ı	XII	1	VIII
132713 =	= 110	002210110 =	= 31819	= 2	35601
9	3		12	8	77
-			·		'
12	4	332	46	19	
9	3	. 3	12	8	
	-		-		
110	1.2	997	560	157	
9	3	3	12	8	
***********	-	-			
997	36	2991	6730	1262	
9	3	3 *	12		
-	-	`	1.2	8	
8974	110	8974	80769 den.	10096	
9	3	3	oo too den.		
				8	
0769 denom	920	0.0000		solo establishment	
0769 denary.	552	26923		80769	denary.
		3			

80769 denary.

IIX

(7)

(Continued on next

		, ,	
1 X .	xii	XII	XII
3)132713	9) t2t290	6) t2t290	4) t2t290
8)147571	9)1179780	6)1858560	4)268683
8)16520	9)1624t2	6)34e4e0	4)78180
8)1846	9)20324	6)69 t95	4)1e050
8)215	9)2842	6)11793	4)5913
23	9)371	6)2333	4)1533
	47	6)463	4)43
		6)90	4)10
		13	4):
VIII 235601 8			4
157 8 262 8			
769 denary.			

) t2t290	2) 121290
1)2686830	2)5151460
4)781803	2)2686830
4)1e0500	2)1343411
4)59130	2)781801
4)15333	2)3t0 t00
4)4393	2)1e0500
4)10e1	2) e6260
4)323	2)59130
4)92	2)2 1671
21	2)15331
	2)8771
	2)4391
	2)21 t1
	2)10 e0
	2)651
	2)321
	2)170
	2)91
	2)41
e ,	2)20
page)	10

(7 continued.)

· II	, ,	14	K ' VI	KII . I	,
11011111000	30=100110	500=21231330	420=13088	290=4712	t2t
	2	4	6	9	12
1243	2	9	9	43	100
1243	2	4	6	9	122 12
	_		_		
2487	4	38	54	388	1474
2	2	4	6	9	. 12
4975	9	155	327	3494	17690
, 2	2	4	6	9	12
9951	19	621	1965	31450	212289
2	2	4	6	. 9	12
19902	38	2487	11793	283052	547468
2	2	4	6	9	
39804	77	9951	70763	547468	_
33009	2	4	6	041400	4
*					
79608	155	39804	424578		•
	2	4	6		
159210	310	159216	2547468		
:	2	4 .	-01110		-
318423	621	636867			
/ 2	2	4			
63686	1243	547468			
2					
1273734					
2					
2547468					

			Express 3	7—Page 142.	
	,	(1)	(2)	(3)	(4)
•	п	VI	XII	m	VIII
100116	01101111100001100	252	62te)32e75721(62te	201210	57264
		252	31556	102221	675
2			101 7	21015	
2	1243	544 2224	161e7 1059t	21212	354604 513354
2	2	544	10091		434070
_		011	58192		
4	2487	122024	52512		51117344
2	2.00 2				
9	4975		58801 58801		
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EXERCISE	38	Page	140
TOTALITY	00-	rage	146.

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774=1096 com. scale,

300

240

(6) 25 ft.=300 in. 20 " =240 "

2 ft. 6 in.= 30 "

(4) 4 ft. 5‡

20 1

21 sq. ft.

(5) XII 4.78

9.6

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8 6		cish 40—Page	149.	33750
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(3)
$243000 = 2^3 \times 3^5 \times 5^3$
3+1=4
4+1=5
3+1=4
$4\times6\times4=96$

	4×6	×4=96
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8)134231	5)223032	15562 12756
8)10241	5)35321	28060 25512
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(7)

5.7.9.11.15.18.20.21.22.24.28.20.33.25.26.40.42.44.45.48.50. 7.9.11. 8. 9. 21.11. 8. 7. 8.28. 7. 9 21.11. 9. 6. 5. 8.11. 8. 11. 11. 8 11. 8. 2. 5.

 $40 \times 21 \times 33 \times 10 = 277200$.

(9)

9999993000 = 10000000000 - 7000. $64276 \cdot 3427 \times 10000000000 = 642763427000000$ $64276 \cdot 3427 \times 7000 = 449934398 \cdot 9$

642762977065601-1

(10)

IX	1X
5)78263	11)78263
5)152303	11)64303
5)27600	11)5266
5)5114	11)430
5)1020	36
5)173	, santana
31	

IX II 7)78263 7)3130403 = 7)36063 7)11160..3 7)214200..3 7)5640..3 7)1407..5 7)13220..5 7)884..5 7)177..3 7)1101..3 7)128..3 7)23..4 7)41..4 7)1t..43.,0 3..0

5) 42÷00006378= 9000(1243994·982%

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	54 27)54(2			81)162(2 162
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		16383	

74002702 ÷ 144 = 513907 ft. 94 in. 513907 ft. $\div 9 = 57100$ yards 7 ft. 57100 yds. ÷ 30½ = 1887 per. 18½ yds. 1887 per. 18 yds. 2 ft. 36 in. Add 7 ft. 94 in.

(23)

40)1887 per. 19 yds. 0 ft. 130 in.

4)47 r. 7 per. 19 yds. 0 ft. 130 in.

11 a. 3 r. 7 per. 19 yds. 0 ft. 130 in.

(24)

1728 | 240.. 180.. 1820.. 1728 1728×65×3=386960

Exe

(25)

6 children will have 6 children's shares 4 women will have 4×2=8

3 men will have $3 \times 5 \times 2 = 30$

3 men 4 w'n & 6 chi'n will have 44 children's sha. 4)\$7894:16

11)\$1973-54

\$179.41 $_{1}^{3}_{1}$ = child's share. \$179.41 $_{1}^{3}_{1}$ ×2=\$ 358.82 $_{1}^{6}_{1}$ =woman's share. \$358.82 $_{1}^{6}_{1}$ ×5=\$1794.12 $_{1}^{8}_{1}$ =man's share.

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(31)

 $1064=2^3\times7\times19$.

- 1..7 1..2..4..8..7..14..28..56

1..19

1..2..4..8..7..14..28..56..19..38..76..152..133..266..532..1064-1..2..4..7..8..14..19..28..38..56..76..133..152..266..532..1064

> (32) 30 ft. 6 in. = 366 in. 20 ft. 11 in. = 251 in. 2 ft. 7 in. = 31 in.

732 ____ in. 31)91866(2963)

62 298 279

— 296313÷36=82 €6 yds.

186 106 93 13

196

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31

Exercise 46-Page 158.

(1)

(2)

 $\stackrel{8}{\text{1}}, \stackrel{13}{\text{1}}, \stackrel{6}{\text{1}}, = \frac{8 \times 13 \times 14}{11 \times 13 \times 14}, \stackrel{12 \times 11 \times 14}{\cancel{11} \times 13 \times 14}, \stackrel{5 \times 11 \times 13}{\cancel{11} \times 13 \times 14} = \frac{1456}{2002}, \frac{1848}{2002}, \frac{715}{2002}$

(3)

(4)

(5)

 $\frac{1}{6}, \frac{1}{6}, \frac{1}{6}, \frac{2}{10}, = \frac{5 \times 7 \times 3 \times 11}{6 \times 7 \times 5 \times 11}, \frac{4 \times 6 \times 5 \times 11}{6 \times 7 \times 5 \times 11}, \frac{4 \times 6 \times 7 \times 11}{6 \times 7 \times 5 \times 11}, \frac{2 \times 6 \times 7 \times 5}{6 \times 7 \times 5 \times 11} = \frac{1925}{2310}, \frac{1320}{2310}, \frac{1848}{2310}, \frac{420}{2310},$

(6)

$$\frac{\frac{1}{2}, \frac{2}{3}, \frac{3}{5}, \frac{2}{5}, = \frac{1 \times 3 \times 5 \times 7}{2 \times 3 \times 5 \times 7}, \frac{2 \times 2 \times 5 \times 7}{2 \times 3 \times 5 \times 7}, \frac{3 \times 2 \times 3 \times 7}{2 \times 3 \times 5 \times 7}$$

$$\frac{2 \times 2 \times 3 \times 5}{2 \times 3 \times 5 \times 7} = \frac{105}{210}, \frac{140}{210}, \frac{126}{210}, \frac{60}{210}.$$

Exercise 47-Page 159.

(1)

\$, \$, \$, \$,

The least common multiple of 5, 8, 6, 4, 15 is 120.

The multiplier for both terms of the first fraction is $\frac{120}{8}$ =24; for the second $\frac{120}{8}$ =15; for the third $\frac{9}{8}$ =20; for the fourth $\frac{120}{8}$ =30; for the fifth $\frac{120}{8}$ =8.

Multiplying by these numbers, we obtain 120, 120, 120, 120, and 120.

(2)

2°c, \$, \$, \$0, 18.

The least common multiple of 11, 3, 7, 77 and 33 is 231.

The multiplier for both terms of the first fraction is $\frac{231}{11} = 21$; for the second, $\frac{231}{3} = 77$; for the third, $\frac{231}{3} = 33$; for the fourth, $\frac{231}{3} = 3$; and for the fifth, $\frac{231}{3} = 3$.

Multiplying by these numbers, we obtain $\frac{123}{231}$, $\frac{134}{231}$, $\frac{134}{231}$, $\frac{144}{231}$, and $\frac{1}{231}$.

(3)

The least common multiple of 2, 3, 5, 6, 8, 10, 15, 16 and 30 is 240.

The multiplier for both terms of the first fraction is $^24^0 = 120$; for the second, $^24^0 = 80$; for the third, $^24^0 = 48$; for the fourth, $^24^0 = 40$; for the fifth, $^24^0 = 30$; for the sixth, $^24^0 = 24$; for the seventh, $^24^0 = 16$; for the eighth, $^24^0 = 15$; and for the ninth, $^24^0 = 3$.

Multiplying by these numbers, we obtain $\frac{1}{2}\frac{20}{40}$, $\frac{1}$

 $\begin{array}{r}
 8 \times 5 \times 7 \times 5 \times 18 \\
 \hline
 5 \times 7 \times 9 \times 5 \times 18 \\
 200 17010 7875
 \end{array}$

350 28350 28350

1456 1848 715 2002 2002 2002

 $\frac{7\times13\times7\times2}{1\times13\times7\times2}$

×11×13×7

×13× 7×2

14014

546 572 616 1001 1001 1001

 $\frac{4\times6\times7\times11}{6\times7\times5\times11},$

(4)

3, 70, 26, 11, 48, 28.

The least common multiple of 5, 10, 25, 30, 45, and 60 is 900.

The multiplier for both terms of the first fraction is $\frac{0.00}{8} = 180$; for the second, $\frac{0.00}{10} = 90$; for the third, $\frac{0.00}{20} = 36$; for the fourth, $\frac{0.00}{20} = 30$; for the fifth, $\frac{0.00}{20} = 20$; and for the sixth, $\frac{0.00}{60} = 15$.

Multiplying by these numbers, we obtain \$48, \$38, \$18, \$38, \$38,

(5)

20, 30, 10, 10.

The least common multiple of 20, 30, 40 and 50 is 600.

The multiplier for both terms of the first fraction is $\frac{600}{20} = 30$; for the second, $\frac{600}{30} = 20$; for the third, $\frac{600}{10} = 15$; and for the fourth, $\frac{600}{60} = 12$.

Multiplying by these numbers, we obtain $\S78$, $\S49$, $\S65$ and $\S70$ 0.

(6)

1, 3, 3, 6, 7, 11, 16 23.

The least common multiple of 2, 3, 4, 6, 8, 12, 16, and 24 is 48.

The multiplier for both terms of the first fraction is $\frac{48}{3} = 24$; for the second, $\frac{48}{3} = 16$; for the third, $\frac{48}{4} = 12$; for the fourth, $\frac{48}{6} = 8$; for the fifth, $\frac{48}{8} = 6$; for the sixth, $\frac{48}{12} = 4$; for the seventh, $\frac{48}{12} = 3$; and for the eighth, $\frac{48}{12} = 2$.

Multiplying by these numbers, we obtain $\frac{14}{48}$, $\frac{32}{48}$, $\frac{32}{48}$, $\frac{49}{48}$, $\frac{$

(7)

4, 11, 18, 47, 36, 46:

The least common multiple of 7, 12, 15, 27, 35 and 40 is 7560.

The multiplier for both terms of the first fraction is 75,00 = 1080; for the second, $7\frac{1}{2}$ = 630; for the third, $7\frac{1}{2}$ = 504; for the fourth, $7\frac{1}{2}$ = 280; for the fifth, $7\frac{1}{2}$ = 216; for the sixth, $7\frac{1}{2}$ = 189.

Multiplying by these numbers, we obtain 5400, 4980, 7888, 7888, 1886, and 7818.

[NAT. ARITH.

, and 60 is 900. n is $\frac{n_0 n}{6} = 180$; for the fourth, th, $\frac{n_0 n}{6} = 15$. , $\frac{n_0 n}{6} = \frac{n_0 n}{6}$; $\frac{n_0 n}{6} = \frac{n_0 n}{6}$;

0 is 600. on is $\frac{600}{20} = 30$; 5; and for the

 $\frac{1}{6}$, $\frac{1}{6}$ $\frac{1}{6}$ and $\frac{1}{6}$ $\frac{2}{0}$.

, 16, and 24 is

on is $\frac{48}{8} = 24$; for the fourth, $\frac{1}{8} = 4$; for the

38, 28, 18, 18,

and 40 is 7560. ction is 7560 = $\frac{60}{6}$ = 504; for the sixth,

10, 4288, 7888,

(8)

18, 3, 1, 11, 11, 18, 9, 18.

The least common multiple of 15, 8, 3, 12, 11, 20, 7, and 35 is 9240.

The multiplier for both terms of the first fraction is $^{2}_{1}^{10}$ = 616; for the second, $^{2}_{3}^{40}$ = 1155; for the third, $^{2}_{3}^{40}$ = 3080; for the fourth, $^{2}_{1}^{40}$ = 770; for the fifth, $^{2}_{1}^{40}$ = 840; for the sixth, $^{9}_{3}^{40}$ = 462; for the seventh, $^{9}_{2}^{40}$ = 1320; for the eighth, $^{2}_{3}^{40}$ = 264.

Multiplying by these numbers, we obtain $\frac{3627}{3276}$, $\frac{3276}{3276}$,

Exercise 48-Page 160.

(1)

\$ of
$$\frac{3}{5}$$
 of $\frac{3}{10}$ of $\frac{3}{12}$ = $\frac{4 \times 3 \times 6 \times 35}{7 \times 5 \times 11 \times 72}$ = $\frac{2520}{27720}$ = 1^{1} f.

(2)

$$\frac{2}{3}$$
 of $\frac{4}{9}$ of $\frac{6}{7}$ of $\frac{61}{100}$ of $\frac{25}{24} = \frac{2 \times 4 \times 6 \times 81 \times 25}{3 \times 9 \times 7 \times 100 \times 24} = \frac{97200}{453600} = \frac{3}{4}$

(3)

$$\frac{21}{35}$$
 of $\frac{6}{11}$ of $\frac{77}{36}$ = $\frac{21 \times 6 \times 77}{35 \times 11 \times 36}$ = $\frac{7}{16}$.

(4)

$$\frac{2}{6}$$
 of $\frac{4}{3}$ of $\frac{1}{17}$ of $\frac{1}{17}$ = $\frac{2 \times 4 \times 3 \times 13}{5 \times 7 \times 11 \times 17}$ = $\frac{312}{6846}$.

EXERCISE 49-Page 161.

$$\frac{5}{9} \text{ of } \text{$$

(2)

$$\frac{3}{3} \text{ of } \frac{1}{3} \text{ of } \frac{1}{13} \text{ of } \frac{1}{13} \text{ of } \frac{1}{13} \text{ of } \frac{1}{13} = \frac{2 \times 5 \times 18 \times 6 \times 11 \times 13}{3 \times 9 \times 132 \times 11 \times 13 \times 17} = \frac{2 \times 5}{3 \times 9 \times 132 \times 11 \times 13 \times 17} = \frac{2 \times 5}{33 \times 17} = \frac{10}{561}.$$

(3)

$$\frac{3}{7} \text{ of } \frac{4}{11} \text{ of } 5\frac{1}{2} = \frac{2 \times 4 \times 11}{7 \times 11 \times 2} = \frac{2 \times 4 \times 11}{7 \times 11 \times 2} = 4$$

1× 8×117× 50×13×13 $\frac{1}{9}$ of $\frac{8}{13}$ of $\frac{117}{200}$ of $\frac{80}{169}$ of $\frac{13}{6}$ of $\frac{13}{6}$ 9×13×200×169×17× 6

$$\frac{1 \times 8 \times 117 \times 50 \times 18 \times 18}{9 \times 18 \times 200 \times 169 \times 17 \times 6} = \frac{1}{17 \times 3} = \frac{1}{17 \times 3}$$

(5) 3×4× 9×33×38×47 γ^{3}_{1} of $\frac{4}{7}$ of $\frac{4}{19}$ of $\frac{3}{19}$ of $\frac{3}{7}$ of $\frac{4}{7}$ = - $11 \times 7 \times 19 \times 47 \times 72 \times 7$

$$\frac{3\times4\times9\times98\times88\times47}{11\times7\times19\times47\times73\times7} = \frac{3\times3}{7\times7} = \frac{3\times3}{7\times7}$$

KEY.

 $\frac{5}{3\times7\times4}=\frac{5}{84}.$

× 6×11×13

×11×13×17

50×13×13

169×17× 6

 $\frac{33\times38\times47}{7\times72\times7} :=$

$$\frac{14}{7 \times 11 \times 1} = \frac{4 \times 3 \times 154}{7 \times 11 \times 1} = \frac{4 \times 3 \times 154}{7 \times 11 \times 1} = \frac{2 \times 4 \times 3}{1} = 24.$$

Exercise 50-Page 162.

$$\frac{\frac{14}{14}}{\frac{11}{27}} = \frac{\frac{14}{48}}{\frac{18}{48}} = \frac{\frac{14 \times 25}{45 \times 42}}{\frac{45 \times 42}{9}} = \frac{\frac{14 \times 25}{3}}{\frac{145 \times 42}{9}} = \frac{5}{3 \times 3} = \frac{5}{3 \times 3}$$

$$\frac{\frac{11}{2}}{\frac{11}{18}} = \frac{\frac{11}{18}}{\frac{11}{18}} = \frac{11 \times 18}{12 \times 143} = \frac{11 \times 18}{\frac{12 \times 148}{2}} = \frac{3}{2 \times 13} = \frac{3}{2 \times 13}$$

$$\frac{15\frac{3}{6}}{7\frac{1}{6}} = \frac{\frac{7}{6}}{\frac{3}{6}} = \frac{\frac{78 \times 5}{5 \times 39}}{\frac{5}{5 \times 39}} = \frac{\frac{2}{78 \times 5}}{\frac{5}{5 \times 39}} = 2.$$

(4)

$$\frac{11\frac{3}{5}}{12\frac{9}{5}}, \frac{3\frac{1}{4}}{9}, \frac{\frac{3}{7}}{\frac{3}{5}} = \frac{\frac{3}{5}}{\frac{3}{6}}, \frac{\frac{1}{4}}{\frac{3}{5}} = \frac{\frac{3}{7}}{\frac{3}{5}} = \frac{35\times5}{3\times68}, \frac{13\times1}{9\times4}, \frac{2\times5}{7\times3} = \frac{17}{2}, \frac{12}{3}, \frac{12}{3}, \frac{12}{3}$$

$$\frac{7_{3}}{15_{1}^{3}}, \frac{5_{8}^{7}}{3_{5}^{3}}, \frac{2_{8}^{3}}{3_{7}^{3}} = \frac{7_{8}^{7}}{6_{3}^{3}}, \frac{4_{8}^{7}}{3_{5}^{3}}, \frac{1_{8}^{8}}{2_{4}^{4}} = \frac{7 \times 4}{12 \times 68}, \frac{47 \times 16}{8 \times 3}, \frac{12 \times 7}{5 \times 24} = \frac{12 \times 68}{3}$$

$$\frac{1}{8\times 9}$$
, $\frac{47\times 2}{3}$, $\frac{7}{5\times 2}$, $= \frac{1}{47}$, $31\frac{1}{9}$, $\frac{7}{10}$

E

3

(6)

$$\frac{16\frac{9}{3}}{11\frac{9}{3}}, \frac{6\frac{1}{3}}{13}, \frac{17}{18\frac{1}{3}}, \frac{21\frac{9}{3}}{10\frac{3}{3}}, \frac{\frac{1}{4}}{4\frac{3}{3}} = \frac{\frac{A_0}{9}}{\frac{8}{3}}, \frac{\frac{8}{17}}{\frac{1}{9}}, \frac{\frac{1}{17}}{\frac{A_0}{8}}, \frac{\frac{1}{17}}{\frac{7}{2}}, \frac{\frac{1}{19}}{\frac{8}{3}} = \frac{\frac{10}{100} \times 8}{8 \times 85},$$

$$\frac{31\times1}{5\times13}, \frac{17\times3}{55\times1}, \frac{108\times7}{72}, \frac{1\times5}{2\times23}, \frac{10}{7}, \frac{31}{65}, \frac{51}{55}, \frac{21}{10}, \frac{5}{46} = 1\frac{3}{7}, \frac{31}{65}, \frac{3}{8}, \frac{1}{8}, \frac{3}{8}, \frac{3$$

Exercise 51-Page 163.

$$\frac{4}{5} \text{ of } \frac{1}{16} = \frac{1}{10} \text{ of a lb.}$$

(2)

$$\frac{3}{3} \text{ of } \frac{3}{7} \text{ of } \frac{1}{12} \text{ of } \frac{1}{20} = \frac{1}{7 \times 6 \times 20} = \mathcal{E}_{\frac{1}{8}\frac{1}{40}}.$$

$$\frac{3}{7} \text{ of } \frac{3}{4} \text{ of } \frac{1}{7} = \frac{5}{9 \times 2} = \frac{5}{18} \text{ wk.}$$

$$\frac{81}{11}$$
 of $\frac{81}{5}$ of $\frac{1}{4}$ of $\frac{1}{5} = \frac{81}{11 \times 4 \times 5} = \frac{21}{2120}$ Eng. E11.

(5)

$$\frac{3}{7}$$
 of $\frac{4}{11}$ of $\frac{1}{51}$ = $\frac{3}{7}$ of $\frac{4}{11}$ of $\frac{2}{11}$ = $\frac{3}{847}$. per

10 50× B

33 8 ×8K

= 13,31,\$1,210,\$6.

$$\frac{2}{7} \text{ of } \frac{4}{7} \text{ of } \frac{1}{14} \text{ of } \frac{1}{8} = \frac{\frac{3 \times 4 \times 295 \times 1}{3 \times 7 \times 14 \times 8}}{\frac{3 \times 7 \times 14 \times 8}{14 \times 8}} = \frac{295}{294} = 1_{\frac{3}{2},\frac{3}{2}} \text{ c.}$$
(7)

Exercise 52-Page 164.

$$\frac{14}{79}$$
 of $\frac{4}{1}$ of $\frac{2}{1}$ of $\frac{4}{1} = 498$ qt.

(2)

$$\frac{2}{9} \text{ of } \frac{4}{1} \times \frac{3}{1} \times \frac{4}{1} \times \frac{5}{1} \times \frac{8}{2} = \frac{2 \times 4 \times 4 \times 5}{3} = 190$$

(3)

$$\frac{7}{2} \times \frac{2}{1} \times \frac{2}{1} \times \frac{4}{1} \times \frac{2}{1} \times \frac{2}{1} \times \frac{2}{1} \times \frac{2}{1} \times \frac{2}{2} = \frac{7 \times 2 \times 2 \times 4 \times 2}{3} = \frac{224}{3}$$

(4)

$$\frac{17}{22} \times \frac{12}{1} \times \frac{8}{1} \times \frac{3}{1} = \frac{17 \times 6 \times 8 \times 3}{11} = \frac{2448}{11} \text{ scr.}$$

(5)

,

£ 1 0.

wk.

Eng. Ell.

y per

Exercise 53-Page 164.

(1)

0 15

bush. pk. gal. qt. pt. 11)3 0 0 0 0

(3)

lbs. oz. dwt. grs. 9)8 0 0 0

lbs. oz. dr. , 7)6 0 0
13 113
(2) yds. qr. na. in, 113) 7 (2 0 113
28 qrs. 26
2 · · · · · · · · · · · · · · · · · · ·
8 na. 2‡
18 13
5
(4) fur. per. yds. ft. in, 9)8 0 0 0 0

and the same of the same	0 13 8
sq. m. a. 1 113) 11 (62 640	r. pr. yds. ft. in. 1 8 4 2 79 _T
7040 a. 678	
260 226	484 yds 452
34 4 	32 9
113 23 40	$\frac{226}{62}$
920 per. 904	248 248
16 301	62 8928 in. 791
480 4 —— 484 yds,	1018

£ s. d 7)4 0 0

35 * 3

Exercise 54-Page 165.

(1)

6 bus. 1 pk. 1 gal. 1 qt. 1 pt. = 411 pts.
50 bush. = 3200 pts.
And the required fraction is 4100.

(2)

35 per. 9 ft. 2 in. = 7040 in. 1 fur. = 7920 in. The required fraction is 7928 = 38 = 3.

(3)

7 hrs. 12 min. = 432 min. 1 day = 1440 min. Therefore the fraction is $\frac{1}{1440} = \frac{3}{16}$.

(4)

2 sq. yds. 2 ft. 120 in. = 3000 in. 3 sq. per. 13½ yds. 1 ft. 72 in. = 135000 in. And the fraction is $730000 = \frac{1}{45}$.

(5)

7 oz. 7 drs. 2 scr. 14 grs. = 3834 grs. 21 lbs. = 120960 grs. The fraction is $\frac{3}{12}\frac{3}{12}\frac{3}{12}\frac{4}{10} = \frac{1}{12}\frac{3}{12}\frac{4}{10} = \frac{1}{12}\frac{3}{12}\frac{4}{10}$.

(6)

9 min. 48 sec. = 588 sec. 1 day = 86400 sec. The required fraction is $\frac{86400}{86400} = \frac{720}{7200}$.

(7)

16 bush. 1 pk. 1 pt. = 1041 pts. 69 bush. = 4416 pts. Therefore the fraction is $\frac{1041}{40416} = \frac{347}{4084}$,

(3)

os. dwt. grs.

r. pr. yds. ft. in. 1 8 4 2 79₇|₃

> 484 yds 452

32 9

288 ft.

62

144

248

248 62

8928 in. 791

1018 1017

1

COL

Th

tor

Th

tor

3 =

1ª-16

+ 84 10

17

17

94

63

+

(8)

3 qrs. $3\frac{1}{9}$ na. = $15\frac{1}{9}$ = $\frac{136}{20}$ na. 1 Eng. ell = 20 na. $\frac{136}{20}$ = $\frac{136}{20}$ = $\frac{136}{20}$ = $\frac{34}{20}$.

. (9)

13 dwt. 7 grs. = 319 grs. 1 lb. Troy = 5760 grs. The required fraction is $3^{3}_{160}^{19}$.

(10)

4800 cub. ft. 54 cords = 6912 cub. ft. Therefore the fraction is $\frac{1}{6}$? $\frac{1}{2}$ = $\frac{1}{2}$ = $\frac{1}{2}$ = $\frac{1}{2}$.

Exercise 55-Page 167.

11

 $\frac{11}{13} + \frac{10}{13} + \frac{9}{13} = \frac{30}{13} = 2\frac{4}{13}.$ (2)

 $\frac{1}{18} + \frac{6}{19} + \frac{7}{18} + \frac{1}{19} + \frac{1}{19} + \frac{1}{19} + \frac{2}{19} = \frac{2}{19} = 3\frac{1}{19} = 3\frac{1}{4}.$

(3)

(4)

 $16\frac{3}{3} + 11\frac{1}{2}\frac{7}{3} + 18\frac{4}{3} + 17\frac{1}{2}\frac{9}{3} + 112\frac{2}{3}\frac{9}{3} = 16 + 11 + 18 + 17 + 112 + (\frac{2}{3}\frac{1}{3} + \frac{1}{2}\frac{7}{3} + \frac{1}{3}\frac{7}{3} + \frac{1}{2}\frac{9}{3} + \frac{1}{2}\frac{9}{3} + \frac{1}{2}\frac{9}{3} + \frac{1}{2}\frac{9}{3} + \frac{1}{2}\frac{1}{3} + \frac{1}{2}\frac{1}{3}$

(5)

 $\begin{array}{c} 4\frac{1}{4} + 1\frac{1}{3} + \frac{7}{17} = 4 + 1 + (\frac{1}{4} + \frac{1}{3} + \frac{7}{17}) = 5 + (\frac{33}{133} + \frac{44}{133} + \frac{1}{133}) \\ 1\frac{34}{133} = 5 + \frac{1}{1}\frac{6}{3}\frac{1}{3} = 6\frac{39}{133}. \end{array}$

(6)

1+3+3+3+6+9+6+8.

These fractions reduced to their least common denominate become $\frac{1360}{1620} + \frac{1660}{16620} + \frac{1690}{16620} + \frac{1690}{2620} + \frac{1690}{26$

(7)

3+4+4 when reduced to their least common denominator come $\frac{1}{2} + \frac{1}{2} + \frac{1}{2} + \frac{1}{2} = \frac{1}{2}$

(8)

1+1++++++

These fractions when reduced to their least common denomitor become 3323 + 3198 + 3498 + 3498 + 9118 = 33197 =\$46.

(9)

1+1+1+1+1+1+1

These fractions when reduced to their least common denomitor become $\frac{1}{2}\frac{1}{6}$ + $\frac{1}{2}\frac{1}{6}$ + $\frac{1}{2}\frac{1}{6}$ + $\frac{1}{2}\frac{1}{6}$ + $\frac{1}{2}\frac{1}{6}$ + $\frac{1}{2}\frac{1}{6}$ = $\frac{1}{2}\frac{1}{6}$ = $\frac{3}{6} = 1 \frac{83}{40}$.

(10)

 $1636 + 476 + 2137 + 78 + 191 = 16 + 47 + 21 + 19 \times (36)$ 3+33+78+3).

16 + 47 + 21 + 19 = 103. + 8 + 37 + 78 + 1 = 1488 + 1388 + 1388 + 1488 + 1488 + 1488 =

 $\frac{84}{83} = \frac{376}{108} = \frac{188}{99} = 1\frac{89}{98}$ 103 + 188 = 10488

(11)

 $17\frac{1}{2} + 43\frac{2}{7} + 168\frac{1}{2} + 207\frac{8}{21} + 506\frac{128}{28} = 17 + 43 + 168 + 168$

 $7 + 506 + (\frac{1}{4} + \frac{3}{7} + \frac{4}{5} + \frac{8}{51} + \frac{185}{286}).$ 17 + 43 + 168 + 207 + 506 = 941.

 $\begin{array}{l} \frac{1}{4} + \frac{3}{7} + \frac{4}{5} + \frac{4}{125} + \frac{125}{125} = \frac{123}{125} + \frac{125}{125} + \frac{125}{125} + \frac{125}{125} + \frac{125}{125} = \frac{123}{125} = \frac{123}{12$

(12)

 $63 + 114 + \frac{9}{86} + 16\frac{7}{16} + \frac{1}{8} + \frac{1}{8}\frac{1}{16} + \frac{17}{18} = 6 + 11 + 16 + \frac{1}{16}$ $\begin{array}{c} + (\frac{3}{4} + \frac{4}{7} + \frac{5}{86} + \frac{7}{16} + \frac{1}{8} + \frac{4}{97} + \frac{11}{18}). \\ 6 + 11 + 16 + 17 = 50. \end{array}$

 $\frac{3+4+86+76+1+4+1}{8+366+366+366+366+366+366}$

 $50 + 3\frac{193}{336} = 53\frac{193}{336}$.

ommon denominato

na. = 38.

na.

= 49 = 34.

 $=3_1^3_8=3_1^4.$

-16 + 21 + 19 +f = 734.

- 11+18+17+1124 $174 + 3\frac{1}{4} = 177$

5+(133+144-

十 8.

8 + 31 28 + 28 28

Dix B.

4

20

7,6

3 +

3章

10 f10

3 -

680

411

= 472 41

115 115

924

136

(13)

 $\begin{array}{l} \frac{1}{6} + \frac{3}{3} + \frac{7}{6} + 68\frac{1}{4} = 68 + (\frac{1}{6} + \frac{3}{3} + \frac{7}{6} + \frac{1}{4}). \\ \frac{1}{6} + \frac{3}{6} + \frac{1}{6} + \frac{1}{4} = \frac{3}{6} + \frac{1}{18} + \frac{1}{18} + \frac{1}{18} + \frac{1}{18} = \frac{3}{18} = \frac{1}{18} \\ 68 + \frac{1}{18} \frac{1}{18} = 69\frac{1}{18} \frac{1}{6}. \end{array}$

(14)

 $\begin{array}{l} 173 & 18 + 89 + 91\frac{1}{12} = 173 + 8 + 91 + (1 + 9 + 1\frac{1}{12}). \\ 173 + 8 + 91 = 272. \\ 1 + 9 + 15 = 912 + 1882 + 1882 = 982 = 1182. \\ 272 + 1182 = 273282. \end{array}$

(15)

(16)

 $\frac{1}{10} + \frac{1}{10} + \frac{1}{10}$

(17)

 $7 + 11\frac{1}{2} + 18 + 26\frac{3}{7} + 79\frac{4}{1} = 7 + 11 + 18 + 26 + 79 + (\frac{1}{2} + \frac{3}{7} + \frac{4}{17}).$ 7 + 11 + 18 + 26 + 79 = 141. $\frac{1}{2} + \frac{3}{7} + \frac{4}{17} = \frac{777}{1574} + \frac{676}{156} + \frac{196}{156} = \frac{199}{156} = 1_{7}^{4}_{56}.$ $141 + 1\frac{48}{156} = 142\frac{6}{156}.$

(18)

 $\begin{array}{l} \frac{4}{5} \text{ of } \frac{2}{5} \text{ of } \frac{2}{5} \frac{1}{5} = \frac{16}{5} = 3\frac{2}{5}, \frac{2}{5} + 7\frac{2}{15} + 3\frac{2}{5} = 10 + (\frac{1}{3} + \frac{2}{15} + \frac{2}{5}) \\ \frac{2}{5} + \frac{2}{15} + \frac{2}{5} = \frac{1}{15}\frac{1}{5} + \frac{2}{15}\frac{1}{5} + \frac{2}{15}\frac{1}{5} = \frac{1}{15}\frac{2}{5} = 1\frac{2}{15}\frac{2}{5} = \frac{2}{15}\frac{2}{5} = \frac{2}$

= 計計 = 1計計.

十 4 十 14).

384.

4 + (18 + 82 +

9388 = "7833 =

A+11+4+

8 + 26 + 79 +

184.

+ (3+1/2+3).

(19)

 13×18 = 4 = 11.3 × 7

 $1\times36\times4\times11$ 1 of 19 of 15 of 4 = $2\times11\times15\times4$

83 × 11 201 = \ = 27. 4×83

· + · · · ·

 $\frac{1}{2} + \frac{1}{16} + \frac{1}{2} = \frac{1}{16} + \frac{1}{16} + \frac{1}{16} = \frac{1}{16} =$ $14 + 1_{140}^{13} = 15_{140}^{13}$.

(20)

 $3\frac{1}{6} + 11\frac{1}{6} + 14\frac{3}{4}\frac{3}{6} = 3 + 11 + 14 + (\frac{5}{6} + \frac{1}{6} + \frac{23}{6}) = 28 + \frac{11}{6} + \frac{1$

 $\frac{5}{8} + \frac{1}{8} + \frac{3}{4}\frac{2}{8}$). $\frac{5}{8} + \frac{1}{8} + \frac{3}{4}\frac{2}{8} + \frac{3}{4}\frac{2}{8} + \frac{3}{4}\frac{2}{8} + \frac{3}{4}\frac{2}{8} = \frac{7}{4}\frac{2}{8} = \frac{7}{4}\frac{2}{8$

(21)

1 of 1 = 1, 1 of 4 = 1, 2 of 3 = 16, 1 of 26 = 16, 1 of 1

 $f \nmid of \nmid of \nmid = 30$.

3++++78+30+30=1000+1000+7880+1000+ $83_{\overline{0}} = 1840 = 11298.$

(22)

 $41\frac{1}{2} + 105\frac{1}{2} + 300\frac{2}{2} + 241\frac{2}{6} + 472\frac{1}{6} = 41 + 105 + 300 + 241$ $=472+(\frac{1}{4}+\frac{2}{5}+\frac{2}{4}+\frac{2}{5}+\frac{1}{4}).$

41 + 105 + 300 + 241 + 472 = 1159.

1+3+1+1+1+1=10+100+138+138+148+146=118= $\frac{09}{0} = 23\frac{9}{6}$.

1159 + 238 = 116138.

(23)

 $92\frac{1}{14} + 37\frac{1}{15} + 7\frac{1}{4} = 92 + 37 + 7 + (\frac{1}{14} + \frac{1}{15} + \frac{1}{4}) = 136 + \frac{1}{14}$ 作十十十十分.

 $\frac{6}{1} + \frac{4}{15} + \frac{2}{3} = \frac{288}{125} + \frac{238}{125} + \frac{138}{125} = \frac{1388}{125} = \frac{1388}{125}$

136 + 1384 = 137344.

77

20

8

6

29

68

61

(6)

$$\frac{10\frac{3}{6}}{\frac{2\frac{5}{6}}{2\frac{5}{6}}} = \frac{\frac{53 \times 5}{5 \times 12}}{\frac{5 \times 12}{5 \times 12}} = \frac{5\frac{3}{6}}{\frac{3}{6}} = \frac{4\frac{5}{6}}{\frac{3}{6}} = \frac{3}{6} \text{ of } \frac{7}{6} = \frac{7}{16}.$$

$$21\frac{1}{6} + 35\frac{1}{6} + 4\frac{5}{16} + \frac{7}{16} = 21 + 35 + 5 + (\frac{1}{6} + \frac{1}{6}) = 61\frac{5}{6}.$$
(25)

 $\begin{array}{l} \frac{1}{14} \text{ of } \frac{1}{14} = \frac{1}{12} = 10 \frac{1}{12}, \quad \frac{1}{12} \text{ of } \frac{3}{12} \text{ of } \frac{1}{12} = \frac{3}{16} \frac{1}{12} = 15 \frac{1}{16} \frac{1}{12}. \\ \frac{1}{12} = \frac{1}{12} = \frac{1}{12} = \frac{1}{12} = \frac{1}{12} = \frac{1}{12}. \end{array}$

(5)

Exercise 56-Page 169.

(3)

in.

1 of a yd. = 51
1 of a ft. = 17
1 of a mile = 5 3 8 1 6
1 of a ft. = 17
2 of a fur. = 12 1 2
$$0\frac{12}{13}$$
3 of a fur. = 12 1 $2\frac{0\frac{12}{3}}{12}$
7 of a yd. = 1 $2\frac{1}{12}$
7 $\frac{1}{12}$ of a yd. = 1 $2\frac{1}{12}$

of
$$\frac{7}{4} = \frac{7}{12}$$
.
+ $\frac{1}{4}$) = 614.

(4)

r. yds, ft. in.
8 1 6
1 2
$$0\frac{3}{1}$$

1 $2\frac{8}{1}$
0 0 $3\frac{9}{14}$

EXERCISE 57-Page 171.

$$\frac{1}{4} - \frac{1}{4}\sigma = \frac{1}{2}\delta - \frac{1}{2}\sigma = \frac{1}{4}\sigma = \frac{1}{4}.$$

(2)

$$\frac{7}{17}$$
 of $\frac{3}{14}$ of $\frac{96}{17} = \frac{3 \times 48}{17 \times 11} = \frac{187}{1496} + \frac{187}{1496} + \frac{906}{1496} + \frac{1188}{1496} = \frac{906}{1496} + \frac{906}{1496} = \frac{$

$$1496 = 1561 = 13$$

$$\frac{8\frac{3}{4}}{6\frac{1}{1}} = \frac{\frac{3}{4}}{\frac{7}{1}} = \frac{\frac{35 \times 11}{4 \times 70}}{\frac{4 \times 70}{1\frac{3}{4}}} = \frac{11}{4 \times 2} = \frac{11}{8} = 1\frac{3}{8}.$$
(3)

(4)

$$\begin{array}{l} 69_{7}^{1}_{1} - 18_{1}^{18}_{46} = 69_{7}^{14}_{446}^{6} - 18_{7}^{18}_{446}^{6} = 68 + 1_{7}^{14}_{446}^{6} - 18_{7}^{18}_{446}^{6} = \\ 68_{7}^{7}_{446}^{6} - 18_{7}^{48}_{46}^{6} = 50_{7}^{3}_{446}^{6} = 50_{3}^{3}_{6}^{6}_{3}^{3}. \end{array}$$

(5)

$$100\frac{1}{8} - 9\frac{6}{8} = 100\frac{4}{8} - 9\frac{6}{8} = 99 + 1\frac{4}{8} - 9\frac{6}{8} = 99\frac{1}{8}^{2} - 9\frac{6}{8} = 90\frac{7}{8}$$
(6)

$$\frac{1}{5^{\frac{1}{8}}} \stackrel{\text{of }}{4^{\frac{7}{8}}} = \frac{37}{8} = \frac{45}{8}. \quad 6\frac{1}{4} - \frac{45}{8} = 6\frac{2}{8} - \frac{47}{8} = 5 + 1\frac{2}{8} - 4\frac{5}{8} = \frac{5}{8} - \frac{45}{8} - \frac{45}{8} = \frac{5}{8} - \frac{45}{8} = \frac{5}{8} - \frac{45}{8} = \frac{5}{8} - \frac{45}{8} - \frac{45}{8} = \frac{5}{8} - \frac{45}{8} = \frac{5}{8} - \frac{45}{8} - \frac{45}{8} - \frac{45}{8} = \frac{5}{8} - \frac{45}{8} - \frac{45}{8$$

$$\begin{array}{c} 611_{7}^{43}_{97} - 610_{98}^{138} = 611_{38507}^{8557}_{9} - 610_{37808}^{37808} = 610 + 1_{8809}^{8557}_{909} - \\ 610_{37808}^{37808}_{18} = 610_{38808}^{48808}_{18808} = _{387688}^{8709}_{909}. \end{array}$$

9

(10)

(11)

(12)

(13)

$$\frac{1}{1} \text{ of } \frac{3}{7} \text{ of } \frac{3}{3} \text{ of } \frac{62}{3} = \frac{1 \times 3 \times 2 \times 33 \times 62 \times 5}{2 \times 7 \times 9 \times 4 \times 33 \times 6} = \frac{155}{262}.$$

$$\frac{12 \frac{319}{764} + \frac{155}{262} = 12 \frac{319}{764} + \frac{1754}{1764} = 12 \frac{319}{124} = 12 \frac{319}{4} = 12 \frac{319}{4} = 12 \frac{319}{4}.$$

$$\frac{17 \frac{31}{17}}{1\frac{33}{23}} = \frac{196 \times 33}{\frac{5}{3}} = \frac{21}{11 \times 56} = 10\frac{1}{2}.$$

$$12\frac{33}{2} - 10\frac{1}{4} = 12\frac{318}{2} - 10\frac{19}{2} = 2\frac{29}{18}.$$

(14)

 $3\frac{1}{13} + 8\frac{1}{9} + 5\frac{1}{6} + 6\frac{1}{2} = 3 + 8 + 5 + 6 + (\frac{1}{12} + \frac{1}{9} + \frac{1}{6} + \frac{1}{4}) = 22 + (\frac{1}{12} + \frac{1}{9} + \frac{1}{6} + \frac{1}{6} + \frac{1}{2}).$

 $\frac{1}{12} + \frac{1}{9} + \frac{1}{8} + \frac{1}{8} = \frac{1}{180} + \frac{20}{180} + \frac{36}{180} + \frac{90}{180} = \frac{161}{180}$

 $22 + \frac{161}{160} = 22\frac{161}{160}$

 $3_{10}^{3} + 2_{5}^{4} + 16_{4}^{4} = 3 + 2 + 16 + (_{10}^{3} + _{5}^{4} + _{4}^{4}) = 21 + (_{10}^{3} + _{5}^{4} + _{4}^{4}).$

 $1^{3}0 + 6 + 1 = 16 + 68 + 16 = 68 = 168$. 21 + 168 = 2268. 22 + 168 = 2268. 22 + 168 = 2268. 22 + 168 = 2268.

57, 58.] KEY.

(15)

(16)

 $\begin{array}{l} 16\frac{1}{7} - 9\frac{1}{14} = 16\frac{10}{133} - 9\frac{08}{133} = 15 + 1\frac{10}{133} - 9\frac{08}{133} = 15\frac{10}{133} - 9\frac{08}{133} - 9$

Exercise 58-Page 173.

(4) (4) (5)

 $\frac{7 \times \frac{5}{6} \times \frac{7}{16} = \frac{745}{765}}{\frac{14}{1} \times \frac{241}{16} \times \frac{33}{9} = \frac{14 \times 241 \times 2}{9} = \frac{6736}{9} = 7495}$

 $\frac{3}{\frac{9}{2}} \times \frac{7}{4} \times \frac{9}{11} \times \frac{11}{\frac{12}{4}} = \frac{3 \times 7 \times 9}{2 \times 4 \times 4} = \frac{169}{3} = 532.$

 $\frac{3}{\frac{1}{5}} \times \frac{3}{\frac{1}{11}} \times \frac{9}{17} \times \frac{182}{\frac{200}{50}} \times \frac{5}{9} = \frac{3 \times 182}{11 \times 17 \times 25} = \frac{546}{4675}.$

= 16.

 $\frac{1}{6} \frac{7}{8} = \frac{21}{16} \frac{8}{6} = \frac{23}{16} \frac{1}{8} = \frac{1}{16} \frac{1}{16} = \frac{1$

0 8 0

 $= 1\frac{35}{5}.$ $- 1\frac{35}{3} = 5\frac{3}{3}.$

 $=\frac{155}{252}$.

 $12\frac{3}{4}\frac{1}{7}=12\frac{3}{4}\frac{9}{7}.$

+ 1 + 1 + 1)=

181.

 $+ \frac{1}{4}) = 21 +$

+133 = 2233.

(8)

(8)
$$\frac{3}{8} \times \frac{11}{8} \times \frac{3}{8} \times \frac{31}{1} \times \frac{8}{5} \times \frac{5}{1} = \frac{3 \times 3 \times 3}{2} = \frac{27}{2} = 13\frac{1}{2}.$$

(9)

$$\frac{\frac{2}{8}}{\frac{9}{8}} \times \frac{\frac{8}{5}}{5} \times \frac{\frac{6}{11}}{11} \times \frac{\frac{4}{19}}{\frac{19}{1}} \times \frac{\frac{11}{289}}{\frac{1}{5}} = \frac{\frac{2\times6\times4}{5}}{5} = \frac{45}{5} = 93.$$

(10)

$$\frac{18}{2} \times \frac{80}{4} \times \frac{180}{11} \times \frac{2}{18} \times \frac{4}{80} \times \frac{1}{90} = 2r.$$

(11)

$$\frac{4}{7} \times \frac{3}{11} \times \frac{9}{16} \times \frac{7}{1} \times \frac{8}{7} \times \frac{8}{18} \times \frac{18}{1} \times \frac{167}{24} = \frac{3 \times 9 \times 167}{4} = \frac{45409}{11274} = 11274.$$

(12)

$$\frac{\frac{1}{7}}{\frac{8}{7}} \times \frac{\frac{8}{7}}{\frac{1}{19}} \times \frac{\frac{6}{9}}{\frac{8}{9}} \times \frac{\frac{10}{4}}{\frac{101}{14}} \times \frac{2}{27} \times \frac{8}{8} =$$

$$\frac{1}{7 \times 8} \times \frac{8 \times 2}{7 \times 19} \times \frac{84 \times 9}{9 \times 8} \times \frac{19 \times 14}{101 \times 4} \times \frac{1}{9} \times \frac{9}{8} = \frac{1}{7 \times 101} = \frac{1}{707}.$$

13)

$$\frac{1}{4} \times \frac{\frac{2}{5}}{1} \times \frac{2}{7} \times \frac{19}{1} = \frac{2 \times 2 \times 19}{7} = \frac{7}{7} = 109.$$

KEY.

= 27 = 131.

[NAT. ARITH.

= 97.

=4502=11271.

101

$$\frac{9}{\frac{10}{5}} \times \frac{7}{1} \times \frac{11}{15} \times \frac{\frac{32}{5}}{11} = \frac{9 \times 7 \times 32}{5} = \frac{90 \times 6}{5} = 403 \frac{1}{5}.$$
(15)

$$\frac{27}{\frac{3}{4}} \times \frac{\frac{7}{4}}{\frac{3}{2}} \times \frac{\frac{3}{4}}{\frac{5}{5}} \times \frac{\frac{3}{4}}{\frac{7}{4}} = \frac{27}{16} = \frac{277}{16}.$$
(16)

$$\frac{11}{8} \times \frac{13}{8} \times \frac{15}{1} = \frac{11 \times 13 \times 15}{8} = \frac{2145}{8} = 268\frac{1}{3}.$$
(17)

$$\frac{1}{8} \times \frac{85}{4} \times \frac{8}{19} \times \frac{19}{3} \times \frac{94}{11} \times \frac{16}{17} \times \frac{49}{8} \times \frac{4}{5} \times \frac{27}{21} \times \frac{81}{3} \times \frac{191}{188} =$$

 $7\times49\times27\times191$ $-= \frac{1768851}{974} = 4729394.$ $2 \times 11 \times 17$

(18)

$$\frac{\frac{27}{37\frac{1}{8}} \times \frac{87\frac{3}{9}}{98\frac{1}{8}} \times \frac{\frac{7}{8}}{2\frac{1}{3}} \times \frac{81\frac{5}{11}}{128} = \frac{\frac{27}{18}}{\frac{189}{8}} \times \frac{\frac{785}{9}}{\frac{785}{8}} \times \frac{\frac{7}{3}}{\frac{7}{3}} \times \frac{\frac{896}{128}}{\frac{128}{128}} = \frac{27\times5}{189} \times \frac{785\times8}{8\times7} \times \frac{7\times8}{8\times7} \times \frac{896\times1}{11\times128} = \frac{5}{3\times11} = \frac{5}{35}.$$
(19)

$$\$\frac{\frac{5}{11}}{11} \times \frac{1}{7} \times \frac{3}{5} \times \frac{17}{19} = \frac{3 \times 17}{11 \times 7} = \$\%$$

33

(20)

$$\frac{75_{3}^{2}}{6_{1}^{1}_{1}} \times \frac{\frac{3}{7} \text{ of } 8_{\frac{1}{2}} \times \frac{1}{15} \text{ of } 28}{\frac{4}{15} \times \frac{1}{7} \text{ of } 24} \times \frac{7_{\frac{1}{2}}}{15} \times \frac{3}{4} \times 14_{\frac{7}{2}} \times \frac{100}{121} \times \frac{4}{15} \times \frac{5}{4} \times \frac{1}{15} \times \frac{5}{4} \times \frac{1}{15} \times \frac{5}{4} \times \frac{1}{15} \times \frac{5}{4} \times \frac{1}{15} \times \frac{1}{2} \times \frac{5}{4} \times \frac{1}{15} \times \frac{1}{2} \times \frac{100}{121} \times \frac{100}{1$$

Exercise 59-Page 174.

(1)

$$\frac{13}{36}$$
 of 4 days, 5 hours, $=\frac{180 \text{ d. } 23 \text{ h.}}{36} = 5 \text{ d. } 0 \text{ h. } 38 \text{ min. } 20 \text{ sec.}$

(2)

$$\frac{13}{43} \text{ of } £29 = \frac{£29 \times 13}{42} = \frac{£377}{42} = £8 \text{ 19s. } 67\text{d.}$$

KEY.

100 121

NAT. ARITH

 $\times \frac{100}{121} \times$

< \frac{4\times \frac{4}{8\times \frac{4}{8}} \times \frac{4}{8}

in. 20 sec.

(3)

 $\frac{7}{9}$ of 186 a. 3 r. $=\frac{186 \text{ a. 3 r.} \times 7}{9} = \frac{1307 \text{ a. 1 r.}}{9} = 145 \text{ a. 1 r.}$

(4)

 $\frac{14}{14}$ of $\frac{1}{7}$ of $\frac{1}{30}$ of $\frac{1}{3}$ of 24 h. 30 m. = 1 h. 38 m.

(5)

 $\frac{3}{7} \text{ of } \frac{4}{9} \text{ of } \frac{2}{40} \text{ of } \frac{7}{9} \text{ of } 33 \text{ bu. } 2 \text{ p. 1 ga.} = \frac{7}{90} \text{ of } 33 \text{ bu. 2 p. 1 ga.} = \frac{33 \text{ bu. 2 p. 1 ga.} \times 7}{90} = \frac{235 \text{ b. 1 p. 1 g.}}{90} = 2 \text{ b. 2 p. 0 g. 3 q 1} \frac{1}{4} \frac{7}{4} \text{ p}$

Exercise 60-Page 175.

(1)

 $\frac{1}{2}$ of $\frac{3}{5} \div \frac{3}{4}$ of $\frac{3}{5} = \frac{1}{2} \times \frac{3}{5} \times \frac{2}{3} \times \frac{4}{35} = \frac{2 \times 4}{5 \times 35} = \frac{1}{175}$

(2)

 $\frac{15}{25} \div \$ \div \$_1 = \frac{15}{22} \times \frac{5}{2} \times \frac{11}{5} = \frac{5}{2 \times 3} = \$$

(8)

 $82_{17}^{1} \div 26_{11}^{1} = \frac{155}{17} \times \frac{41}{101} = \frac{155 \times 41}{17 \times 119} = \frac{6355}{2023} = 3\frac{286}{2023}.$

(4)

 $2\frac{1}{2} \div \frac{3}{4} + \frac{5}{8} = \frac{5}{4} \div \frac{11}{8} = \frac{5}{2} \times \frac{\frac{3}{8}}{11} = \frac{5 \times 4}{11} = \frac{20}{11} = 1$

45

28

25

(5)

$$1\frac{1}{2} \div \frac{1}{7}$$
 of $2\frac{3}{7}$ of 16 of $2\frac{5}{7}$ of $\frac{7}{70} = \frac{7}{\frac{4}{3}} \times \frac{7}{1} \times \frac{4}{11} \times \frac{1}{16} \times \frac{4}{25} \times \frac{4}{25} \times \frac{4}{11} \times \frac{1}{16} \times \frac{4}{25} \times \frac{4}{11} \times \frac{1}{16} \times \frac{4}{25} \times \frac{4}{11} \times \frac{1}{16} \times \frac{4}{11} \times \frac{4}{11} \times \frac{1}{16} \times \frac{4}{25} \times \frac{4}{11} \times \frac{1}{11} \times \frac{1}{16} \times \frac{4}{11} \times$

$$\frac{\frac{2}{70}}{\frac{1}{1}} = \frac{7 \times 7}{2 \times 11} = \frac{49}{22} = 2\frac{4}{2}$$

(6)

$$2\frac{1}{3} \div (\frac{5}{2} \div \frac{1}{3} \times 0f 9) = \frac{7}{3} \div (\frac{5}{9} \text{ of } \frac{32}{6} \text{ of } \frac{1}{9}) = \frac{7}{8} \times \frac{9}{5} \times \frac{8}{83} \times \frac{3}{83}$$

$$\frac{3}{9} = \frac{7 \times 9 \times 3 \times 3}{5 \times 16} = \frac{567}{80} = 7\frac{7}{80}$$

(7)

$$481 \div \frac{1}{3} + \frac{3}{3} \text{ of } 6 = \frac{97}{3} \div \frac{1}{3} + \frac{1}{4} = \frac{97}{3} \div \frac{1}{3} \frac{1}{8} = \frac{97}{4} \times \frac{18}{89} = \frac{97}{4} \times \frac{18}{89} = \frac{1}{1}$$

$$\frac{97 \times 18}{20} = \frac{1746}{80} = 1945.$$

(8)

$$6\frac{1}{2} \div \frac{3}{8} \text{ of } \frac{9}{10} + \frac{8}{17} = \frac{13}{2} \div \frac{27}{80} + \frac{8}{17} = \frac{13}{2} \div \frac{859}{850} = \frac{13}{2} \times \frac{13}{2}$$

425

$$\frac{850}{859} = \frac{13 \times 425}{859} = \frac{5525}{859} = 6373$$

(9)

$$\frac{9}{8} \times \frac{10}{3} \div \frac{2}{3} \times \frac{25}{3} = \frac{9}{15} \times \frac{10}{3} \times \frac{4}{3} \times \frac{4}{3} \times \frac{4}{35} = \frac{4 \times 4}{3 \times 5} = \frac{16}{15} = 1.5$$

$$=\frac{13}{2}\times$$

$$\frac{16}{15} = 1_{15}^{1},$$

(10)

$$\frac{67}{\frac{3}{3}} \div \frac{3}{\frac{3}{3}} = \frac{67 \times 3}{9 \times 35} \div \frac{3 \times 8}{7 \times 33} = \frac{67 \times 3}{\frac{9}{3} \times 35} \times \frac{7 \times 33}{3 \times 5} = \frac{67 \times 11}{3 \times 5 \times 8} = \frac{67 \times 11}{3 \times 5 \times 8} = \frac{737}{120} = \frac{617}{120}.$$
(11)

$$\frac{5}{9}$$
 of $\frac{30}{11} \div \frac{4}{11}$ of $\frac{13}{9}$ = $\frac{5}{9} \times \frac{11}{11} \times \frac{7}{4} \times \frac{7}{122} = \frac{5 \times 10 \times 7}{9 \times 61} = \frac{350}{349}$

$$\frac{1}{2} \text{ of } \frac{1}{3} \text{ of } \frac{3}{4} \text{ of } \frac{3}{5} \div \frac{6}{6} \text{ of } \frac{3}{2} \text{ of } \frac{3}{4} \text{ of } \frac{3}{4} \times \frac{1}{2} \times \frac{3}{4} \times \frac{7}{4} \times \frac{6}{4} \times \frac{2}{4} \times \frac{1}{4} \times \frac{3}{4} \times \frac{7}{4} \times \frac{6}{4} \times \frac{2}{4} \times \frac{3}{4} \times \frac{1}{4} \times \frac{1}{4}$$

$$\frac{7}{\frac{3}{2}} \div \frac{7}{\frac{3}{4}} = \frac{7 \times 2}{4 \times 9} \div \frac{7 \times 4}{3 \times 9} = \frac{7 \times 2}{4 \times 9} \times \frac{3 \times 9}{7 \times 4} = \frac{3}{2 \times 4} = \frac{3}{2}.$$

$$\frac{3}{35} \div \frac{3}{35} = \frac{3}{25} \div \frac{21 \times 2}{5 \times 35} = \frac{3}{25} \times \frac{5 \times 35}{21 \times 2} = 1$$

$$\frac{2\times136}{7\times18} = \frac{113\times2\times17}{9\times3\times107} = \frac{3842}{2889} = 1\frac{983}{2889},$$

EXERC

121

7

31

3

3

5

41

(16)

$$\frac{31}{4} \times \frac{\frac{7}{7}}{7} \times \frac{\frac{1}{3}}{\frac{3}{3}} \times \frac{\frac{1}{10}}{\frac{3}{3}} \div \frac{\frac{41}{7}}{7} \times \frac{\frac{1}{10}}{\frac{1}{10}} \times \frac{\frac{1}{7}}{7} \times \frac{\frac{11}{4}}{\frac{4}{7}} = \frac{31}{10} \times \frac{\frac{2\times9}{7\times7}}{10\times3} \times \frac{\frac{7}{7}}{10\times3} \times \frac{\frac{41}{9\times7}}{19} \times \frac{\frac{3\times4}{7\times2}}{8\times7} \times \frac{\frac{11\times7}{4\times4}}{4\times4} = \frac{31}{4} \times \frac{\frac{3\times4}{7\times7}}{10\times7} \times \frac{\frac{4}{7\times7}}{10\times7} \times \frac{\frac{4}{7\times7}}{11\times7} = \frac{31\times3\times9\times19\times4}{5\times41\times11} = \frac{63612}{2255} = 28\frac{473}{2255}.$$

Exercise 61-Page 176.

$$\frac{\frac{11}{11}}{\frac{11}{11}} = \frac{19 \times 3}{11 \times 5} = \frac{27}{5}. \quad £8 \quad 14s. \quad 6\frac{1}{2}d. \div \frac{57}{57} = £8 \quad 14s. \quad 6\frac{1}{2}d. \times \frac{57}{57} = £8 \quad 8s. \quad 5\frac{1}{2}d.$$

(2)

(3)

3 a. 3 r. 3 per. $\div \frac{3}{5} = 3$ a. 3 r. 3 p. $\times \frac{5}{3} = \frac{3 \text{ a. 3 r. 3 p. } \times 5}{3} = \frac{$

£7 16s. 2d. \div 4 = £7 16s. 2d. \times 2 = $\frac{£7 ext{ 16s. 2d. } \times 9}{4}$ = £17 11s. 41d.

KEY.

Exercise 62-Page 178.

$$\frac{12\frac{1}{7}}{7} \frac{\frac{4^{2}}{1}}{\frac{7}{3\frac{1}{4}}} = \frac{\frac{1}{12}}{\frac{1}{12}} = \frac{\frac{1}{12}}{\frac{1}{4}} = \frac{\frac{1}{12}}{\frac{2}{4}} = \frac{\frac{1}{12}}{\frac{2}}} = \frac{\frac{1}{12}}{\frac{2}{4}} = \frac{\frac{1}{12}}{\frac{2}} = \frac{\frac{1}{12}}{\frac{2}} = \frac{\frac{1}{12}}{\frac{2}} = \frac{\frac$$

[NAT. ARITE.

11 × -= 11×7

× 4 × 4 × 4

× 11×4

88.

6ad. × 84 =

W = 1 m.

ft

3 p. × 5 3

2d. × 9

4

$$\frac{12\frac{1}{4}}{5\frac{1}{4}} = \frac{\frac{25}{4}}{\frac{15}{4}} = \frac{\frac{25}{4}}{\frac{15}{4}} = \frac{\frac{25}{4}}{\frac{25}{4}} = \frac{\frac{25}{4}}{\frac{25}{4}} = \frac{\frac{25}{4}}{\frac{25}{4}} = \frac{\frac{25}{4}}{\frac{25}{4}} = \frac{\frac{25}{4}}{\frac{25}{4}} = \frac{\frac{1}{4}}{\frac{25}{4}} = \frac{\frac{1}{4}}$$

Exercise 63-Page 180.

$$\frac{800}{2000} = \frac{2}{5} \cdot \frac{420}{2000} = \frac{1}{100} \cdot \frac{100}{2000} = \frac{1}{20} \cdot \frac{160}{2000} = \frac{3}{25} \cdot \frac{35}{2000} = \frac{7}{400} \cdot \frac{160}{2000} = \frac{3}{25} \cdot \frac{160}{2000} = \frac{3}{25} \cdot \frac{160}{2000} = \frac{3}{25} \cdot \frac{160}{2000} = \frac{3}{25} \cdot \frac{1}{2000} = \frac{3}{25} \cdot \frac{1}{2000}$$

$$\frac{2}{5}$$
 of $\frac{4}{5}$ of $\frac{4$

 $6_3^7 \times 65_4^3 \text{ cts.} = \frac{55}{2} \times \frac{26}{3} \text{ cts.} = \frac{14}{32} \frac{465}{2} \text{ cts} = $4.52\frac{1}{32}$

(5)

$$\frac{1}{3} + \frac{1}{10} + \frac{1}{3} + \frac{1}{10} = \frac{140}{120} + \frac{140}{120} + \frac{140}{120} = \frac{140}{120} =$$

(6)

$$\frac{5\frac{4}{6}-2\frac{1}{8}}{3\frac{3}{8}+\frac{9}{20}} \text{ of } \frac{4\frac{1}{2}+5\frac{19}{26}}{4\frac{1}{20}} \text{ of } \frac{2\frac{3}{6}+1\frac{3}{3}}{7\frac{19}{4}-2\frac{1}{4}} = \frac{5\frac{3}{4}\frac{5}{6}-2\frac{1}{40}}{3\frac{1}{2}\frac{5}{6}+\frac{9}{20}} \text{ of } \frac{4\frac{9}{8}\frac{5}{6}+5\frac{3}{8}\frac{8}{6}}{\frac{8}{20}} \text{ of } \frac{2\frac{3}{8}+\frac{1}{2}}{7\frac{19}{24}-2\frac{1}{4}} = \frac{3\frac{2}{4}\frac{7}{6}}{4\frac{2}{20}} \text{ of } \frac{10\frac{1}{6}\frac{3}{6}}{\frac{8}{2}\frac{1}{6}} \text{ of } \frac{4\frac{4}{15}}{5\frac{1}{2}\frac{3}{4}} = \frac{1\frac{47}{40}}{\frac{8}{4}} \text{ of } \frac{5\frac{13}{60}}{\frac{8}{2}\frac{1}{6}} \text{ of } \frac{9\frac{4}{8}}{\frac{1}{2}\frac{3}{4}} = \frac{2\times64}{2\times5} = \frac{128}{2\times5} = \frac{15\frac{3}{8}}{2\times5}$$

$$\frac{8}{2} \times \frac{1}{2} \times \frac{1}{2}$$

(7)

5×3×5

75

$$1670_{13}^{7} \times 12\frac{2}{4}$$
 cts. $= \frac{21717}{13} \times \frac{51}{4}$ cts. $= \frac{11071567}{52}$ cts. $= $212.99\frac{3}{2}$.

(8)

 $\frac{3}{3}$ of the longer $= \frac{3}{4}$ of the shorter; therefore $\frac{1}{3}$ of the longer $= \frac{1}{2}$ of $\frac{3}{4} = \frac{3}{8}$ of the shorter.

Hence the longer $= \frac{3}{8} \times 3 = \frac{9}{8}$ of the shorter.

5×188

5× 8

The whole tree = longer + shorter = $\frac{9}{8} + \frac{8}{8}$ of shorter = $\frac{137}{8}$ of the shorter.

If 136 ft. $=\frac{1}{8}^{7}$ of the shorter, $\frac{1}{17}$ of 136 $=8=\frac{1}{8}$ of the shorter. Hence shorter $=8\times8=64$ ft.; and longer =136-64=72 ft.

(9)

$$97\frac{1}{4} + 127\frac{2}{8} + 500\frac{2}{8} + 333\frac{1}{3} = 97\frac{30}{120} + 127\frac{48}{120} + 500\frac{45}{120} + 333\frac{40}{120} = 1057\frac{6}{12}\frac{2}{9} = 1058\frac{43}{120}.$$

 $\$1000 + \$1375\frac{1}{2} + \$6831 + \$4013\frac{3}{16} = \$1000 + \$1375\frac{8}{16} + \$6831 + \$4013\frac{3}{16} = \$13219\frac{1}{16} = \$13219 \cdot 68\frac{3}{4}.$

= 1.

= %.

 $\times \frac{4}{45} = 46$

\$4.5232,

1=

(10)

 $\begin{array}{lll} 12\frac{1}{6} + \frac{1}{16} = 13\frac{1}{16}, & 8\frac{1}{4} + 1\frac{1}{16} = 9\frac{1}{16}, & 13\frac{1}{3}\frac{1}{6} - 9\frac{1}{16} = 3\frac{1}{6}\frac{1}{6} = 2\frac{1}{6}\frac{1}{6}, \\ 7\frac{1}{16} - 6\frac{1}{16} = \frac{1}{12}, & \frac{2}{16}\frac{1}{1} \times \frac{1}{2} \times \frac{1}{2} = \frac{2}{16}\frac{2}{16}\frac{1}{16} = 14\frac{2}{16}\frac{1}{16}, \\ \frac{2}{16} + \frac{1}{16} = \frac{2}{16}\times \frac{1}{16} = \frac{2}{16}\frac{1}{16}\times \frac{1}{16}=\frac{2}{16}\frac{1}{16}\times \frac{1}{16}\times \frac{1}{16}=\frac{2}{16}\frac{1}{16}\times \frac{1}{16}\times \frac{1}{16}=\frac{2}{16}\frac{1}{16}\times \frac{1}{16}\times \frac{1}{16}\times \frac{1}{16}\times \frac{1}{16}\times \frac{1}{16}=\frac{2}{16}\frac{1}{16}\times \frac{1}{16}\times \frac{1}{16}\times \frac{1}{16}\times \frac{1}{16}=\frac{2}{16}\frac{1}{16}\times \frac{1}{16}\times \frac{1}{16$

(11)

 $197 \times $63 = \frac{169}{2} \times $97 = $1383 = $134.154.$

(12)

 $37611 \times $753 = 4779 \times $403 = 4087737 = $28387.061.$

(13)

 $147\frac{1}{3} + 320\frac{1}{5} = 147\frac{1}{5} + 320\frac{1}{5} = 467\frac{1}{5}$. $467\frac{1}{5} - 156\frac{1}{5} = 467\frac{1}{5} - 156\frac{1}{5} = 311\frac{2}{5}$.

 $\frac{7 (1\frac{1}{2} \text{ of } \frac{3}{2})}{\frac{1}{6} \left(\frac{3}{3\frac{1}{2}} \text{ of } 7\right)} \div 7\frac{7}{8} = \frac{\frac{7 \times \frac{3}{2} \times \frac{3}{4}}{\frac{3}{4} \times \frac{3}{4}}}{\frac{1}{6} \times \frac{3}{\frac{7}{4}} \times \frac{7}{4}} \div \frac{63}{8} = \frac{\frac{7 \times 3 \times 3}{1 \times 2 \times 4}}{\frac{1}{6} \times \frac{5}{7} \times \frac{7}{4}} \times \frac{8}{8} = \frac{7 \times 3 \times 3}{\frac{1}{6} \times \frac{5}{7} \times \frac{7}{4}} \times \frac{8}{8} = \frac{7 \times 3 \times 3}{\frac{1}{6} \times \frac{5}{7} \times \frac{7}{4}} \times \frac{8}{8} = \frac{7 \times 3 \times 3}{\frac{1}{6} \times \frac{5}{7} \times \frac{7}{4}} \times \frac{8}{8} = \frac{7 \times 3 \times 3}{\frac{1}{6} \times \frac{7}{4} \times \frac{7}{4}} \times \frac{8}{8} = \frac{7 \times 3 \times 3}{\frac{1}{6} \times \frac{7}{4} \times \frac{7}{4}} \times \frac{8}{8} = \frac{7 \times 3 \times 3}{\frac{1}{6} \times \frac{7}{4} \times \frac{7}{4}} \times \frac{8}{8} = \frac{7 \times 3 \times 3}{\frac{1}{6} \times \frac{7}{4} \times \frac{7}{4}} \times \frac{8}{8} = \frac{7 \times 3 \times 3}{\frac{1}{6} \times \frac{7}{4} \times \frac{7}{4}} \times \frac{8}{8} = \frac{7 \times 3 \times 3}{\frac{1}{6} \times \frac{7}{4} \times \frac{7}{4}} \times \frac{8}{8} = \frac{7 \times 3 \times 3}{\frac{1}{6} \times \frac{7}{4} \times \frac{7}{4}} \times \frac{8}{8} = \frac{7 \times 3 \times 3}{\frac{1}{6} \times \frac{7}{4} \times \frac{7}{4}} \times \frac{8}{8} = \frac{7 \times 3 \times 3}{\frac{1}{6} \times \frac{7}{4} \times \frac{7}{4}} \times \frac{8}{8} = \frac{7 \times 3 \times 3}{\frac{1}{6} \times \frac{7}{4} \times \frac{7}{4}} \times \frac{8}{8} = \frac{7 \times 3 \times 3}{\frac{1}{6} \times \frac{7}{4} \times \frac{7}{4}} \times \frac{8}{8} = \frac{7 \times 3 \times 3}{\frac{1}{6} \times \frac{7}{4} \times \frac{7}{4}} \times \frac{8}{8} = \frac{7 \times 3 \times 3}{\frac{1}{6} \times \frac{7}{4} \times \frac{7}{4}} \times \frac{8}{8} = \frac{7 \times 3 \times 3}{\frac{1}{6} \times \frac{7}{4} \times \frac{7}{4}} \times \frac{8}{8} = \frac{7 \times 3 \times 3}{\frac{1}{6} \times \frac{7}{4} \times \frac{7}{4}} \times \frac{8}{8} = \frac{7 \times 3 \times 3}{\frac{1}{6} \times \frac{7}{4} \times \frac{7}{4}} \times \frac{8}{8} = \frac{7 \times 3 \times 3}{\frac{1}{6} \times \frac{7}{4} \times \frac{7}{4}} \times \frac{8}{8} = \frac{7 \times 3 \times 3}{\frac{1}{6} \times \frac{7}{4} \times \frac{7}{4}} \times \frac{8}{8} = \frac{7 \times 3 \times 3}{\frac{1}{6} \times \frac{7}{4} \times \frac{7}{4}} \times \frac{8}{8} = \frac{7 \times 3 \times 3}{\frac{1}{6} \times \frac{7}{4} \times \frac{7}{4}} \times \frac{8}{8} = \frac{7 \times 3 \times 3}{\frac{1}{6} \times \frac{7}{4} \times \frac{7}{4}} \times \frac{8}{8} = \frac{7 \times 3 \times 3}{\frac{1}{6} \times \frac{7}{4}} \times \frac{7}{4} \times \frac{7}{4}$

$$\frac{\mathbb{Y} \times \mathbb{R} \times \mathbb{R}}{1 \times \mathbb{R} \times \mathbb{R}} \times \frac{\mathbb{R}}{\mathbb{R}} = 1. \quad \frac{\frac{1}{2} + \frac{1}{3} + \frac{1}{4}}{1 \quad 1 \quad 1} = \frac{\frac{6}{12} + \frac{4}{12} + \frac{3}{12}}{1 \quad 1 \quad 1} = \frac{1}{1 \quad 1 \quad 1} = \frac$$

(15)

 $17\frac{1}{7} \div 7\frac{1}{7} = \frac{123}{7} \div \frac{57}{7} = \frac{123}{7} \times \frac{7}{57} = \frac{123}{53} = 2\frac{17}{3}$

(16)

917=311=211.

 $\frac{7}{16} - \frac{1}{8} \frac{1}{6} = \frac{9}{8} \frac{7}{16}$

4.154.

38387.061.

3 - 1561 =

3×3

\$×7

 2×4 = 1/3 × ---

12 12

1 1

1-359

 $=2\frac{17}{53}$.

33 + 45 + 45 = 348 + 448 + 448 = 1348 = 788 $7^{\frac{1}{2}} - 5^{\frac{1}{2}} = 7^{\frac{1}{2}} = 7^{\frac{1}{2}} = 5^{\frac{1}{2}} = 2^{\frac{1}{2}} = 2^{\frac{1}{2}} = \frac{2}{12}$

 $94\frac{1}{6} + 93\frac{1}{9} = 94\frac{9}{7} + 93\frac{8}{7} = 187\frac{1}{7} = 13481$

22 193 × 44 ÷ 13481 = X × 18481 60

(17)

 $\begin{array}{l} 2\frac{1}{3} + \frac{1}{3} + 4 = 2\frac{1}{3} + \frac{1}{3} + 4 = 7\frac{7}{3} = \frac{1}{3}\frac{1}{3}. \\ 2 \div \frac{1}{3}\frac{1}{3} = 2 \times \frac{1}{3}\frac{7}{3} = \frac{1}{3}\frac{1}{3} - \frac{7}{3} = \frac{1}{3}\frac{1}{3} - \frac{7}{3} = \frac{1}{3}\frac{1}{3} - \frac{7}{3} = \frac{7}{3}. \\ \frac{1}{3}\frac{1}{3} + \frac{1}{3}\frac{1}{3} = \frac{1}{3}\frac{1}{3} - \frac{7}{3}\frac{1}{3} = \frac{7}{3}\frac{1}{3}. \end{array}$

583 - × - = 532. FØA 72

(18)

1+1=8. 11+23=412=42. 214-11=4=4.

187 187 187 49 $3\frac{1}{10}-3=247=\frac{1}{10}$ -=5376-x-x-x-X 3×12 36 12 20 92

13 + 21 = 1 × 3 = 70. 51 + 31 = 1 × 4 = 4 = 14. $_{16}^{7} + 1\frac{19}{26} = 2\frac{23}{53}$.

(19)

 $1 - (\frac{1}{3} + \frac{1}{3}) = \frac{1}{6}$. $\frac{2}{3}$ of $\frac{1}{3} = \frac{1}{6}$. $\frac{1}{3} - \frac{1}{6} = \frac{2}{16}$. $\frac{1}{6} + \frac{2}{16} = \frac{2}{16}$ $\frac{1}{8} - \frac{2}{30} = \frac{1}{30}$. $\frac{1}{30}$ of \$40000 = \$1333.33 $\frac{1}{3}$.

Exercise 66-Page 183.

(2) (1)

 $\frac{9}{25}$ =25)9 1=4)1 $\frac{1}{2} = 2)1$ 2=8)3

> ·25=25 . 375 $\cdot 36 = 36 \sigma$ • 5

97

(3)

75)73 (·9733+ 67.5	123)574(4·666+ 492	34)15 (.44117+
5.50	82.0	1.40
5.25	73 · 8	1.36
•250 •225	8·20 7·38	40 34
250	•820	60
225	•738	34
25	82	260 238
1	(4)	22

7)6 12)5 9)4 -857142+ ·4166+ ·44444+

(5)

112)17 (-15178571	1296)718 (·554012+				
5·80	800	70·00			
5·60	784	64·80			
·200	160	5·200			
·112	112	5·184			
880	480	1600			
784	448	1296			
960	320	3040			
896	224	2592			
640 560	960	448			
800	64				

Exercise 67-Page 184.

(1)	(2)	(3)
12)1·0 in.	12)17·0 grs.	20)7·0 grs.
3)2·083333 ft.	2)1·41666666	3)2.35 scr.
51)3·694444 yd.	20)3·70833333 dwt.	8)·7833333 dr.
2 2	12)·18541666 oz.	12)·0979166 oz.
11) 7·388888 40)·671717 per.	·01545138+ lb.	·0081597+1b.
·01679+ fur.		
(4)	(5)	(7)
12)9·0 in	4)2·0 na.	60)21·0 sec.
3)2·75 ft.	4)3·5 qr.	60)55·35 min.
$5\frac{1}{2})2 \cdot 91666$	·875 yd.	12)12·9225 hr.
2 2		2)1.076875
11)5.83333		·5384375 day.
40)35·53030 per.	(6)	
8)5.88825 far.	13s. 4d. = 160	d.
•73603+ mi	5s. = 60d. de. $\frac{60}{160} = \frac{3}{8} = \cdot 3$	375
(8)	. ,	(9)
3 of \(\frac{1}{2} \) of 6\(\frac{3}{4} \) d. =\(\frac{2}{2} \) d. a:		f 1 mil. = 12672 in.
\$7d.=1 of 27 of £3 =	$=\frac{27}{2240}$ of £\frac{1}{3}.	12)12672
$27 \div 2240 = 0$	012053.	2

F

7)25344

3620 - 571428+

44117+

[NAT ARITH.

0 60 38

22

·44444+

·554012+

3040 2592

448

(10)

\(\) of \(\frac{2}{5} \) of \(\frac{1}{3} \) lbs. \(= \frac{1}{3} \) lbs. \(= 110 \) \(\frac{1}{5} \) drs. \(= \frac{1}{16} \) drs. \(\frac{2}{16} \) of an oz. \(= 12 \) drs. \(\frac{1}{16} \) \(\frac{2}{16} \) \(\frac{1}{16} \)

1664(9.2444	L-f-	(11)	
1620	1	2)1.0 pts.	
440		4)1.5 qt.	
360		2)1·375 gal.	1
800 720	18 A	4)3·6875 pk.	
800 720	Mary of the de	•921875 hu	sh.
800 720	ejet •	S one of the second sec	
80			

Exercise 68-Page 186.

(1)	tt	(2)	(3)
•3945 24	,	•3965 * 8	·309153 20
15780 7890		3·1720 fur.	6·183060 dwt.
9·4680 60	hrs.	6.8800 per.	732240 366120
28·0800 60		44000 4400	4.393440 grs.
4.8000	sec.	4·8400 yds.	
		2·5200 ft.	
		6.2400 in.	

ts.

t.

5 gal. 75 pk.

1875 hush.

(3)

309153

183060 dwt. 24

732240 66120

393440 grs.

(4) (5)

EXERCISES 67, 68.1

 $22.75 = 22\frac{75}{100} = 22\frac{3}{4}$. 7 b. 1 p. 1 g. 1 qt. = 237 qts. £2 2s. $6d. \times 22\frac{3}{4} = £48$ 6s. $10\frac{1}{2}d$. $11.17825 \times 237 = 2649.24525$ qt. = 82 b. 3 p. 0 g. 1 q. 0.4905 pts

(6) -(7) (8) .2057 1 f. 36 p. 2 y. 5 in. = 15125 in. .625 12 $15125 \times .176 = 2662 \text{ in.} =$ 2.4684 oz. 1.875 mil. 13 per. 2 yds. 1 ft. 4 in. 20 9.3680 dwt. 7.000 fur. 24 14720 7360 8.8320 grs.

4 30¼
-500000 qt. 14400
2 120

1.000000 pt. 1.4520 yd.

9.7920 in. = 9 196 in.

Exercise 71-Page 191.

$$\begin{array}{ccc}
\cdot 0013 &= 5335. \\
\cdot 00007103 &= 557993355.
\end{array}$$

$$•987654321 = $$$7$$5$$333 = $197739369.$$

Exercise 72-Page 192.

KEY.

(3)

Exercise 73-Page 194.

141839

 $\frac{205}{99000} = \frac{41}{19800}$

(1)

Dissimilar.		Similar.	Si	milar and Coter	minous.
•9	=	99999	=	•999999999	
6.327	=	6.327272	=	6.3272727272	
19.43	=	19.43000	=	19.4300000000	
27.0278	=	27.027878	=	27.0278787878	
0347123	=	0347123	=	·0347123123 2	carried.

Sum, = 53.8198638274

NAT. ARITH.

909.

1936

= 334791.

1333881

= 3011535.

86		KI	EY.	[NAT. ARITH.
Dissimilar		Similar.	2)	Similar and Coterminous.
7-427	=	7.42727	= 7	1-427272727272727
9 · 1234	=	9.123423	= 8	123423423423423
17-298764	3 =	17.2987643 =	= 17	· · 298764376437643
18.67	=	18.67676 =	= 18	-676767676767676 2 carried
		•	= 52 3)	.526228203901471
Dissimila	r.	Similar.	-	milar and Coterminous.
4.95	=	4 959595	Billions Design	4.9595959595
7.164	=	7.1641641	=	7 · 1641641641
4.7123	=	4.7123123	= :	4.7123123123
•9731	7 =	- 101311	=	-9731777777 2 carried.
		Sum,		7-9092502138
Dissimilar.		Similar.		imilar and Coterminous
1.5	=	1.5000		1.500000000
99 • 083	=	99.0830	=	99.083000000
162	=	162162	=	.162162162
·814	=	·814814	=	·814814814
2.93	=	2.93939	=	2.939393939
3.769230	=	3.769230769	=	3.769230769
97.26	=	97.2666	OMATOMO OMATOMO	97-26666666
134.09	=	134.09090	=	134.090909090 3 carried.

Sum,

339 • 626177443

[NAT. ARITH.

carried.

oterminous

00

4.9

6

3

3 carried.

EXERCISE 74-Page 195.

(1)

Dissimilar. Similar and Coterminous.

 $729 \cdot 3\dot{4}\dot{2}\dot{7} = 729 \cdot 34\dot{2}\dot{7}\dot{4}\dot{2} = 729 \cdot 34\dot{2}\dot{7}\dot{4}\dot{2}$ $93 \cdot 126 = 93 \cdot 126\dot{0}\dot{0} = 93 \cdot 126\dot{0}\dot{0}\dot{0}$

636 · 216742

(2)

Dissimilar. Similar. Similar and Coterminous,

 $1 \cdot 437291 = 1 \cdot 43729137 = 1 \cdot 4372913729137$ $\cdot 00713 = \cdot 00713 = \cdot 007131313131313$

1.4301600597824

(3)

Dissimilar. Similar. Similar and Coterminous

1·12754 = 1·12754 = 1·12754754754754 ·47384 = ·473847 = ·47384738473847

•65370016280907

(4)

Dissimilar. Similar and Coterminous.

 $42 \cdot 18763 = 42 \cdot 1876333 = 42 \cdot 1876333333$

17.0000008432 = 17.0000008432 = 17.0000008432

25 · 1876324900

Exercise 75-Page 196.

$$2.9 = 23 = 3.$$
 $7.25 \times 3 = 21.75.$

•297 =
$$\frac{3.97}{9.99}$$
 = $\frac{1}{3}$ and 7.72 = $7\frac{73}{100}$ = $7\frac{18}{25}$ = $\frac{193}{25}$.

$$\frac{11}{37} \times \frac{193}{25} = \frac{91193}{925} = 2.29513.$$

•818 =
$$\frac{810}{990}$$
 = $\frac{9}{11}$ and •77 = $\frac{77}{100}$. $\frac{9}{10}$ × $\frac{77}{100}$ = $\frac{63}{100}$ = •63

$$1.735 = 1\frac{28}{90} = 1\frac{364}{496} = \frac{859}{496} \text{ and } .47053 = \frac{42848}{6000} = \frac{2689}{6000}.$$

$$\frac{159}{195} \times \frac{3528}{100} = \frac{39312511}{12500} = .81654168350$$

$$4.722 = 4\frac{650}{900} = 4\frac{3}{18} = \frac{85}{18}$$
 and $198 = \frac{198}{999} = \frac{28}{111}$.

Exercise 76-Page 196.

(1)

$$082 = \frac{82}{999}$$
 and $123 = \frac{123}{993} = \frac{41}{333}$.

$$\frac{82}{999} \div \frac{41}{413} = \frac{6}{99} \times \frac{33}{47} = \frac{2}{3} = \frac{6}{6}$$

(2)

389.185 =
$$389_{99}^{185} = \frac{388796}{999}$$
 and $15.7 = 157 = 142$.

$$\frac{388796}{399} \div \frac{143}{9} = \frac{388796}{999} \times \frac{0}{143} = \frac{2739}{111} = 24.6.$$

(3)

$$\cdot 81654168350 = \frac{81654986686}{99999999900088} = \frac{19206769837}{124999898780}.$$

 $=\frac{193}{25}$.

 $\frac{63}{00} = .63$

48 = 3529.

= 111.

337

1660786

(4)

Exercise 77.

(1)

 $\frac{1}{2}$ of $\frac{3}{16}$ of $14 = \frac{1}{2} \times \frac{3}{16} \times \frac{14}{16} = \frac{1}{8} = \frac{1}{8}$.

(2)

 $\begin{array}{l} \cdot 67 = \frac{61}{90} \text{ and } 2 \cdot 13 = 2\frac{13}{99} = \frac{211}{99}. \\ \frac{21}{9} \times \frac{211}{99} = \frac{1287}{8917} = 1 \cdot 4445566778 + \frac{1}{99}. \end{array}$

(3)

(4)

wk.

·678125 = 4 days 17 hours 55 minutes 30 seconds.

7

4.746875 days.

24 92437

2987500

1493750 92437 = \$\$\$\frac{3}{2}\frac{1}{2} = \frac{1}{2}\

17.925000 hours.

60

55.500000 minutes.

60

30.000000 seconds.

(5)

Dissimilar. Similar and Coterminous.

67-234 = 67-2343434 = 67-23434343434

98.713 = 98.71371371 = 98.71371371371

91.03471234 = 91.03471234 = 91.03471234234

Sum, = 256.98276949039

Dissimilar. Similar and Coterminous.

256.98276949039 = . 256.98276949039

100.123456789 = 100.12345678945

Difference = 156.85931270094

(6)

- 12) 9 in.
- 3) 2·75 ft.
- 51) 2.916 yds.
- 2 2
- 11) 5.833
- 40) 36·5303 rds.
 - 8) 5.913257 fur.

·739157196 miles.

(7)

17.428571 sq. ft. = $17\frac{42857}{999999}$ sq. ft. = $17\frac{3}{7}$ sq. ft.=17 sq. ft. 61\(\phi\) in

100.8 sq. in. = 1008

·73

D

Difference, = 16 sq. ft. 10453in,

oterminous.

43434 (

71371 84234

9039

ninous.

_

9.

5

. .

ft. 614 in

. 10458in,

(8)

91789772 917897

*91789772 of 2 a. = $\frac{99871875}{990000000} \times \frac{9}{1}$ a. = $\frac{99871875}{498700000} = \frac{99871875}{1}$ a. 13 per. 22 yds.

11.287 (9)

 $11 \cdot 287 = 11\frac{285}{1990} = 11\frac{10}{66}. \quad 1 \cdot 0428571 = 1\frac{428577}{99999990} = 1\frac{3}{70}.$

(10)

 $47.345 = \frac{17.345}{1000}$ and $1.76 = 176 = \frac{175}{100}$.

 $\frac{47345}{1000} \div \frac{175}{99} = \frac{47345}{1000} \times \frac{99}{176} = \frac{937431}{95000} = 26.7837428571.$

(11)

Dissimilar. Similar and Coterminous.

85·62 = 85·626 = 85.62626

13.76432 = 13.76432 = 13.76432

Difference, = 71.86193

(12) , (13)

•734 of a lb. = 11.744 oz. 2 ft. 5\frac{1}{3} in. = $29\frac{1}{3}$ in. = $\frac{8.8}{3}$ in.

·198 of an oz.= .198 oz.

 $27.3 \text{ ft.} = 27\frac{1}{3} \text{ ft.} = 328 \text{ in}$

Difference, = 11.546 oz.

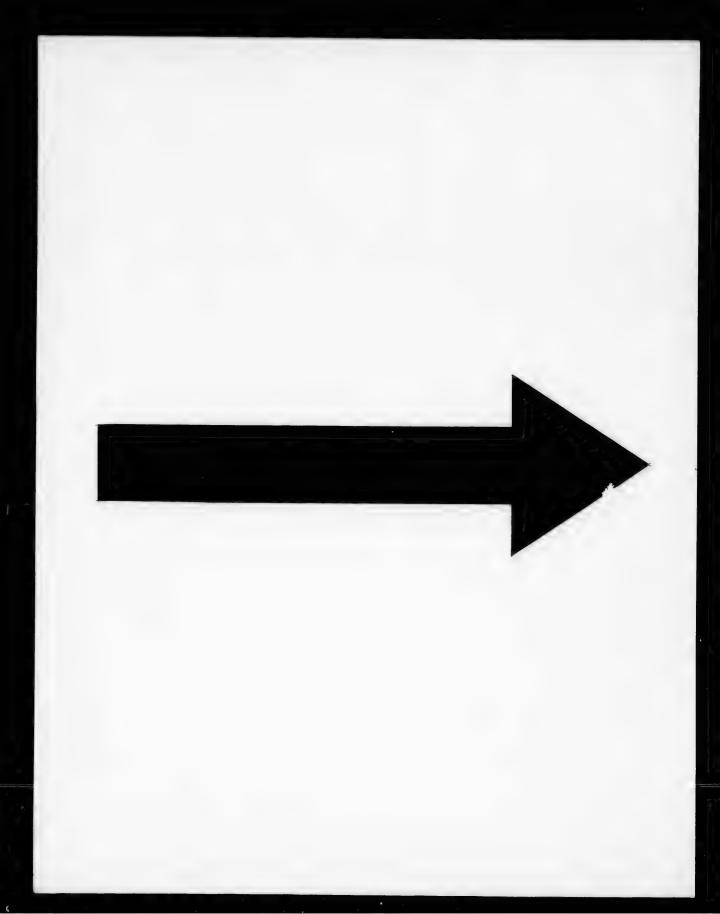
 $20.16 \text{ ft.} = 20\frac{1}{6} \text{ ft.} = 242 \text{ in.}$

 $328 \times 242 \div \frac{88}{3} = \frac{328}{1} \times \frac{242}{1} \times \frac{3}{88} = 2706 \text{ in.} = 75\frac{1}{6} \text{ yds.}$

(14)

 $3.145 = 3\frac{1}{9}\frac{4}{9}\frac{4}{9} = 3\frac{8}{56} = \frac{173}{56}$ and $4.297 = 4\frac{297}{595} = 4\frac{1}{3}\frac{1}{7} = \frac{159}{37}$.

 $\frac{173}{56} \times \frac{159}{37} = \frac{27507}{2135} = 13.5169533.$



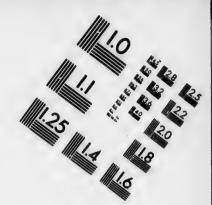
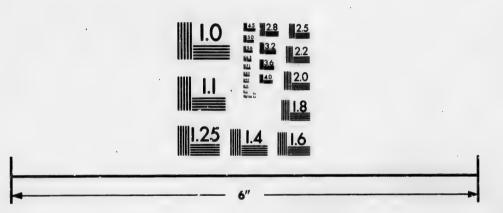


IMAGE EVALUATION TEST TARGET (MT-3)

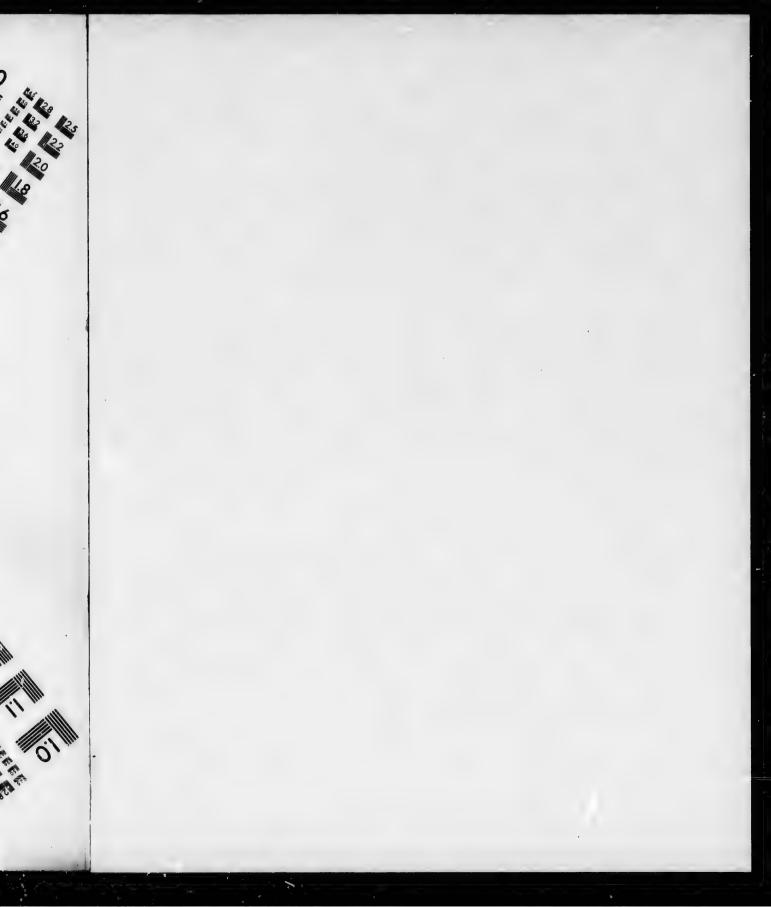


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2 carried

(15)

 $^{3}_{40}$. Here $40 = 2^{3} \times 5$. Therefore the equivalent decimal will contain 3 places $^{7}_{41}$. " $24 = 2^{3} \times 3$. " " " " 3 " $^{3}_{15}$. " $15 = 5 \times 3$. " " " " 1 4 $^{1}_{44}$. " $144 = 2^{4} \times 3^{2}$. " " " " " 4 " $^{1}_{44}$. " $15 = 5 \times 3$. " " " " " 1 4 $^{1}_{44}$. " $^{$

(16)

 $81\frac{3}{3} = 81 \cdot 6 \text{ and } 328\frac{33}{3} = 328 \cdot 23.$ Dissimilar. Similar Similar and Coterminous $81 \cdot 6 = 81 \cdot 666 = 81 \cdot 66666666$ $61 \cdot 126 = 61 \cdot 126 = 61 \cdot 12366666$ $328 \cdot 23 = 328 \cdot 2323 = 328 \cdot 23232323$ $5 \cdot 624 = 5 \cdot 62462 = 5 \cdot 62462462$

Sum, = 476.65028119(17) -2.83 6.8×3 \ 2.8×2.27

$$\frac{\left(\frac{1\cdot6+2\cdot629}{1\cdot6+2\cdot629} \times \frac{2\cdot25}{2\cdot25}\right) + \frac{1\cdot136}{1\cdot136}}{1\cdot136}$$

$$= \left(\frac{1\cdot61}{4\cdot296} \times \frac{20\cdot4}{2\cdot25}\right) + \frac{2\frac{4}{6} \times 2\frac{27}{99}}{1\frac{1}{9}\frac{3}{9}\frac{6}{9}}$$

$$= \left(\frac{1\frac{6}{9}\frac{5}{9}}{4\frac{2}{9}\frac{3}{9}\frac{6}{9}} \times \frac{20\frac{2}{8}}{2\frac{4}}\right) + \frac{2\frac{4}{7} \times 2\frac{3}{17}}{1\frac{3}{9}\frac{3}{9}}$$

$$= \left(\frac{1\frac{1}{1}\frac{1}{8}}{4\frac{2}{9}\frac{9}{9}} \times \frac{\frac{102}{2}}{\frac{3}{4}}\right) + \frac{\frac{1}{2}^{4} \times \frac{3}{17}}{\frac{25}{2}}$$

$$= \left(\frac{\frac{2}{1}\frac{3}{8}}{4\frac{2}{9}\frac{9}{9}} \times \frac{\frac{3}{4}}{\frac{3}{4}}\right) + \frac{\frac{1}{2}^{4} \times \frac{1}{17}}{\frac{2}{2}\frac{5}{2}}$$

$$= \left(\frac{\frac{1}{4}}{1\frac{1}{1}\frac{9}{1}} \times \frac{\frac{3}{4}}{\frac{3}{4}}\right) + \frac{\frac{7}{1}\frac{9}{1}}{\frac{2}{2}\frac{9}{9}} = \left(\frac{11}{2}\frac{1}{1} \times \frac{13}{16}\right) + \frac{28}{8}$$

$$= \left(\frac{3}{8} \times \frac{13}{16}\right) + \frac{28}{8} = \frac{17}{8} + \frac{28}{8} = \frac{48}{8} = 9.$$

72791 decimal.

E-morray 78-Page 198.

•	EXERCI	su 78	-Page	198	•		
ı		(1	1)				
∀ 9)431213	1	3)43	12131		8)43	12131	
9)22432	-	3)12	234023.	.2	8)2	42343	7
9)1204	35	3)2	224322	2	8)	14022	2
9)34	47	3)41240	2	8)1032	1
9)2	10	3)12043	1		8)32	6
	12	rum, silbo	3)2144	1	a regit som	2	1
			3)344	2			
			3)113	0	ende #18 in April ne i	on est among the	
			3)21	0			
,			3)3	2			
			1	0			
4010101 ~	10/	: 0758 :	100	111 10200	211222		/III 6127
4312131 = 5	9	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,		3	· 4	8	
23 5	11 9		; ; ; ; ; ; ; ; ; ; ; ; ; ; ; ; ; ; ;	3	299	17	
116	99			1	898	142	
582	898	**	3	3 3	2695	1137	
2911 5	8087	· · ·	9	9	8087	9098	
14558	72791	dec.	29	9	24263	72791	dec.

72791 dec.

ralent decimal ntain 3 places

1 3 "
1 1 "
1 4 "
1 "
1 9 "

d Coterminous

666666

366666

232323

462462 2 carried

028119

2.27

136

3

4

) +

(3)

 $976.432 \div 00000096 = 97643200000 \div 96 \text{ and } 96 = 12 \times 8.$

8)813693333333

1017116666-6

* (4)

$$\frac{(2\frac{7}{8} + .5625 - 15 + \frac{1}{16}) \div \frac{1}{3}}{(1\frac{6}{17} \times \frac{1}{8} \times 296 \times \frac{1}{16} + \frac{1}{16}) \div .9472947} =$$

(25+16-11+16)×11

a X A

$$\frac{\frac{16}{16}}{\frac{16}{12}} = \frac{\frac{16}{11}}{\frac{6}{11}} = \frac{16}{6} = 2\frac{3}{6}.$$

(5)

lbs. oz. dr. scr. lbs. oz. dr. scr. grs. 9 7 7 2) 97 3 4 1 17 12

115 8 1167 8 9340 3 3 2783 28021 20 55660) 5604376

560437(10,3837,55660

3837

KEY. (6)

 $96 = 12 \times 8$

X17X8291

[NAT. ARITH.

15 yds. = 540 in. and 7 ft. = 84 in. 6 ft. = 72 in. and 4 ft. = 48 in. $540 \times 84 \times 13$) - $(72 \times 48 \times 13)$ = 589680 - 44928 = 544752. $544752 \div 108 = 5044$

(7)

11 8 10"" 2//// 8 5 104 10 111 0 7 (8)

1167 . 1147 3 of 3+60f8 789

(9) (10)

77/77. 42. 27. 21. 33. 14. 7. 11. 63. 30 pts. 2)782436 6..27.. 8.. 8.. 2 27 4)391218..0 pt. 10 2)97804..2 qt.

 $77 \times 27 \times 10 = 20790 = 1$ c. m.

4)48902..0 gal.

12225..2 pks.

12225 bush. 2 pks. 0 gal. 2 qts.

	_			
1	1	1	•	

п		IX
**	0	

284)36187942(1375		814
28e4	· / 9	(12)
9e47 82t0 18679 17274 14054 11888 23882 23554	34 9 312 9 2810 9 25298	$150528 = 2^{10} \times 3 \times 7^{8}$ $10+1 = 11$ $1+1 = 2$ $2+1 = 3$ $11 \times 3 \times 2 = 66$
32t·0 28e·4 5t·80 55·t8 4·94	227683 9 2049151	
ah mb		/14\

(13)(14)

2 wks. 2 dys. = 16 d	ys.	72	81	= 8	1+	2 X	10+7	X	10 X	10.
·1234625	lbs.	OZ.	dr.				lbs.			
16	27	4		×	81	=	231	11	91	
			10							
7407750	-									
1234625	272	9		X	2	= .	545	3	12	
			10							
1.9754000 dys.										
24	2726	2	12	X	7	=	19083	3	4	
								-	-	
39016000							19860	2	91	
19508000										

23·4096000 hrs.

24·5760000 min.

34.5600000 = 34 15 sec.

OX3XT.

 $+7 \times 10 \times 10$. lbs. oz. dr.

231 11 94

545 3 12

083 3

860 2 91

11. 2

66.

(15)

£16 3s. $8\frac{1}{4}$ d. = \$64.74 $\frac{7}{1}$ g and £67 17s. $7\frac{1}{4}$ d. := \$271.52 $\frac{1}{12}$ c. \$98.17 + \$42.29 + \$64.74 $\frac{7}{12}$ g + \$97.19 + \$127.67 $\frac{1}{2}$ = \$430.27 $\frac{1}{12}$ g = \$158.75.

(16)

(18)

$$[\{(2\frac{1}{3} \times .5 \text{ of } 1\frac{1}{7}) + 9\frac{1}{7}] + .09 + \frac{33}{31}\} - 11\frac{6}{7}] \div (\frac{11}{6}) \text{ of } \cdot 16)$$

 $[(.7632763 \times 11) \times \frac{1}{8} \text{ of } \frac{10}{10} \frac{1}{6}] \times (\frac{1}{2} \text{ of } \cdot 2 \text{ of } \cdot 3 \text{ of } \cdot 25 \text{ of } 96) \div 2$

$$[\{(\frac{7}{3} \times \frac{1}{2} \times \frac{1}{7}) + 9\frac{1}{2}\frac{7}{4} + \frac{1}{1}\frac{1}{4} + \frac{2}{2}\frac{3}{3}\frac{7}{4}\} - 11\frac{6}{7}] \div (\frac{1}{6}\frac{1}{6})$$

$$(3638 \times \frac{1}{4} \times 8 \times 188 \times \frac{1}{4} \times 1 \times 1 \times 1 \times \frac{1}{4} \times \frac{1}{4} \times 1 \times 1 \times \frac{1}{4}) \div 8$$

$$\{(2+9\frac{1}{2}\frac{7}{4}+\frac{1}{17}+\frac{2}{2}\frac{3}{3}\frac{3}{1})-11\frac{6}{17}\}\div(\frac{1}{2}\frac{1}{1}\times\frac{1}{8})$$

1 × 87884 × 1

$$\frac{(12-11\frac{6}{17})\div(\frac{1}{2}+\frac{1}{2})}{\frac{1}{16}} = \frac{\frac{1}{1}\times\frac{6}{1}\times\frac{6}{1}}{\frac{1}{16}+\frac{1}{1}} = \frac{\frac{1}{1}}{\frac{1}{16}+\frac{1}{1}} = \frac{\frac{1}{1}}{\frac{1}} =$$

18891 = 34062.

(19)

8 children will have 8 children's shares.

One woman will have 3 children's shares \therefore 6 women will have $6 \times 3 = 18$ children's shares.

One man will have 6 children's shares \therefore 4 men will have $4 \times 6 = 24$ children's shares.

4 men, 6 women, and 8 child. will therefore have 50 child. shares.

£550 3s. $1\frac{1}{2}d. \div 50 = £11$ 0s. $0\frac{3}{2}d. = child's share.$

£ 11 0s. $0\frac{2}{4}$ d. \times 3 = £33 0s. $2\frac{1}{4}$ d. = woman's share.

£ 33 0s. $2\frac{1}{4}$ d. \times 2 = £66 0s. $4\frac{1}{4}$ d. = man's share.

(20)

 $16\frac{7}{11} + 19\frac{1}{8} + 23\frac{7}{8} + 129\frac{1}{7} = 16 + 19 + 23 + 129 + (\frac{7}{11} + \frac{1}{8} + \frac{7}{8} + \frac{1}{7}) = 187 + 3\frac{5}{3}\frac{19}{3}\frac{9}{6} = 190\frac{5}{3}\frac{19}{3}.$

(21)

 $8100 = 2^{\circ} \times 3^{4} \times 5^{\circ}$

1..3..9..27..81

1..2..4

1..3..9..27..81..2..6..18..54..162..4..12..36..108..324

1..3..9..27..81..2..6..18..54..162..4..12..36..108..324.. 5..15..45..135..405..10..30..90..270..810..20..60..180..

540..1620..25..75..225..675..2025..50..150..450..1350..

4050..100..300..900..2700..8100.

Therefore the divisors of 8100 are 1, 2, 3, 4, 5, 6, 9, 10, 12, 15, 18, 20, 25, 27, 30, 36, 45, 50, 54, 60, 75, 81, 90, 100, 108, 135, 150, 162, 180, 225, 270, 300, 324, 405, 450, 540, 675, 810, 900, 1350, 1620, 2025, 2700, 4050, 8100.

LCCB.

omen will have

men will have

50 child. shares. ld's share.

man's share.

n's share.

23 + 129 +190 308

..36.. 108 .. 324

..36..108..324..

..20..60..180.. 0.. 450.. 1350 ..

4, 5, 6, 9, 10, 12, 90, 100, 108, 135, 0, 675, 810, 900, (22)

2691)11817(4 10764

1053)2691(2

2106

585)1053(1 585

468)585(1 468

> 117)468(4 468

(23)

sec. 60)2551443

60)42524.. 3

24)708..44

29..12

29d, 12 h., 44 m., 3 sec. sec.

60)31556928

60)525948..48

24)8765..48

9828 is divisible by 117 ... 117 is the G. C. M.

365.. 5 365 d., 5 h., 48 m., 48 sec.

(24)

14 ft. 11 in. 179 in. 38 miles = 2407680 in. $2407680 \div 179 = 13450138.$

(25)

11 ft. \times 13 ft. \times 15 ft. = 2145 cub. ft.

One cubic foot weighs $62\frac{1}{2}$ lbs. $2145 \times 62\frac{1}{2} = 134062\frac{1}{2} = \text{weight}$ of 2145 cub. ft.

One gallon weighs 10 15s. $134062\frac{1}{2} \div 10 = 13406\frac{1}{4} = \text{gals. in}$ 1340624 lbs.

(26)

£73 \times 400 = \$292.00 $17s. \times 20 = 11\frac{2}{3}d. = 47 \text{ far. } \times 5 \div 12 = 11\frac{2}{3}d.$ 3.40 19,7

> £73 17s. 11ad. = \$295.597

> > (27)

 $93_{11}^{4} - 76_{23}^{17} = 92_{11}^{15} - 76_{13}^{17} = 16_{203}^{158} = \frac{4206}{203}$ 4206 258 1206 ÷ 203 = --=4999=2477- X -228 17

$$\frac{\frac{56 \div \frac{3}{3}}{1\frac{1}{5} \text{ of } \frac{5}{5} \div 10\frac{1}{3}}}{\frac{1}{15} \times \frac{3}{6} \times \frac{1}{3} \times \frac{1}{3}}{\frac{1}{3} \times \frac{1}{3} \times \frac{1}{3}}} \times \frac{3}{8} \times \frac{\frac{3}{3} \times \frac{3}{5}}{\frac{1}{3} \times \frac{1}{3}}}{\frac{1}{3} \times \frac{1}{3} \times \frac{1}{3}} \times \frac{3}{8} \times \frac{\frac{3}{3} \times \frac{3}{5}}{\frac{3}{3} \times \frac{3}{3}}}{\frac{3}{1} \times \frac{1}{3} \times \frac{1}{3}}} = \frac{\frac{1}{3} \times \frac{3}{3} \times \frac{3}{3}}{\frac{3}{1} \times \frac{3}{3}}}{\frac{3}{1} \times \frac{3}{3} \times \frac{3}{3}} = \frac{\frac{3}{3} \times \frac{3}{3}}{\frac{3}{1} \times \frac{3}{3}} = \frac{\frac{3}{3} \times \frac{3}{3}}{\frac{3}{3} \times \frac{3}{3}} = \frac{\frac{3}{3} \times \frac{3}{3}}{\frac{3}{1} \times \frac{3}{3}} = \frac{\frac{3}{3} \times \frac{3}{3}}{\frac{3}{3}} = \frac{\frac{3}{3} \times \frac{3}{3}}{\frac{3}} = \frac{3}{3} \times \frac{3}{3} = \frac{3}{3} \times \frac{3}{3} = \frac{3}$$

$$\frac{\frac{8}{45 \times 3 \times 31}}{16 \times 2} \times \frac{8}{5} \times \frac{87}{\frac{2 \times 8 \times 87 \times 2}{127}} = \frac{3 \times 9 \times 31}{16 \times 2 \times 2 \times 2} = \frac{3 \times 9 \times 31}{16 \times 2 \times 2 \times 2} = \frac{3 \times 9 \times 31}{16 \times 2 \times 2 \times 2}$$

			pe -
5)91342		12)91342	2)91342
5)190	744	12)83 <i>t</i> 49	2)461761
5)40	151	12)7731	2)230930
5)8	8910	12)703	2)115t11
5)	1843	65	2)62160
5)393	•	2)31530
	5)82	,	2)16270

5)8 · 2 1..3 2)1627..0 2)869..0 2)434..1 2)217..1

 $2)\overline{109..0}$ $2)\overline{5t..0}$ $2)\overline{2t..1}$

2)15..0 2)8..0 2)4..0 2)2..9

1..0

 $\frac{1\times 9\times 31}{\times 2\times 2\times 2}$

жі 2)91342

2)46176..1

2)23093..0 2)115t1..1

> 2)62t6..0 2)3153..0 2)1627..0

(29 continued.)

	•			
XI.	. A	xII	11	
. 91342 11	132330 5	14 65319 12	1000	000100110000101
100		77	2 2	260
1103	42	927	4 2	521
12137	213	11125	8 2	1043
133509 dec.	-	133509 dec.	16	2086
	5340		32	4172
	26701		2 65	8344
	5 133509 dec.	•	130	16688
			2	2
	•		200	3:377
				66754 3
		·		183509 dec.

2)434..1 2)217..1 2)109..0

2)869..0

2) 5t..0

2)2t...1

2)15..0

2)8..0

2)4..0

2)2..9

1..0

\$1

21

for

six

23

\$.1

\$1

(30) (30) (30) (30) (30) (30)	(31) m. f. p. y. ft. i	in. (32)
2)3840	72 3 7 2 1	$\$.47 \times 97 = \$.45.59.$
2)1920	579 fur.	(33)
2)960		(73×4×11)÷128=25,8.
2)480	23167 per. 51	\$3.621×2532=\$90.9631.
2)240	115837	
2)120	115831	
2)60	1274 01 yds.	
2)30	382262} ft.	·
3)15	12	
5	4587157 in. 12	
1	55045884 lines	•

(34)

93.723 = 93750 =
$$\frac{92786}{93750}$$
 and 29.4173 = 29550 = $\frac{293850}{111}$ = $\frac{92786}{293879}$ = $\frac{92786 \times 111}{11 \times 293879}$ = (35)

One bushel of oats weighs 34 lbs. ... in 73429 lbs. there are $73429 \div 34 = 2159\frac{3}{3}$ bushels.

(36)

In 719630 lbs. of wheat there are 719630 \div 60 = 11993 5_6 bus. \$1.80 \times 11993 5_6 = \$21588.90, Or \$1.80 per bushel = 3 cents per lb. 719630 \times 3 = 2158890 cents. = \$21588.90,

(38)

< 97 = \$45·59.

(33)

11)-128=2534.

2532=\$90.9631.

(32)

21389)180781(8 171112

(37)

9669)21389(2 19338

\$72.14 + \$93.76 = \$165.90

2051)9669(4

 $$165.90 \times 9.47 = 1571.0730

8204

 $$1571.0730 \div 11 = $142.8248 +$

1465)2051(1 1465

586)1465(2

1172

293)586(2

Last divisor 293 = G. C. M.

(39)

75, 4, 9, 33, 14, 70, 1.

The least common multiple of 11, 5, 7, 33, 14, 10 and 2 is 2310. The multiplier for both terms of the first fraction is ${}^{23}1^{+0}$ = 210; for the second, $^{23}_{10} = 462$; for the third, $^{23}_{10} = 330$; for the fourth, $\frac{2310}{33} = 70$; for the fifth, $\frac{2310}{14} = 165$; for the sixth, ${}^{23}_{10}{}^{10} = 231$; for the seventh, ${}^{23}_{10}{}^{10} = 1155$.

Multiplying by these numbers, we obtain 1478, 1848, 2370, 2370, $\frac{560}{2310}$, $\frac{1816}{2310}$, $\frac{16}{2310}$, and $\frac{1168}{2310}$ for the required fractions.

(40)

 $\$.11 \times 17 = \1.87 . $\$.37\frac{1}{2} \times 19 = \$7.12\frac{1}{2}$. $\$2.17 \times 14\frac{1}{2} =$ \$31.46\frac{1}{2}\$. \$.27 \times 67 = \$18.09\$. \$1.37\frac{1}{2} \times 15 = \$20.62\frac{1}{2}\$. \$1.87 + \$7.121 + \$31.461 + \$4.75 + \$11.50 + \$18.09 + $$20.62\frac{1}{4} + $7.93 = $103.35\frac{1}{4}$

168 **— 2**83872.

786×111 $\times 293879$

29 lbs. there are

60 = 119935 bus. r 1b.

1588.90.

Exercise 84-Page 210.

(1)

Baskets.
$$$13.42: \frac{1.22}{$18.43 \times 87} = $106.14.$$

(2)

(8)

(4)

(5)

Feet. ft.
$$7 \times 112$$

5 : 112 :: 7 : $\frac{7 \times 112}{5} = 156$ ft.

(6)

Cows. days.
$$\frac{9}{39 \times 27} = 48^3_5$$
 days.

(7)

Acres. bus.
$$9 \times 48$$

5 : 48 :: 9 : $\frac{9 \times 48}{5}$ = 86% bush.

(8)

Perches. days. 2×808 73:803:: 2:--== 22 days. ZB.

176 22

(10)

-58 155 \$20.88×465

103:465:: \$20.88: -108

86

(11)

9 639 \$ 5 brls. 73×1278

16: 1278:: 72: ____ = 5751 barrels.

(12)

Men. Acres 165×3 11:3::165: - = 45 acres.

(13)

125

Barrels, loaves 250×67 4: 67 :: 250 : - = 4187 loaves.

(14)

Bushels. brls. 16×88 190: 38:: 16: $\frac{190}{190} = 3\frac{1}{3}$ barrels.

6.14.

549 days.

\$124.80.

lays,

(15)

Days. men 99×12

 $15: 12:: 90: \frac{44 \times 12}{15} = 72 \text{ men}$

(16)

D'. work. brls. 2×279

17: 279 :: 2: $\frac{2}{17}$ = 32\frac{1}{4} barrels.

(17)

Hours. miles.

 $1:24::27:27\times 24=648$ miles.

(18)

Cows. lbs. 30×23

 $7:23::30:\frac{}{7}=98\frac{4}{7}$ lbs.

Exercise 85-Page 211.

(1)

 $\frac{1}{6}: \frac{31}{36}:: \$9750: \frac{\frac{375}{250}}{1} \times \frac{\frac{21}{25}}{\frac{26}{3}} \times \frac{16}{8} = \$42000.$

(2)

Yard. s. 5 $\frac{1}{8} : \frac{3}{4} : \frac{3}{4} : \frac{3}{7} = \frac{3}{2} = 2^{6} d.$

(3)

Tons. $\frac{3}{3}:8\frac{1}{3}::\$7.49:\frac{\$7.49\times8\frac{1}{3}}{\frac{7}{4}}=\frac{1.07}{1}\times\frac{25}{8}\times\frac{3}{7}=\$80.25.$

(4)

·14 4·06

Yards. \$28.42: \(\frac{28.42}{\times 4} \) \(\frac{5}{2} \) \(\frac{28.42}{\times 4} \) \(\frac{7}{2} \) \(\frac{7}

ls.

(5)

,

Dollar. bag $\frac{4}{5} : \frac{7}{40} :: \frac{3}{5} : \frac{7}{5} : \frac{3}{5} : \frac{7}{40} :: \frac{3}{5} :: \frac{3}{5} :: \frac{3}{40} :: \frac{3}{5} :: \frac{3}{5} :: \frac{3}{40} :: \frac{3}{5} :: \frac{3} :: \frac{3}{5} :: \frac{3}{5} :: \frac{3}{5} :: \frac{3}{5} :: \frac{3}{5} :: \frac{3}$

(6)

(7)

Tons. days. $107_{17}^{3} \times 11\frac{1}{17}$ $1180 \times \frac{9}{128} \times \frac{5}{17} = 70\frac{185}{187}$ dys. $17\frac{3}{6} : 11\frac{1}{17} :: 107_{18}^{3} : \frac{107_{18}^{3} \times 11\frac{1}{17}}{17_{8}^{3}} = \frac{11}{11} \times \frac{1}{17} \times \frac{5}{88} = 70\frac{185}{187}$ dys.

(8)

Tons. cords. $22\frac{1}{3} \times 11\frac{9}{26} = \frac{20\frac{1}{3} \times 11\frac{9}{26}}{15\frac{7}{16}} = \frac{20\frac{1}{3}}{9} \times \frac{295}{26} \times \frac{18}{202} = 16\frac{7}{18}$ cords.

(9)

Yds. yds \$ $\frac{3}{1}$ of $\frac{3}{3}$ of $\frac{3}{3}$

 $\frac{4}{11} \times \frac{15}{165} = \$_{2} \%.$

224

Exercise 86—Page 212.

(1)

37 sq. yds. 4 ft. 120 in. = 48648 in., and 9 sq. yds. 2 ft. = 11952 in.

2027

Inches. 3.50×48648

11952: 48648:: \$3·50; _____ = \$14·245-

11952

498

= \$80.25.

12000.

2.80.

(2)

12 lbs. 10 oz. = 154 oz.

Ounces.

1: 154:: \$1.25: $1.25 \times 154 = 192.50 .

(3)

10 yds. = 40 qrs., and 3 yds. 2 qrs. = 14 qrs.

.17

Quarters.

B-46×14 40:14::\$3.40:---=\$1.19.

> Ø¥ 20

(4)

15 oz. 12 dwt. 16 grs. = 7504 grs., and 13 oz. 14 grs. = 6254 grs.

. 95 3127

Grains.

B - 86×8324

7504: 6254:: \$3.80: --= \$3·167 + * BOX

1876

938

3 lbs. 1 oz. 11 dwt.=751 dwt. and 12 lbs. 6 oz. 4 dwt.=3004 dwt.

(5)

150

Dwt. 600×X21

3004: 751:: 600: ----= \$150.

B004

(6)

Barrels. h. m. s. 2 h. 46 m. 39 s. x 24

54: 24:: 2 46 30: = 1 hr. 14 min.

安東

(7)

73 yds. 3 qrs. 2 na. 1 in= $2660\frac{1}{2}$ in. 3 Fl. e. 2 qrs. 1 na.= $101\frac{1}{4}$ in. And £4 17s. $8\frac{1}{4}$ d. = $1172\frac{1}{4}$ d.

Inches. d. $\frac{1172\frac{1}{4} \times 2660\frac{1}{4}}{101\frac{1}{4} : 2660\frac{1}{4} : \frac{1172\frac{1}{4} : \frac{2}{101\frac{1}{4}}}{101\frac{1}{4}} = \frac{\frac{521}{4889} \times \frac{5321}{2}}{\frac{3}{4} \times \frac{3}{2}} \times \frac{\frac{3}{498}}{\frac{3}{45}} = \frac{2779341}{299} \text{ d.} = £128 \text{ 6s. } 1084d.$

(8)

(9)

Pages. $\frac{156 \times 400}{327 : 400 :: 156 : \frac{227}{327} = 190 \frac{20}{109}$, i. e. on the 191st p.

(10)

46 a., 3 r., 14 p. = 7494 p., and 35 a., 2 r., 10 p. = 5690 p.

Perches. £ $100 \times 5690 = £75$ 18s. 63 147d.

7494 : 5690 :: 100 : $\frac{100 \times 5690}{100 \times 100} = £75$ 18s. 63 147d.

(11)

Days. miles. 12×68 48: 68:: 12: $\frac{17}{48}$ =17 miles per day.

·50.

4 qrs.

rs. = 6254 grs.

167+

rt.=3004 dwt.

r. 14 min.

(12)

Shillings. 1bs. $\frac{113}{7} \times \frac{113}{7} \times \frac{3}{7} \times \frac{3}{84} = \frac{38307}{1568} = 24 \frac{775}{568}$ lbs

(13)

 $17493 \times 1000 \times 5$ cub. ft. = 87465000 cub. ft. $192724 \times 1000 \times 4$ cub. ft. = 770896000 cub. ft. 87465000 + 770896000 = 858361000 cub. ft.

Cubic feet. ton. 858361000 = 95373\frac{4}{9000} = 95373\frac{4}{9000} tons.

(14)

 $50000 \times 9000 = 450000000 = \text{cub. ft. of gas in } 50000 \text{ tons of coal}$ Cubic feet. hour.

4: 450000000 :: 1: 450000000 = 112500000 h.= 12842 y. 170 d.

(15)

lbs. lbs. lbs. lb. lb. $4+3+2+1+\frac{1}{2}=10\frac{1}{2}$ lbs.

101: 11270 :: 1: $\frac{11270}{10\frac{1}{2}}$ =1073, and 31 lbs. remaining.

(16)

 $180 \text{ miles} = 180 \times 1760 = 316800 \text{ yards}.$

Yards. day.

100: 316800: 1: $\frac{100}{100}$ = 3168 dys. or about 83 yrs.

Exercise 87-Page 216.

* (1)

120: 90 bush. 6: 14 horses.

7 15 :: 56 days : - 130×6 \$6×90×14

 $-=7\times14=98\,\mathrm{days}$.

(2)

28: 32 ft. high. $: \frac{69 \times 33 \times 15}{8 \times 28} = 9 \times 15 = 135 \text{ men.}$

(3)

3: 45 length. \} ::1 lb.: \(\frac{45}{25 \times 45} = \frac{45}{25 \times 4} \) $\frac{3 \times 11}{3 \times 11} = \frac{1}{15} = \frac{3 \times 4}{15} = 3 \times 4 = 12 \text{ lbs.}$ 11: 1 width.

(4)

10: 100 length. $: 3 \text{ lbs.} : \frac{3 \times 1\frac{1}{4} \times 100}{1\frac{1}{4} \times 10} = 2 \times 1\frac{1}{4} \times 10 = 25 \text{ lbs.}$

(5)

44: 132 tons. $\left. \begin{array}{c} 2 & 8 \\ 12 \times 5 \times 182 \end{array} \right.$ 18: 5 days. $\left. \begin{array}{c} 2 & 8 \\ 12 \times 5 \times 182 \end{array} \right.$

 $-=2\times5=10$ horses. 44 × 18

(6)

4: 14 men. : 27s.: 27×14×10 $-=27\times5=135s.=£6$ 15s. 7 : 10 days.) XXX

ib. ft. cub. ft.

= 24 (575 lbs

ıs.

00 tons of coal

12842 y. 170 d.

tining.

rds.

out 83 yrs.

(7)

3:5 masters.

8:10 apprentices.

5:8 weeks

6:51 days per wk.

144×51×8×10×5

BXBXBXB

86×18×5

6×4

 $=3\times2\times6=36$ men.

6

3

13

19

(8)

6: 18 s.mak.)

4 : 5 weeks.

:: 36 pairs of men's shoes :-

135 pairs men's and the women's = $\frac{24}{36} = \frac{9}{3}$ of 135 = 90 pairs.

(9)

3 2 9: 18 feet high. 13×18×6

: 12 men : -4 : 6 days.

#X#

(10)

130: 390 miles.) 3×14×840 :: 3 days :- $=3\times2\times3=18$ days. 7: 14 hours. 186×4

(11)

10 : 60 oz.) 60×30 80 80 1

221 : 30 d. 10×221 1 1 10

(12)

10: 5 compositors)

7: 14 hours.

20: 40 sheets. 24: 16 pages.

50: 60 lines.

40 : 50 letters.

16×5× 14×40×16× 60×50 :: 16 days :-

10×7×20×24×50×40 Jan 1 1

 $2 \times 16 = 32$ days.

0×5

(18×5 6×4 f 135 = 90 pairs.

 $\times 2 \times 6 = 36$ men.

 $\times 2 \times 3 = 18$ days.

 $-=4\times2=8d$ 15

X16× 60×50

DF×04×FE

(13)

386 : 240 men. 5 : 9 days. 10 : 12 hours. 6 : 5 degrees. 5: 3 yards wide

3 : 2 yards deep

en grant and A to b 70×340×9×13×5×8×2 :: 70 yards : -\$\$6×5×10×6×5×\$ $9 \times 2 \times 2 = 36$ yards.

(14)

6: 12 horses. 4: 9 months. : 16 acres : 4 2 4: 9 months. $-=4\times2\times9=72$ acres. Water State 6XX

(15)

12 25: 139 persons) \$90×139×7 :: 300 bush. : _____ = 11676 bushels. 1 : 7 years.

(16) 3 2 108 4×84×864×5×8 48: 32 men. . 36: 864 feet long. :: 4 days : -8: 5 feet high. 48×88×8×4 16 4: 3 feet wide.

(17)

679: 22407 sold's. :: 702 bushels: — 234 33 265×55462×113 \$48×849 $234 \times 33 = 7722$ bushels.

(18)

* . To work that I 28 13: 494 suits.) 12×494×27 19: 27 days. \ :: 12 tailors : \ \ \ \frac{18 \times 18}{1} - = 648 tailors. 18 × 18

18

11 42

(19)

```
17:40 head of cattle 30:51 days. : 5 a. 2 r. 10 p. : 5 a. 2 r. 10
```

5 a. 2 r. 10 p. × 4 = 22 a. 1 r.

(20)

Exercise 88.—Page 21

(1)

31 baskets peaches = 24 dollars
12 dollars = 2 tons

12 dollars = 2 tons35 tons = x cords

 $\frac{17 \times 17 \times 19 \times 92 \times 31 \times 12 \times 35}{116 \times 28 \times 92 \times 57 \times 22 \times 2} = \frac{31 \times 35}{2 \times 2 \times 2} = \frac{1085}{8} = 135\frac{5}{8}.$ (2)

6 lbs. tea = 29 lbs. sugar
17 lbs. sugar = 1 bushel
27 bushels = 4 tons
34 tons = 15 cows
29 cows = 1160 dollars
20 dollars = x lbs. tea.

 $\frac{3}{6 \times 17 \times 27 \times 34 \times 29 \times 20} = \frac{17 \times 17 \times 27}{5 \times 58} = \frac{7803}{2903} = 26\frac{28}{29}$

7 2 11

2

```
4 B
```

17×80

 $\frac{1085}{8} = 135\frac{5}{8}$.

280³ = 26²⁵/₂5

(3)

(4)

$$\frac{\frac{4}{29 \times 7 \times 187 \times 4 \times 11 \times 69 \times 21}}{\frac{16 \times 17 \times 74 \times 91 \times 11 \times 792}{4}} = \frac{11 \times 7 \times 21}{4} = \frac{1617}{4} = 4041.$$

(5)

$$\left\{
 \begin{array}{l}
 7 \text{ A} = 11 \text{ B} \\
 5 \text{ B} = 8 \text{ C} \\
 15 \text{ C} = 21 \text{ D} \\
 11 \text{ D} = 5 \text{ E} \\
 42 \text{ E} = x \text{ A}
 \end{array}
 \right\} = \frac{7 \times 5 \times 15 \times 11 \times 42}{11 \times 8 \times 21 \times 5} = \frac{7 \times 15}{4} = \frac{105}{4} = 26\frac{1}{4}$$

d

11 qu

(6)

7 barrels flour = 23 cords
6 cords = 11 cwt.
46 cwt. = £28
£77 = 9 sheep
5 sheep = 8 tons
9 tons =
$$x$$
 barrels flour

 $\frac{3}{3}$ $\frac{7}{7}$
 $\frac{3}{4}$ $\frac{7}{4}$
 $\frac{3}{4}$
 $\frac{3}{4}$
 $\frac{7}{4}$
 $\frac{3}{4}$
 $\frac{7}{4}$
 $\frac{3}{4}$
 $\frac{7}{4}$
 $\frac{3}{4}$
 $\frac{7}{4}$
 $\frac{3}{4}$
 $\frac{7}{4}$
 $\frac{7}{4$

15×24×50×48071

$$\frac{20 \times 22 \times 20}{5} = 961 \times 6 = 5769 \text{ s.} = £288 \text{ 9s.}$$

(7)

EXERCISE 89.—Page 222.

$$\frac{7}{8} \times \frac{17}{11} \times \frac{28}{29} \times \frac{11}{119} \times \frac{2}{69} = \frac{2}{3} = 2:2$$

£119
$$\times$$
 400 = \$476.00
164. \times 20 = 3.20
61d. = 36 far. \times 5 ÷ 12 \cdot 10%
£119 16s. 61d = \$479 30%

(4)

$$\begin{array}{c} 9: 13 = 9 \div 13 = \cdot 692 \\ 21: 27 = 21 \div 27 = \cdot 777 \\ 7: 10 = 7 \div 10 = \cdot 7 \\ 17: 15 = 11 \div 15 = \cdot 733 \end{array}$$

Hence 21: 27 is the greatest, and 9: 13 the least.

(5)

Dissimilar. Similar. Similar and Coterminous. $76 \cdot 23478 = 76 \cdot 234784784784784784784$ $19 \cdot 1342291 = 19 \cdot 134229122912291$ $Difference, = 57 \cdot 100555661872493$

(6)

71324t undenary = 1146287 denary, 23421 quinary = 1736 denary, and t4e7 duodenary = 17995 denary.

 $1146287 \times 1736 = 1989954232 \div 17995 = 110583_{17}^{13}_{17}^{14}_{9}^{7}$. $110583_{17}^{13}_{9}^{14}_{9}^{7}$ denary* = $53ee3_{17}^{7}_{17}^{3}_{7}^{7}$ duodenary, $12014313_{10}^{11}_{9}^{10}_{14}^{14}_{9}^{7}$ quinary, and $760t0_{12}^{9}_{12}^{7}_{12}^{7}_{7}$ undenary.

(7)

 $= 13\frac{1}{8}$.

=

= £288 9s.

 $\frac{2}{2} = 2 : 3$

)) §

) 5

^{*} To reduce the fractional part, reduce both numerator and denominator separately.

```
yds. qrs. na. in. yds. qrs. na. in.
  17)63 3
                2 1 (3 3 0 011
     51
                            ·913625 of an acre = ·913625×4840=
     12
                               4421 · 945 sq. yds.
                                4421 · 945 × $.67=$2962 · 70+
     51
     51
                                                      (10)
                           \frac{1}{8} of \frac{3}{6} of \frac{7}{8} of 20 bush. \times \cdot 5 \times \cdot 6 \times \frac{7}{8} =
                             1 × 3 × 7 × 20 × 1 × 3 × 7 =
                          \frac{40}{32} bush. = 1 bush. 2 pks. 0 gal. 1 qt.
      21
     5\frac{1}{2} = \frac{1}{2} \div 17 = \frac{1}{3}\frac{1}{4}
                                    (12)
Whole amount of increase = 2571437 - 1842265 = 729172.
                                      729172×100
   1842265 : 100 :: 729172 : -
```

$$1842265 : 100 :: 729172 : \frac{729172 \times 100}{1842265} = 39 \text{ per cent.}$$

$$\begin{array}{c} (13) \\ \frac{1}{3} \text{ of } \frac{2}{3} \text{ of } \frac{18}{29} - \frac{1}{8} \text{ of } \frac{2}{3} \text{ of } \frac{5}{3} = \frac{9}{29} - \frac{5}{84} = \frac{3}{2} \frac{9}{436}. \end{array}$$

100: 7::11:
$$\frac{11\times7}{100} = \frac{700}{100}$$
. $11 - \frac{700}{100} = 10_{100}^{23}$.

(15)

$$79 \times 16 \times \pounds \cdot 00163 = \pounds 2 \cdot 06032 = \pounds 2 \ 1s. \ 2\frac{208}{6}\frac{1}{2}d.$$

$$\begin{array}{c}
(16) \\
3 \\
10:12 \text{ hours} \\
20:35 \text{ acres}
\end{array}$$
::31 days:
$$\frac{21 \times 3 \times 12 \times 35}{4 \times 10 \times 20} = \frac{63}{16} = 3 \frac{15}{6} \text{ days.}$$

(9)

13625×4840=

2962 - 70+

0)

 $\cdot 5 \times \cdot 6 \times 7 =$ $\times 3 \times 7 =$

. 0 gal. 1 qt.

5 = 729172.

39 per cent.

359

23

. 2898đ.

= 3 days.

(17)

 $(\frac{1}{2} \text{ of } \frac{9}{1} \times \cdot 02 \times \cdot 456) \div (\frac{1}{2} \text{ of } \frac{9}{2} \text{ of } \frac{1}{2} \text{ of } 51) =$

76

1 152 17 8 8 1 2×38

5 11 50 888 16 2 1 51 5×11×25×37

(18)

- × $\times -= 4 \times 13 = 52$

(19)

50 barrels = 125 yards

80 yards = 6 bales,

13 bales = 31 hogsheads x hogsheads = 1000 barrels

5 3 125

125×6×31×1000 $125\times3\times3$

50×80×13 2×13 2 16

(20)

 $73.47 \times .0063 \div 17.2345 = \frac{7.347}{1.00} \times \frac{63}{10000} \div \frac{5739}{3330} =$

7347 63 3330

- x -- x - $-=\frac{154132713}{37391000000}=\cdot026856599989+$ 100 10000 57391

(21)

2 roods 7 per. 4 yds. 3 ft. 117 in. = 3416481 in. and 7 acres = 43908480 inches.

3416481-43908480 = .0778+

(22

 $\frac{2}{7}$ of $\frac{1}{5}$ of 70 miles $=\frac{16}{3}$ miles $=5 \cdot 33333 + \text{miles}$. $\cdot 73$ of 11 fur. $=8 \cdot 03$ fur. $=1 \cdot 00375$ mile. $5 \cdot 33333 - 1 \cdot 00375 = 4 \cdot 32958$ miles.

(23)

274312 nonary = 167195 denary, 1101011010 = 858 denary, and .5555 septenary = 2000 denary.

 $167195 - 858 = 166337 \times 2000 = 332674000.$

332674000 denary = 764876837 nonary.

= 10011110101000011001111010000 binary, = 11146453021 septenary.

(24)

275 | 44. 275. 18. 190. 200. 225 18. 18. 10. 9 275 × 38 × 18 = 188100 = 1. c. m.

(25)

10:6 weeks

6:5 days

11:10 hours

2400:8742 feet long

18:20 feet wide

11:8 feet high

men $60 \times 6 \times 5 \times 10 \times 8743 \times 20 \times 8$:: 60: $\frac{60 \times 6 \times 5 \times 10 \times 8743 \times 20 \times 8}{10 \times 6 \times 11 \times 2400 \times 18 \times 11}$

 $\frac{5\times2914\times2}{11\times3\times11} = \frac{29140}{363} = 80\frac{100}{363}.$

(26)

 $172000 = 2^6 \times 5^3 \times 43$. Increasing each exponent by 1 and multiplying them together we obtain $6 \times 4 \times 2 = 48$.

3333+miles. 5 mile. iles.

858 denary, and

674000.

11010000 binary,

2914 BX43×30×8

11×8E×9

nent by 1 and (2 = 48.

(27)

42 $7 = 42\frac{7}{9} = \frac{385}{9}$ and $9 \cdot 7i23 = 9\frac{1}{9}\frac{16}{9} = 9\frac{11}{10}\frac{86}{66} = \frac{16171}{1669}$. $\frac{385}{9} \times \frac{16171}{1666} = \frac{6625895}{1988} = 415 \cdot 471137804.$

(28)

 $73 \cdot 42 \times 27$ 100 : 27 :: \$73.42 : -=\$19.8234.100 $\$73 \cdot 42 - \$19 \cdot 8234 = \$53 \cdot 5966.$

(29)

 $6300 = 2^2 \times 3^2 \times 5^2 \times 7.$

1..5..25

1..2.. 4

1..5..25..2..10..50..4..20..100

1..3.. 9

1..5..25..2..10..50..4..20..100..3..15..75..6..30..150..

12..60..300..9..45..225..18..90..450..36..180..900

1..5..25..2..10..50..4..20..100..3..15..75..6..30..150..

12..60..300...9..45..225..18..90..450..36..180..900..7..

35..175..14..70..350..28..140..700..21..105...525...42 .

210..1050..84..420..2100..63..315..1575..126..630..3150 ..252..1260..6300.

Therefore the divisors of 6300 are 1, 2, 3, 4, 5, 6, 7, 9, 10, 12, 14, 15, 18, 20, 21, 25, 28, 30, 35, 36, 42, 45, 50, 60, 63, 70, 75, 84, 90, 100, 105, 126, 140, 150, 175, 180, 210, 225, 252, 300, 315, 350, 420, 450, 525, 630, 700, 900, 1050, 1260, 1575, 2100, 3150, 6300

 $\frac{2}{7}$ of $\frac{3}{8}$ of $3\frac{1}{2}$ lbs. = $\frac{3}{8}$ lbs., $\frac{9}{7}$ of $\frac{3}{6}$ of $\frac{3}{2}$ of $\frac{3}{7}$ of $\frac{3}{7}$ of $\frac{3}{7}$ of $\frac{3}{7}$ of $\frac{3}{7}$ and $\frac{3}{8}$ of $\frac{7}{9}$ of $\frac{1}{10}$ of $\frac{21}{60}$ of 90 lbs. $=\frac{1}{200}\frac{323}{00}$ lbs.

441 lbs. \$ 3 × 1322 1838 3 : 1323 :: 8 · X - $=\frac{126}{25} = $5.04.$ 200

(31)

7 men will have 7 men's shares.

One woman has 1_{1}^{3} of a man's share; ... 2 women will have 2 $\times 1_{1}^{3} = 1_{1}^{6}$ of a man's share.

One child has f of $f_1^3 = f_2^6$ of a man's share; ... 11 children will have $f_1^3 = f_2^6$ of a man's share.

7 men, 2 women, and 11 children will have 7 + 16 + 6 = 877 men's shares.

\$2739 \cdot 18 \div 8\frac{7}{7} = \$325 \cdot 99\frac{1}{6}\frac{3}{4}\frac{7}{7} = a man's share.

\$\gamma^3\tau\$ of \$325 \cdot 99\frac{6}{6}\frac{3}{4}\frac{7}{7} = \$888 \cdot 90\frac{4}{6}\frac{4}{7} = a woman's share.

\$\frac{2}{7}\$ of \$88 \cdot 90\frac{4}{6}\frac{4}{4}\frac{7}{7} = \$25 \cdot 40\frac{1}{6}\frac{2}{4}\frac{7}{7} = a child's share.

23 bush. 2 pks. 1 gal. 1 qt. 1 pt. = 1515 pts. 1515 \times 9000 \times 1 = 4545000 in. = 71 miles 5 fur. 34 per. 3 yds.

$$\frac{4158}{10395} = \frac{462}{1155} = \frac{66}{165} = \frac{22}{55} = \frac{2}{5}$$

(37

VIII.

 $\frac{1}{2}$, $\frac{2}{3}$, $\frac{4}{5}$, $\frac{3}{7}$. Here the common denominator is $2 \times 3 \times 5 \times 7 = 322$. The numerators of the fractions are, for the first, $1 \times 3 \times 5 \times 7 = 151$; for the second, $2 \times 2 \times 5 \times 7 = 214$; for the third, $4 \times 2 \times 3 \times 7 = 250$; for the fourth, $2 \times 2 \times 3 \times 5 = 74$; and the equivalent fractions are, $\frac{151}{322}$, $\frac{214}{322}$, $\frac{2}{322}$, and $\frac{74}{322}$, which when added together $=\frac{731}{322}=2\frac{65}{322}$, the numbers all through being in the octenary scale.

women will have 2

; . 11 children

s share.

an's share. 's share.

(34)

$$= 104 : 5.$$

515 pts. ur. 34 per. 3 yds.

2 × 3 × 5 × 7 for the first, 1 x \times 7 = 214; for h, $2 \times 2 \times 3 \times$ $\frac{1}{2}$, $\frac{21}{32}$, $\frac{4}{32}$, $\frac{25}{32}$, and the numbers all

$$\begin{vmatrix}
 17 \text{ sheep} &= 6 & \text{cows} \\
 26 & \text{cows} &= 27 \text{ acres} \\
 12 & \text{acres} &= 13 & \text{horses} \\
 11 & \text{horses} &= 28 & \text{goats} \\
 x & \text{goats} &= 68 & \text{sheep}
 \end{vmatrix}
 = \frac{8}{17} \times \frac{21}{26} \times \frac{18}{12} \times \frac{28}{11} \times \frac{18}{1} \times \frac{28}{1} \times \frac{18}{1} \times \frac{28}{11} \times \frac{18}{1} \times \frac{18}{11} \times$$

 $21 \times 28 = 70$ goats.

(39)

Exercise 90 .- Page 226.

(1)

 $\$.35 \times 92647 = \32426.45 .

(2) £ g d. 4d. | 1 4746 17 0 = cost of 94937 pails at 1s. 1d. | 1 1582 5 8 = " " 395 11 5 = " " " at 1d.

£6724 14 1 = cost of 94937 pails at 1s. 5d.

(3) (4) $\$ \cdot 071 \times 95972 = \$7197 \cdot 90$ $$28.80 \times 62 = 1785.60 . (5) (6)

 $\$ \cdot 32\frac{1}{4} \times 2310 = \$750.75.$ $\$ \cdot 37\frac{1}{4} \times 2117 = \$793 \cdot 87\frac{1}{4}$ (7)

£ g d. 6d. | 1 . 375 6 0 = price of 7506 pairs at 1s. 3d. 4 187 13 0 = 66 66 at 6d. 2d. 1 93 16 6 = 46 46 - at 3d. 23 9 11 = 44 at 2d.

£680 4 $7\frac{1}{2}$ = price of 7506 pairs at 1s. $9\frac{3}{4}$ d.

Then £171 10

1

```
(8)
                                                   (9)
 \$ \cdot 171 \times 1217 = \$212.971
                                     $3.071 \times 2103 = $6466.721.
                                 (10)
    10s.
                 2096
                    3
              £6288
                           0 = cost of 2096 oz. at £3.
     58.
                1048
                           0 =
                                                 at
                                                      0 10s.
 2s. 6d.
                 524
                           0=
                                                 at
                                                          5a.
 1s. 3d.
                 262
                           0 =
                                                 at
                                                          2s. 6d.
   11d.
         4
                 131
                           0 =
                                    44
                                                 at
                                                          1s. 3d.
                  13
                           0 =
                                    44
                                            "
                                                 at
                                                         0 13d.
              £8266
                           0=
                                            66
                                                at £3 18s. 101d.
                                (11)
        10 dwt.] 1
                      $1.55
                           6 .
                      $9.30
                               = cost of 6 oz.
         5 dwt.
                  ł
                        . . 771 =
                                     " 10 dwt.
2 dwt. 12 grs.
                         ·383 =
                                          5 dwt.
I dwt. 6 grs.
                         ·194 =
                                      11
                                          2 dwt. 12 grs.
        2 grs.
                 13
                         ·09 | =
                                      44
                                          1 dwt. 6 grs.
                         00\frac{31}{48} =
                                          2 grs.
                     $10.75\frac{23}{24} = cost of 6 oz. 18 dwt. 20 grs.
                               (12)
  10s.
             £98 0
                       0 = \cos t of 98 yards at £1.
  58.
              49
                       0=
                                                   0 10s.
              24 10
                       0 =
                                "
                                                      5s.
           £171 10
                      0 = \cos t of 98 yards at £1 15s.
2 qrs.
             £1 15
1 gr.
                  17
                      6 = \cos t \text{ of } 2 \text{ qrs.}
l na.
        ł
                   8
                      9 =
                                " 1 qr.
                   2
                      21 =
                                    1 na.
             £1 8 \cdot 5 = cost of 3 qrs. 1 na.
```

 $5\frac{1}{4}$ = cost of 3 qrs. 1 na. at £1 15s. per yard. £172 18 $5\frac{1}{4}$ = cost of 98 yds. 3 qrs. 1 na. at £1 15s. per yd

0 = cost of 98 yards at £1 15s.

(9) 03 = \$6466 · 721.

£3.

0 10s.

0 58.

0 2s. 6d. 0 1s. 3d.

0 0 13d.

£3 18s. 101d.

2 grs.

6 grs.

dwt. 20 grs.

1. 0 10s.

0 5s.

1 15s.

s. per yard.

£1 15s. per yd

```
(13)
1s. 20
         £1376
                    0 = rent of 344 acres at £4.
ld.
            17
                   0=
                           46
                                        at
                                            0 ls.
                    8 ==
                            66
                                        at
                                           0.
                                               0 1d.
        £1394 12 8 = rent of 344 acres at £4 1s. 1d
```

£1394 12 8 = rent of 344 acres at £4 1s. 1d. $\frac{3 \ 8 \ 4_{32}^{31}}{2}$ " 3 roods 15 per. at £4 1s. 1d. per ac. £1398 1 0_{22}^{31} = " 344 a. 3 r. 15 per. at £4 1s. 1d.

(14)

(15)

2 qrs.
$$\begin{vmatrix} \frac{1}{2} \\ \frac{1}{2} \end{vmatrix}$$
 £1 2 4
£4 9 4 = price of 4 yards at £1 2 4 per yard
11 2 = " 2 qrs. " "
2 9½ = " 2 na. " "
1 4½ = " 1 na. " "
£5 4 8½ = price of 4 yds. 2 qrs. 3 na."

(16)

1 rood.
$$\frac{1}{4}$$
 $\frac{\pounds 1}{32}$ $\frac{\pounds 57}{12}$ 0 = price of 32 acres at £1 16s.
9 0 = " 1 rood. " $\frac{1}{2}$ peri $\frac{1}{5}$ $\frac{1}{5}$ = " 10 per. " $\frac{5}{3}$ = " 2 per. " $\frac{5}{3}$ = " 2 per. " $\frac{5}{3}$ = " 2 per. " $\frac{1}{4}$ $\frac{1}{5}$ = price of 32 acres 1 rood 14 per.

(17)

(18)

 $\$1.67\frac{1}{2} \times 724 = \$1212.70.$

(19)

 $$1.933 \times 721 = $1396.933.$

£1 2 4 per yard

"

" " 66

na." 16

£1 16s.

"

77

ood 14 per.

6d. per gal.

(20) 10s. 4514 2 £9028 0 0 = cost of 4514 rods at £2. 6s. 8d. 🖠 2257 0 0= 44 at 0 10 10d. 1 1504 13 4= 44-44 at 0 6 8 1d. 10 188 1 8= " " at 0 0 10 d. + 18 16 2 =" " at 0 0 1 9 8 1= " 46 at 0 0 01 £13005 19 3= " " at £2 17 74

(21) 10s. | . \frac{1}{2} | £3749 7 6 3 £11248 2 6 = price of 3749 acres at £3 58. 1874 13 9 = " Ť at 0 10 ' 6d. 937 6 101= 10 " at: 0 5 93 14 81= " at 0 £14153 17 93 = price of 37493 acres at £3 15 6

(22)

 $|£17 0 0 = \cos t \text{ of } 17 \text{ cwt. at } £1$ 8d. 3 8 0= 66 66 1d. 11 4= " " at 0 0 8 **1** 5= at 0 0

£21 0 9 = cost of 17 cwt. at £1 4 9

1 qr. | ‡ £1 4 9 16 lbs. + 6 21 = cost of 1 qr. 1 15. 16 $36\frac{3}{7} = "16 lbs.$ 0 273= " 1 lb.

9 $11_{712}^{37} =$ " 1 qr. 17 lbs.

£21 0 9 = cost of 17 cwt. at £1 4s. 9d. per cwt. 9 $11_{11}^{37} =$ " 1 qr. 17'lbs.

£21 10 $8_{11}^{37} =$ " 17 cwt. 1 qr. 17 lbs. " "

1

(23)

2 qrs.	1 1	\$11.55					,
		78					,
		9240	-			4	
		8085					•
		\$900.90	=	cost of	78 cw1	t. at \$11.55	707 0
l qr.	7	5.771	-		2 qrs.	"	per cwi
7 lbs.	1	2 . 883			1 qr.	"	"
lbs.	+	·723	=	44	7 lbs.		44
l lb.	1	•414	=	"	4 lbs.		**

(24)

£10 10 20

£210 0 = price of 20 tons at £10 10s.

19 cwt. 3 qrs. $27\frac{1}{3}$ lbs. = 1 ton. $-\frac{1}{2}$ lb. The price of 1 ton is £10 10s., and the price of $\frac{1}{2}$ lb. = $\frac{1}{4480}$ of £10 10s. = $\frac{63}{112}$ d. . . . the price of 19 cwt. 3 qrs. $27\frac{1}{2}$ lbs. =£10 10s. $-\frac{63}{112}$ d. =£10 9s. $11\frac{49}{112}$ d.

£210 0 0 = price of 20 tons at £10 10s. 10 9 11_{112}^{49} = " 19 cwt. 3 qrs. $27\frac{1}{2}$ lbs.

£220 9 11_{112}^{49} = " 20 tons 19 cwt. 3 qrs. $27_{\frac{1}{2}}^{\frac{1}{2}}$ lbs. at £10 10s. per ton.

	(2

219				
219				
950	•			•
550		•		
0				
.50 =	price of	219 tons	nt \$45.50) nowdon
		10 cwt.	"	por ton
.371 =		5 cwt.	66	"
.271 =		1 cwt.	86	"
		2 qrs.	66	"
56% =	"		66	66
	$13\frac{3}{2} = 56\frac{7}{8} =$	133 = " 567 = "	133 = " 2 grs.	133 = " 2 qrs. "

Exercise 91—Page 228.

BILLS OF PARCELS.

(No. 2.)					
9 pair of worsted starts	d.		£	8.	d.
9 pair of worsted stockings, at 4	6	per pair	2	0	R
o pair of sink ditto, at	0	44		14	_
17 pair of thread ditto. at.		"		14.	8
23 pair of cotton ditto, at.	10	66			_
14 pair of yarn ditto, at	10		D	11	2
10 main of	4	**	1	12	8
18 pair of women's silk gloves, at 4	2	66 .	3	15	0.
19 yards of flannel, at 1	71	per yard	1	10	101

•	Ans. £2	3 15 41
(No. 3.)		
751 lbs. of sugar, at 72	cents per lb.	\$5 -854
os ins. of tea, at	"	58.59
126 lbs. of butter, at	66	16.38
354 lbs. of raisins, at	"	6.711
17 lbs. of sago, at	() () () () () () () ()	2.55
23 lbs. of rice, at	" "	2.07
581 lbs. of starch, at22	"	12.87
•	4	

Ans. \$105.022

" "

1.55 per cwt.

46 " 66

"

12 lbs.

10s.

price of 1 ton is 10 10s. $= \frac{63}{112}$ d. 10 10s. — 163 d·

s. bs.

rs. 27½ lbs. at er ton.

1		٨				
	108 Samenta 1 22	(No. 4.)			
	198 Sangster's National A 197 Robertson's Philosop	rithmetic	, at	\$0.60	211	0.00
	197 Robertson's Philosop 83 Hodgins' Geography.	hy of Gra	mmar, at.	0.50		
	83 Hodgins' Geography, 57 Sangster's Algebraic	at	*****	1.00		8.50
	57 Sangster's Algebraic l 217 Strachan's Canadian I	Formula,	at	0.101		3.00
	217 Strachan's Canadian I 143 Hodgins' Geography of	Penmansh	in. at.	0.124		1.121
	143 Hodgins' Geography of 227 Sangster's First Arithm	British P	rovinces	0.374		.371
	227 Sangster's First Arithm	netic, at.	zovinces, at	0.45		35
				0.30	68	.10
		(No. 5.)		Ans. \$	521	25
		_	d.			
	91 yards of silk, at			£	s.	d.
	Jarus of Howered ditta	04 32	9 per yard	6	1	11
	4 Julus Of Hustring, at			10	1	6
	- " Julus VI Drocade at		10 "	4	0	31
	4 Julus OI Satin, at		3 "	7	17	6
	113 yards of velvet, at	10	8 "	6	10	8
	1	18	0 "	10	4	9
	•	,	An	8. £44		-
		(No. 6.)		o. £44	15 1	10
	- Thecacuanha at		@0 ob			
	College Colleg		-		\$9 ·	
	THE COURT OF THE PARTY OF THE P				20 ·	47
			1 A - A		21 -:	25
					54 . 2	25
	56 " gum camphor, at	••••••	0.61		16 .4	17.
		••••••	0.27		15-1	2
				Ans. \$1:	36.0	_
	(1	Vo. 7.)		ψ1.	90.9	4
	151 lbs. of currents		s. d.	£ s.	. d.	
]	151 lbs. of currents, at	••••••	0 4 per li		-	
1	171 lbs. of Malaga raisins, at	••••••	0 51 "		10	,
1	193 lbs. of sun raisins, at	•••••	0 6 "		10	
	The state of the s		0 31 "	4	_	
	pepper, at		1 6 "	12	111	
	TO OI BUDNE WATCHE TO	1 44	0 81 "	1 3	9	
-	3 oz. of cloves, at	•••••	0 9 per of	- 0	01	
			o por o		9	
1.			Ans.	£3 13	51	
	2.00					

Exercisus 91, 92.1

```
...$0.60 $118.80
... 0.50
           98.50
... 1.00
           83.00
... 0.121
            7.121
.. 0.371
           81.371
at 0.45
          64 35
. 0.30
          68 - 10
```

d

Ans. \$136.94

		+	0 04
	£	s.	đ.
lb.		5	2
14		7	107
6		9	101
6		4	111
•		12	9
	1	3	01
oz.		9	9
-			

s. £3 13 51

Exercise 92-Page 231.

(2)

 $427 \cdot 1 \div \cdot 0000637 = 4271000000 \div 637 = 6704866 \cdot 561 + .$

(3)

10s.
$$\begin{vmatrix} \frac{1}{2} \\ \frac{1}{2} \end{vmatrix}$$

171

19

25s. $\begin{vmatrix} \frac{1}{4} \\ \frac{1}{4} \end{vmatrix}$

26d. $\begin{vmatrix} \frac{1}{4} \\ \frac{1}{4} \end{vmatrix}$

2d. $\begin{vmatrix} \frac{1}{4} \\ \frac{1}{4} \end{vmatrix}$

2e. $\begin{vmatrix} \frac{1}{4} \\ \frac{1}{4} \end{vmatrix}$

2f. $\begin{vmatrix} \frac{1}{4} \\ \frac{1}{4} \end{vmatrix}$

2f.

£379 19 $7\frac{1}{4} = \cos t \text{ of } 19 \text{ tons at } £19 19 11\frac{3}{4}$

19 cwt. 3 qrs. $27\frac{1}{2}$ lbs. = 1 ton $-\frac{1}{2}$ lb. The price of 1 ton is 19 19s. 11 $\frac{3}{4}$ d., and the cost of $\frac{1}{2}$ lb. $=\frac{1}{4480}$ of £19 19s. 11 $\frac{3}{4}$ d. = 1_{17320}^{1279} d.; ... the cost of 19 cwt. 3 qrs. 27_{2}^{1} lbs. = £19 19s. 11\frac{2}{4}\,\text{d}. \rightarrow 1_1\frac{1}{2}\frac{7}{9}\text{d}\,\text{d}. = £19 19s. $10_{177900}^{12160}\text{d}.$ £379 19 71 = cost of 19 tons.

19 19 $10\frac{12161}{7920} =$ 19 cwt. 3 qrs. 27½ lbs.

£399 19 $5\frac{16641}{17920}$ = " 19 tons 19 cwt. 3 qrs. 27½ lbs.

(4)

Dissimilar.	F	Similar.	8	Similar and Coterminous.
73 - 723	=	73 - 723723	=	73 • 723723723
11.342	=	11.3422	=	11.34222222
16.713	=	16.7130	=	16.713000000
19.034	=	19.034034	=	19.034034034
713 • 213437		713 • 213437	=	713 · 213437437
12.345678	=	12.345678345		12.345678345 2 carried.

 $Sum = 846 \cdot 372095763$

(5)

5:
$$7 = 5 \div 7 = .714 + 9 : 13 = .9 \div 13 = .692 + 12 : 17 = 12 \div 17 = .705 + 12 : 10 = .7 \div 10 = .7$$
Hence 5: 7 is the greatest, and 9: 13 least.

$$\frac{5}{7} \times \frac{9}{13} \times \frac{12}{17} \times \frac{7}{10} = \frac{54}{221} = 54 : 221.$$

(6)

1 acre = 160 rods, and 25 acres 2 roods 35 rods = 4115 rods.

rods.
$$160:4115:: \$80.50: \frac{40.25}{80.50} \times 4115 = \$2070.3593.$$

$$\frac{160}{16}$$

(8)

 $$3.684 \times 7439 = $27431.314.$

and Coterminous.

723723723

34222222

713000000

34034034

13437437

45678345

2 carried.

72095763

the greatest,

ast.

221.

ls = 4115 rods.

2070 - 3593.

(9)

135795. The G. C. M. of 135795 and 222210 is 12345; when both terms of the fraction are divided by 12345, it becomes 11/8.

714235. Here 714235 and 999999 have no G. C. M.; .. the fraction cannot be reduced.

 $\frac{1003375}{100000}$. The G. C. M. of 109375 and 100000 is 3125; when both terms of the fraction are divided by 3125, it becomes reduced to 35.

 $\frac{20301}{33633}$. The G. C. M. of 20301 and 33633 is 303; when both terms of the fraction are divided by 303, it is reduced to its lowest terms, viz., 67

(10)

34½ bushels turnips = 17 bushels potatoes
9 " potatoes =
$$59\frac{1}{2}$$
 lbs.tea
6 lbs. tea = $11\frac{1}{2}$ stone flour
13 stone flour = 360 cents
38 cents = 12 lbs.based

$$38 \text{ cents}$$
 = 12 lbs. bread
119 lbs bread = x bushels turnips

$$\frac{\frac{3}{84\frac{1}{3}}}{17} \times \frac{\frac{9}{59\frac{1}{3}}}{\frac{59}{8\frac{1}{3}}} \times \frac{\frac{8}{11\frac{1}{3}}}{11\frac{1}{3}} \times \frac{\frac{19}{89}}{\frac{19}{40}} \times \frac{\frac{19}{89}}{\frac{12}{3}} \times \frac{\frac{7}{119}}{1} = \frac{3 \times 13 \times 19}{8\frac{1}{3} \times 40} = 2\frac{61}{340}$$

(11)

$$=\frac{7\times11}{2\times3}=12\frac{5}{6}\,\mathrm{days}.$$

		(13)	,
12)723	42	1x. 6)72342	1X. 3)72342
12)540	32	6)118062	3)237132
12)40	-	6)17310	3)72340
-	07	6)2644	3)23711
,	23	6)404	3)7231
		6)60	3)2370
`.		10	3)721
	, englisher :	Rd 1	3)232
ł			21
x.	-		

				21
72342	XII. = 23702	VI.	ı	
9	12	= 1004402	= 21	02101102
		6	3	
65	0 =		_	
9	27	6	7	
•	12	6	3	
×00	-	-	_	
588	331	36	21	
9	12	6		
-		_	3	
5296	3972	220	-	
9	. 12		65	1765
	-	6	3	3
47666	47666	1004		-
, , , , ,	**************************************	1324	196	5296
		6	3	3
		-	-	
		7944	588	15888
		6	3	
		4.50		3
		47666	1765	47666

IX. 3)72342

3)23713..2 3)7234..0 3)2371..1

3)723..1 3)237..0

3)72..1 3)23..2 3)7..0

2..1

2102101102

1765

5296

15888 3

47666

III

3

21 3

65

3

196

588

765

		1

		(14)	
II.		ıv.	•
1111(1 2	100000	333333	100000
-	eed	4	4
3	·	Circus .	ele a company
2	2	15	4
		. 4	S 4
7	4	-	7 -
2	19.3	63	16
- K	2	4	4
15	7		
2	8	255	64
-	· 15 . HOURS	. * 4 . *	4
31			
2	16	1023	256
	, 2	4	4
63 Greates	,	4095 Greates	1024 Least.
	VI.	VIII.	vIII.
55555	100000	777777	
6	6	8	100000
-		_	8.
35	6	63	_
6	6	8	8
-	****		. 8
215	36	511	-
6	6	8	64
			8
1295	216	4095	er man
6	6	. 8	512
	-	-	8
7775	1296	32767	4096
1	6	8 7 17	8
46655 Greatest.	7776 Least. 2	262143 Greatest.	32768
	(Continued o	n next page.)	
	,	a next page.)	

(14 continued.)

Mi.			XII.
			AII.
			100000
. 12			12
* minima			
143			16
12			12
			12
****			-
1727			144
12		٠,	12
-			14
20735	100.40		
			1728
12,		1 . 6	- 12
0.1000			
248831		4_	20736
12			
-			12
2985983 Greatest.			
		248832 Least.	

(15)

 $1728 = 2^6 \times 3^3$.

1..2..4..8..16..32..64

1..3..9..27

1..2..4..8..16..32..64..3..6..12..24..48..96..192..9..
18..36..72..144..288..576..27..54..108..216..432..864..

Therefore the divisors of 1728 are 1, 2, 3, 4, 6, 8, 9, 12, 16, 18, 24, 27, 32, 36, 48, 54, 64, 72, 96, 108, 144, 192, 216, 288, 432, 576, 864, 1728.

(16)

30 2 · 4 · 6 · 8 · 10 · 12 · 14 · 16 · 18 · 20 · 22 · 24 · 26 · 28 · 30 14 2 4 2 · 7 · 8 · 3 · 2 · 11 · 4 · 13 · 14 12 4 4 · 8 11 · 2 · 13 14 18

 $30 \times 14 \times 12 \times 143 = 720720 = 1$. c. m.

0000

ast.

6..192..9.. .432..864..

3, 8, 9, 12, 16, 216, 288, 432,

Dissimilar. Similar. Similar and Coterminous.

97.91342 = 97.913423 = 97.913423423423423423

18.1234567 = 19.1234567 = 18.123456745674567

Difference = 79.789966677748855

(18)

20 ft. 7' 19 ft. 5 7" 1 0 0 1"'' 8 6 11 391 1

400 7 11 1 = 44 sq. yds. + $\frac{4}{9}$ + $\frac{7}{108}$ + $\frac{11}{1296}$ + $\frac{15}{15}$ = $\frac{44 \cdot 80 \cdot 53}{15 \cdot 65 \cdot 2}$ sq. yds. = $44 \cdot 517$ + sq. yds. \$2 \cdot 87\frac{1}{3} \times 44 \cdot 517 = \$127 \cdot 98 +.

(19)

916 acres 3 roods 17 per. 7 yds. = 4437591 $\frac{1}{4}$ sq. yds., and 43 acres 1 rood 2 per 17 yds. = 209407 $\frac{1}{4}$ sq. yds. 4437591 $\frac{1}{4}$ ÷ 209/ $\frac{1}{4}$ = 4437591 · 25 ÷ 207407 · 5 = 21 · 19117+.

Exercise 94-Page 233

(1)

 $\$742 \cdot 10 \times \cdot 05 = \$37 \cdot 10 \frac{1}{2}$. $\$1000 \times \cdot 11 = \110 .

(3)

 $$734 \cdot 19 \times \cdot 10 = $73 \cdot 419.$

(4)

 $$1624.50 \times .875 = 1421.4375

5)

 $$994.70 \times .125 = $124.3375.$

(6)

\$777.50 \times .0875 = \$68.03125, or \$68.031.

(7)

(8)

 $$7135.80 \times .0225 = $160.5555.$

2740 ... = 548.

(9)

(10)

 $\$7490 \times \cdot 10 = \749

 $$740 \times .045 = 33.30

 $$7490 \times \cdot 17 = $1273 \cdot 30$ $$7490 \times \cdot 27 = $2022 \cdot 30$

 $$1680 \times \cdot 025 = $42 \cdot 00$ \$42.00 - \$33.30 = \$8.70

 $$7490 \times \cdot 46 = $3445 \cdot 40$

(11)

 $729 \times \cdot 11 = 80 \cdot 19$

 $\$763 \cdot 22 \times \cdot 25 = \$190 \cdot 8050$

729—80·19 = $648 \cdot 81 = 648^{-81}_{100}$. \$847·16 × ·16 = 135·5456 $$1234 \cdot 17 \times \cdot 0625 = 77 \cdot 135625$

Sum = \$403 · 486225

(13)

(14)

 $$17429 \cdot 40 \times \cdot 43 = $7494 \cdot 64\frac{1}{5}$ $$17429 \cdot 40 \times \cdot 37 = 6448 \cdot 87$

 $68978 \times \cdot 36 = 24832 \cdot 08.$

(15)

\$78

 $\$13943 \cdot 52$ $29800 \times \cdot 17 = 5066$ $$17429 \cdot 40 - $13943 \cdot 52 = $3485 \cdot 88.$ 29800 - 5066 = 24734

Exercise 95-Page 235.

(1)

(2)

 $$1000 \times .045 = $45.$ $$1678.30 \times .0225 = $37.76175,$

(3)

 $7531 \cdot 19 \times \cdot 0375 = 282 \cdot 419625$. $508 \cdot 60 \times \cdot 0125 = 6 \cdot 3575$

(5)

(6)

\$7863·50 × ·0175=\$137·61125. \$878·30 × ·025=\$21·9575

(7)

(8)

 $7193 \cdot 16 \times \cdot 03125 = 224 \cdot 78625$. $6734 \cdot 10 \times \cdot 17 = 1144 \cdot 797$.

(9)

 $\$7.13 \times 718 \times .0425 = \$217.57195.$

(10)

 $$1.85 \times 8243 \times .05625 = $857.7871875.$

Exercise 96—Page 236.

(1)

(2)

 $$7893.87 \times .02 = $157.8774.$ $$8000 \times .00875 = $70.$

(3) $\$8643 \cdot 22 \times \cdot 0125 = \$108 \cdot 04025.$

 $$78963.80 \times \cdot 00875 = $690.93325.$

(5)

 $$1987 \cdot 27 \times \cdot 0375 = $74 \cdot 522625.$

3.031.

(8)

.. = 548.

(10)

5 = \$33.30 .

5 = \$42.00

30 = \$8.70

\$190 . 8050

135 • 5456

77-135625

\$403 - 486225

4)

 $= 24832 \cdot 08.$

5) -17 = 5066

5066 = 24734

2)

37 - 76175.

Exercise 97-Page 237.

(1)

 $$4000 \div 1.0125 = $3950.61728 + = sum to be invested.$ \$4000 - 3950.61728 = \$49.38271 = commission.

(2)

 $$7500 \div 1.045 = $7177.03349 = \text{sum to be expended in laces.}$ \$7500 - \$7177.03349 = \$322.96651 = commission.

(3)

\$8470 \div 1.05 = \$8066.66\(^2_3\) = sum to be invested. \$8066.66\(^3_3\) \div \$6.40 = 1260\(^4_3\) barrels.

(4)

 $$11000 \div 1.00875 = $10904.584882 = \text{sum to be invested.}$

(5)

 $$13000 \div 1.045 = $12440 \cdot 1913 + = \text{sum to be invested.}$ $$13000 - $12440 \cdot 1913 = $559 \cdot 8086 + = \text{commission.}$ $$12440 \cdot 1913 + \div $3 \cdot 63 = 3427 \cdot 0499 \text{ yds.}$

Exercise 98-Page 238.

(1)

\$9000 \div 0.83 = \$10843.373. \$8500 \div 1.11 = \$7657.6576.

(3)

 $$17500 \div 1.0125 = $17283.951 =$ amount to be invested. $$17283.951 \div 1.07 = $16153.22 =$ stock.

(4)

\$20000 \div 1.0175 = \$19656.01965 = amount to be invested. \$19656.01965 \div 0.97 = \$20263.937 = stock remitted.

(5)

 $$200 \times 100 = $20000 = \text{par value of 200 shares.}$

\$1 stock costs \$1.055. $$1.055 \times 20000 = $21100 = \text{cost of stock}$.

\$21100 $\times \cdot 00875 = \$184 \cdot 625 = \text{brokerage.}$ \$21100 + \$184 \cdot 625 = \$21284 \cdot 625 = whole cost.

Exercise 99-Page 240.

(1)

 $$7500 \times \cdot 0175 = $131 \cdot 25.$ $$8375 \times \cdot 0075 = $62 \cdot 8125.$

(2)

(3)

 $\$6000 \times \cdot 01875 = \112.50 $\$5000 \times \cdot 0117 = \$58 \cdot 50.$

(5)

(7)

\$36000 $\times \cdot 03 = 1080 . \$27000 $\times \cdot 0482 \times 4 = $5205 \cdot 60$.

(9)

\$39000 $\times \cdot 022 = 858 . \$17800 $\times \cdot 005 = 89 .

(11)

 $$12350 \times \cdot 013 \times 7 = $1235.$

be invested.

ended in laces. sion.

invested.

be invested.

e invested. nission.

\$7657·6576.

invested.

Exercise 100-Page 241.

(1)

(2)

 $$17000 \div 965 = $17616.58.$ $$22750 \div .94 = $24202.127.$

(3)

(4)

\$15000÷·9775=\$15345·2685. \$33000 ÷·9425=\$35013·2625.

Exercise 101-Page 243.

 $1347 \times 5 = 6735$ lbs. = gross weight. $6735 \times -06 = 404 \cdot 1$ lbs. tare.

> 6330 · 9 lbs. = net at 31 cents per 11 = 6330 · 9 $\times \cdot 035 = $221.58.$

> > (2)

 $127 \times 11 = 1397$ lbs. = gross weight. $1397 \times \cdot 03 = 41.91 \text{ lbs.} = \text{tare.}$

> 1355.09 lbs. = net at \$.012 per lb. = 1355.09 $\times \cdot 012 = \$16 \cdot 26.$

> > (3)

.29 × ·13 = \$16.77.

(4)

 $31 \times 207 = 6417$ lbs. = gross weight. 207 × 21 = 4651 lbs. = tare.

> 59511 lbs. = net at 52 cents per lb. = 59511 × $.0575 = $342 \cdot 1968.$

(2)

(4)

 $214 \times \cdot 47 = $100.58.$

(5)

= \$24202 · 127.

Exercise 102-Page 243.

5=\$35013·2625.

(1)

 $$17429.80 \times .21 = $3660.2580. $2920.16 \times .075 = $219.012.$

 $\$71342 \cdot 90 \times \cdot 25 = \$17835 \cdot 725.$ $\$913 \cdot 73 \times \cdot 2 = \$182 \cdot 746.$

(5)

 $$14713 \cdot 19 \times \cdot 33 = $4855 \cdot 3527.$

11 = 6330.9

Exercise 103-Page 244.

(1)

\$23900 \div 7142300 = \$0.0033462 = rate per dollar. $\$ \cdot 0033462 \times 14729 \cdot 50 = \$49 \cdot 2878 + .$

(2)

\$100000 \div 5793000 = \$.017262 = rate per dollar. $\$ \cdot 017262 \times 18600 = \$321 \cdot 0732.$

(3)

\$100000 ÷ 5793000 = \$.017262 = rate per dollar. $\$ \cdot 017262 \times 7500 = \$129 \cdot 465.$

(4)

\$100000 ÷ 5793000 = \$.017262 = rate per dollar. $\$ \cdot 017262 \times 11400 = \$196 \cdot 7868.$

 $b = -1355 \cdot 09$

= 59511 ×

B

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Exercise 104-Page 252.

(1)

Here $P = $723 \cdot 19$, $r = \cdot 067$, and $t = 7 \cdot 32$. Then $L = Prt = 723 \cdot 19 \times \cdot 067 \times 7 \cdot 32 = $354 \cdot 6813036$.

(2)

Here $P = 857 \cdot 19$, $r = \cdot 065$, and t = 61 or $6 \cdot 5$. Then $A = P(1 + rt) = $857 \cdot 19 \times 1.4225 = 1219.352775 .

(3)

Here t = 11, and r = .725. Then $n = tr + 1 = 11 \times .725 + 1 = 8.975$.

(4)

Here $P = \$654 \cdot 32$, $I = \$234 \cdot 56$, and $r = \cdot 07$. Then $t = \frac{I}{Pr} = \frac{234 \cdot 56}{654 \cdot 32 \times \cdot 07} = 5 \cdot 12112$ or 5 years 1 m. 13 d.

(5)

Here A = \$1200, P = \$700, and t = 5. Then $r = \frac{A-P}{Pt} = \frac{1200-700}{700 \times 5} = \frac{1}{700 \times 5} = \frac{1}{700 \times 5} = \frac{1}{700 \times 5} = \frac{1}{100 \times 5} = \frac{1$

(6)

Here n = 4, and r = .23. Then $t = \frac{n-1}{r} = \frac{4-1}{.23} = 13$ years 15 days.

(7)

Here P = \$270, I = \$87 and $r = \cdot 07$. Then $t = \frac{I}{Pr} = \frac{87}{270 \times \cdot 07} = 4$ years $7\frac{5}{21}$ months. \$354.6813036.

\$1219·352775.

years 1 m. 13 d.

er unit .. 143 =

= 8.975.

(8)

Here P=\$680, t=11, and r=11. Then $A=P(1+ri)=680 \times 2.265=1540.20

(9)

Here A=\$2000, t=20, and r=.08. A 2000 Then P = --= \$769.23 1. 1+rt 2.6

(10)

Here n = 21, and t = 24. n-1 21-1 Then r = - $- = .83\frac{1}{3} =$ rate per unit. $... 83\frac{1}{3} =$ rate per cent.

(11)

Here n = 23, and $r = \cdot 16$. 23 — 1 n-1Then t = - = --= 1371 years

(12)

Here P = \$679.18, r = .0775, and t = 11.73. Then $I = Prt = 679 \cdot 18 \times \cdot 0775 \times 11 \cdot 73 = 617.4255 .

(13)

Here P = \$950, A = \$1763.42, and t = 10. A - P = 1763.42 - 950Then r = -- = .08562 =rate per unit $Pt = 950 \times 10$... 8.562 = rate per cent.

ays.

onths.

(14)

Here P = \$666,
$$A$$
 = \$1347.50, and r = .06.
Then $t = \frac{A - P}{Pr} = \frac{1347.50 - 666}{666 \times .06} = 17.054 + \text{ years, or } 17$
years 19 days.

(15)

Here
$$P = \$273$$
, $I = \$100$, and $r = \cdot 09$
Then $t = \frac{I}{Pr} = \frac{100}{273 \times \cdot 09} = 4 \cdot 07$ years = 4 years 25 days.

(16)

Here
$$P = \$476.30$$
, $A = \$500$, and $t = 2$.
Then $r = \frac{A - P}{Pt} = \frac{500 - 476.30}{476.30 \times 2} = .0248 = \text{rate per unit.}$
 $\therefore 2\frac{12}{5} = \text{rate per cent.}$

(17)

Here
$$P = \$749.49$$
, $I = \$257$, and $t = 7$.
Then $r = \frac{I}{Pt} = \frac{257}{749.49 \times 7} = .04898 = \text{rate per unit.}$
 $\therefore 4.898 = \text{rate per cent.}$

(18)

Here
$$A = \$1111 \cdot 11$$
, $t = 11$, and $r = \cdot 11$.
Then $P = \frac{A}{1 + rt} = \frac{1111 \cdot 11}{2 \cdot 21} = \$502 \cdot 7647$.

(19)

$$P = £167.47, r = .11, \text{ and } t = 9.$$

 $I = Prt = 167.47 \times .11 \times 9 = £165.7953 = £165.158.10_{1.22}^{1.02} d.$

Exercise 105-Page 253.

1)

 $11 \div 2 = 5\frac{1}{2}$ cents. $16 \div 2 = 8$ cents = \$0.08.

(3)

9 years and 8 months = 116 months, and 116 \div 2 = 58 cents = \$0.58.

(4)

16 years and 3 months = 195 months, and $195 \div 2 = 97\frac{1}{2}$ cents = $$0.97\frac{1}{2}$.

(5)

11 years and 7 months = 139 months, and 139 \div 2 = 69½ cents = \$0.695.

(6)

12 years and 5 months = 149 months, and 149 \div 2 = 74½ cents = \$0.745.

(7)

3 years and 2 months = 38 months, and $38 \div 2 = 19$ cents = interest of \$1 for given rate and time. $$0.19 \times 279.40 = 53.086 .

(8)

6 years and 7 months = 79 months, and $79 \div 2 = 39$; cents = interest of \$1 for given rate and time. $$0.395 \times 189.70 = 74.9315 .

years, or 17

ears 25 days.

rate per unit.

ate per unit.

11. 7647.

5 15s. 10 109 d.

T

Th

(9)

3 years and 11 months =47 months, and $47 \div 2 = 23\frac{1}{2}$ cents = interest of \$1 for given rate and time. $\$0.235 \times 1463 = \343.805 .

(10)

11 years and 1 month = 133 months, and $133 \div 2 = 66\frac{1}{2}$ cents = interest of \$1 for given rate and time. \$0.665 \times 28967.50 = \$19263.3875.

Exercise 106-Page 254.

(1)

 $2 \div 6 = \frac{1}{3} \text{ mill} = \$0003.$ $7 \div 6 = \frac{1}{6} \text{ mills} = \$0.001\frac{1}{6}.$

(3)

 $11 \div 6 = 1\frac{5}{6}$ mills = \$0.001\frac{5}{6}. $27 \div 6 = 4\frac{1}{2}$ mills = \$0.004\frac{1}{2}.

(5)

 $47 \div 6 = 7\frac{5}{6}$ mills = \$0.007 $\frac{5}{6}$.

(6)

 $8 \div 2 = 4 \text{ cents} = \$0.04.$ $12 \div 6 = 2 \text{ mills} = \$0.002 \text{ and } \$0.04 + \$0.002 = \$0.042$

(7)

 $66 \div 6 = 11 \text{ mills} = \$0.011.$

(3)

2 years 2 m'ths = 26 months, and $26 \div 2 = 13$ cents = \$0.13. $19 \div 6 = 3_6^1$ mills = \$0.003 $_6^1$ and \$0.13 + \$0.003 $_6^1$ = \$0.133 $_6^1$.

 $= 23\frac{1}{2}$ cents =

= 66½ cents=

(2

 $11s = \$0.001\frac{1}{6}.$

(4)

 $lls = \$0.004\frac{1}{2}$.

= \$0.042

 $\begin{array}{l}
 \text{nts} = \$0.13. \\
 = \$0.133 \\
 \vdots
 \end{array}$

(9)

7 years 8 m'ths = 92 months, and 92 \div 2 = 46 cents = \$0.46. 9 \div 6 = $1\frac{1}{2}$ mills = \$0.001 $\frac{1}{2}$ and \$0.46 + \$0.001 $\frac{1}{2}$ = \$0.461 $\frac{1}{2}$.

(10)

17 years 11 months = 215 months, and $215 \div 2 = 107\frac{1}{2}$ cents = \$1.075. 23 ÷ 6 = $3\frac{5}{6}$ mills = $\$0.003\frac{5}{6}$, and $\$1.075 + \$0.003\frac{5}{6} = \$1.078\frac{5}{6}$.

(11)

12 years 7 months = 151 months, and $151 \div 2 = 75\frac{1}{2}$ cents = \$0.755. 17 ÷ 6 = $2\frac{5}{6}$ mills = $\$0.002\frac{5}{6}$, and $\$0.755 + \$0.002\frac{5}{6} = \$0.757\frac{5}{6}$.

Exercise 107-Page 255.

(1)

Interest on \$1 for 7 months = \$0.035 Interest on \$1 for 17 days = $2\frac{5}{6}$

Therefore interest on \$1 for 7 months 17 days, = $\$0.037_0^5$ Then $\$0.037_0^5 \times 917.30 = \34.704516 .

(2)

Interest on \$1 for 3 months
Interest on \$1 for 13 days

= \$0.015

Therefore interest on \$1 for 3 months 13 days = $\frac{$0.017_{6}^{1}}{$1.017_{6}^{1} \times 842.50} = $14.462916.$

(3)

Interest on \$1 for 2 years 11 months = \$0.175 Interest on \$1 for 10 days = 1?

Therefore interest on \$1 for 2 years 11 m'ths 10 days = $\$0.176\frac{2}{3} \times 573.83 = \101.3766 .

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(4)

Interest on \$1 for 6 years 9 months = \$0.405Interest on \$1 for 19 days = $3\frac{1}{6}$

Therefore interest on \$1 for 6 years 9 m'ths 19 days = $\$0.408\frac{1}{6}$ Then $\$0.408\frac{1}{6} \times 642.30 = \262.16545 .

(5)

Interest on \$1 for 5 years 5 months = \$0.325Interest on \$1 for 7 days = $1\frac{1}{6}$

Therefore interest on \$1 for 5 years 5 months 7 days = $\$0.326_6^1$ Then $\$0.326_6^1 \times 1427.875 = \465.7252 .

(6)

Interest on \$1 for 4 years 7 months = \$0.275 Interest on \$1 for 16 days = 23

Therefore interest on \$1 for 4 years 7 m'ths 16 days = $$0.277_3^2$$ Then $$0.277_3^2 \times 709.63 = 197.040596$.

(7)

Interest on \$1 for 7 years 7 months = \$0.455Interest on \$1 for 22 days = 3°_{3}

Therefore interest on \$1 for 7 years 7 m'ths 22 days = $$0.458\frac{2}{3}$$ Then $$0.458\frac{2}{3} \times 2463.20 = $1129.7877 + $2463.20 = 3592.9877 .

(8)

Interest on \$1 for 9 years 9 months = \$0.585 Interest on \$1 for 9 days = 1;

Therefore interest on \$1 for 9 years 9 months 9 days = $$0.586\frac{1}{2}$$ Then $$0.586\frac{1}{2}$ × 999.99 = $586.494135.$ = \$0·405

 $78 = \$0.408\frac{1}{6}$

3½

(9)

Interest on \$1 for 3 years 4 months = \$0.20 Interest on \$1 for 27 days = 41

Therefore interest on \$1 for 3 years 4 m'ths 27 days = $$0.204\frac{1}{2}$ Then $$0.2045 \times 68.70 = 14.04915 .

(10)

Interest on \$1 for 3 years = \$0.18 Interest on \$1 for 28 days = 4

Therefore interest on \$1 for 3 years 28 days = \$0.184 Then \$0.184 \$0.

(11)

Interest on \$1 for 7 years 4 months = \$0.44 Interest on \$1 for 11 days = 15

Therefore interest on \$1 for 7 years 4 m'ths 11 days = $$0.441_6^5$ X 200 = \$88.366 + \$200 = \$288.366.

(12)

Interest on \$1 for 9 years 3 months = \$0.555 Interest on \$1 for 9 days = 11

Therefore interest on \$1 for 9 years 3 months 9 days = $$0.556'_{5}$ Then $$0.5565 \times 743.63 = $413.830095 + $743.63 = 1157.460095 .

Exercise 108-Page 256.

(1)

Interest on \$1 at 6 per cent. for given time = $$0.526\frac{2}{3}$. Interest on \$1234.56 at 6 per cent. for given time = $$0.526\frac{2}{3} \times 1234.56 = 650.2016 .

Hence interest on \$1234.56 at 7 per cent. for given time= \$650.2016 + one sixth of \$650.2016 = \$758.5685.

= \$0.325 $= 1\frac{1}{6}$

 $rs = \frac{1}{\$0.326_6^1}$

= \$0.275 $= 2\frac{3}{3}$

 $5 = 50.277_3^2$

= \$0.455 $= 3\frac{3}{3}$

= \$0.458\frac{2}{3}\$ = \$3592.9877.

= \$0.585 = 11

\$0.586

5.

(2)

Interest on \$1 at 6 per cent. for given time = \$0.126%. Interest on \$9876.54 at 6 per cent. for given time = \$0.126% × 9876.54 = \$1252.67449

Hence interest on \$9876.54 at 3 per cent. for given time = \$1252.67449: 2 = \$626.337245.

(3)

Interest on \$1 at 6 per cent. for given time= $$0.216\frac{2}{3}$. Interest on \$715.30 at 6 per cent. for given time = $$0.216\frac{2}{3} \times 715.30 = 154.98166 .

Hence interest on \$715.30 at 8 per cent. for given time= \$154.98166 + one third of \$154.98166 = \$206.6422.

(4)

Interest on \$1 at 6 per cent. for given time=\$0.141\frac{1}{3}.

Interest on \$555.55 at 6 per cent. for given time = $$0.141\frac{1}{3} \times 555.55 = 78.51773 .

Hence interest on \$555.55 at 12 per cent. for given time = \$78.51773×2=\$157.03546; amount=\$157.03546 + \$555.55=\$712.58546:

(5)

Interest on \$1 at 6 per cent. for given time= $$0.016_3^2$. Interest on \$7766.55 at 6 per cent. for given time = $$0.016_3^2 \times 7766.55 = 129.4425 .

Hence interest on \$7766.55 at 5 per cent. for given time = \$129.4425 — one sixth of \$129.4425 = \$107.86875. Amount =\$107.86875 + \$7766.55 = \$7874.41875.

(6)

Interest on \$1 at 6 per cent. for given time = $$0.521\frac{1}{3}$. Interest on \$500 at 6 per cent. for given time = $$0.521\frac{1}{3} \times 500$ = $$260.666\frac{3}{3}$.

Hence interest on \$500 at 16 per cent. for given time = $$260.666\frac{3}{3} \times 2\frac{3}{3} = 695.111 ; amount = \$695.111 + \$500 = \$1195.111.

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Interest on \$1 at 6 per cent. for given time = \$0.2061. Interest on \$576 at 6 per cent, for given time = \$0.206\(\times \) 576

= \$118.752.

Hence interest on \$576 at 5 per cent, for given time = \$118.752 —one sixth of \$118.752 = \$98.96.

(8)

Interest on \$1 at 6 per cent. for given time = \$0.1516.

Interest on \$2478.91 at 6 per cent, for given time = \$0.1516 × 2478.91 = \$376.38116.

Hence interest on \$2478.91 at 4\} per cent. for given time = \$376.38116 - one fourth of \$376.38116 = \$282.285.

(9)

From May 9th to December 11th = 216 days. Interest on \$1 at 6 per cent. for 216 days = \$0.036.

Interest on \$780 at 6 per cent. for 216 days = $$0.036 \times 780 =$ \$28.08.

(10)

From August 16th 1851 to June 19th 1852 = 308 days.

Interest on \$1 at 6 per cent. for given time = \$0.051.

Interest on \$1830.63 at 6 per cent. for given time = \$0.0511 × 1830.63 = \$93.97234.

Hence interest on \$1830.63 at 7 per cent. for given time = \$93.97234 + one sixth of \$93.97234 = \$109.63439.

(11)

From September 3rd 1858 to January 9th 1859 = 128 days. Interest on \$1 at 6 per cent. for given time = \$0.021. Interest on \$6200 at 6 per cent. for given time = $$0.021\frac{1}{3} \times 6200$ **=** \$132.266.

Amount = \$132.266 + \$6200 = \$6332.266.

= \$0.1265 x

tiven time =

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265.

32. = \$0.216% ×

given time= 422.

ļ. = \$0·1411 ×

iven time = +\$555.55=

\$0.0163 × ven time =

5. 75.

 $521\frac{1}{3} \times 500$

en time == 11+\$500=

Exercise 109 .- Page 258.

(1)

F	ron	June	2nd to	July	1.7th	there are	45	days
•	"	July .	17th to	October	6th	**	81	· ii
	"	October	6th to	December	11th	"	66	44
	"	December	11th to	March	29th	"	109	"
	"	March	29th to	October	7th	"	192	66

Whole sum \$1217.30 for 45 days = \$54778.50 for 1 day. 1st endorsement 207.80

Balance \$1009.50 for 81 days = \$81769.50 for 1 day. 2nd endorsement 209.60

Balance \$799.90 for 66 days = \$52793.40 for 1 day. 3rd endorsement 320.90

Balance \$479.00 for 109 days = \$52211.00 for 1 day.
4th endorsement 421.83

Balance \$57.17 for 192 days = \$10976.64 for 1 day.

Whole interest = that of \$252529.04 for 1 day.

Interest on \$252529.04 at 6 per cent. for 1 year = \$15151.7424. Hence interest for 1 day = $$15151.7424 \div 365 = 41.5116 .

Then interest due = \$41.5116
Balance on Note = \$57.17

Principal and interest due = \$98.6816

EXE

F

1st e

2nd

3rd e

4th e

5th e

Inter

50 for 1 day.

50 for 1 day.

10 for 1 day.

00 for 1 day.

64 for 1 day.

4 for 1 day.

\$15151.7424

= \$41.5116.

16

16

(2)

From	17th Ju	ne	to	5th	Septen	nber	there	are !	80 d	lays.
66		ptember							93	11 /
46		cember					"	1	86	**
"		ine				arv	"	2	41	"
"		bruary							15	"
"		ecember					u		33	"
Wh	ole sum	\$7348-2	5 for	80	davs :	= \$ 5	87860	0.00	for	1 day.
		2463.8			•					
Bala	ance	\$4884.4	- 5 for	93	days	= \$4	15425	3.85	for	1 day
		t 392·2								
Bal	ance	\$4492.2	5 for	186	days	= \$ 8	35558	3.50	for	1 day.
3rd endo	orsemen	t 982·20	0							
		\$3510.0		241	days	= \$8	34592	2.05	for	1 day.
4th endo	orsemen	t 2842·90)							
Bala	ance	\$667.1	5 for	318	days	=\$2	210152	2.25	for	1 day.
5th endo	rsemen	317·2	3	,						
Bala	ance	\$349.9	2 for	133	days :	= \$	346539	9.36	for	1 day.

Whole interest = that of \$2980286.01 for 1 day.

Interest on \$2980286.01 at 8 per cent. for 1 year = \$238422.8808. Hence interest for 1 day = \$238422.8808 \div 365 = \$653.2133.

Then interest due = \$653.2133

Balance on Note = \$349.92

Principal and interest due = \$1003.1333

EXE

\$673

\$693 20

\$714 21

\$735 22

\$757 22 \$780 23

\$804 \$828 24' \$853 673-\$179

\$860 34. \$894. 35. \$930. 37. \$967. 38.6 \$1046. 41 \$1088. 860. \$22

Exercise 110.—Page 259.

1	
\$1800	Principal (1
108	Principal. Interest for 1st year.
	•
\$1908 114:48	Amount for 1 year = principal for 2nd year.
114.48	Interest for 2nd year.
\$2022.48	Amount for 2 years = principal for 3rd year.
121.3488	Interest for 3rd year.
\$2143.8288	Amount for 3 years = principal for 4th year.
128-629728	
\$2272.458528	Amount for 4 years = principal for 5th year.
136-347511	Interest for 5th year.
\$2408.806039	Amount for 5 years.
1800	Given Principal.
\$608.806 =	Compound interest required.
\$700	Principal. (2)
49	Interest for 1st half year.
\$749	
52.43	Amount for 1 half y. = principal for 2nd half y. Interest for 2nd half year.
\$801.43	Amount for 1 year - principal for 2nd half-
56.1001	Amount for 1 year = principal for 3rd half y. Interest for 3rd half year.
\$857.5301	Amount for 1 vears = principal for 4th half
60.027107	Interest for 4th half year.
\$917.557207	Amount for 2 years = principal for 5th half v
64.229004	Interest for 5th half year.
\$981.786211	Amount for 21 years = principal for 6th bals -
68.725034	Interest for 6th half year.
\$1050.511245	Amount for 3 years = principal for 7th half y
73 • 535 787	Interest for 7th half year.
\$1124.047032	Amount for 3½ years
700	Given Principal.
\$424.047 =	Compound interest required.
	ompount interest required.

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EXERCISE 110.1

KEY.

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	\$673.40 Principal. 20.202 Interest for 1st quarter.
or 2nd year.	\$693.602 Amount for 1 quar. = principal for 2nd quarter. 20.80806 Interest for 2nd quarter.
for 3rd year.	\$714.41006 Amount for 1 half y. = principal for 3rd quart. 21.4323018 Interest for 3rd quarter.
for 4to year.	\$735.8423618 Amount for 3 quarters = principal for 4th quar. 22.0752708 Interest for 4th quarter.
for 5th year.	\$757.9176326 Amount for 1 year = principal for 5th quarter. 22.7375289 Interest for 5th quarter.
ioi om year.	\$780.6551615 Amount for 5 quarters = principal for 6th quar. 23.4196548 Interest for 6th quarter.
•	\$804.0748163 Amount for 3 half y. = principal for 7th quarter. 24.1222444 Interest for 7th quarter.
	\$828-1970607 Amount for 7 quarters = principal for 8th qr. 24-8459118 Interest for 8th quarter.
for 2nd half y.	\$853.0429 = Amount for 2 years required. Given Principal.
	\$179.6429 = Compound Interest required.
r 3rd half y.	\$860 Principal. (4)
for 4th half y	34.4 Interest for 1st half year. \$894.4 Amount for 1 half year = principal for 2nd half y. Interest for 2nd half year.
or 5th half v	\$930·176 Amount for 1 year = principal for 3rd half year. 37·20704 Interest for 3rd half year.
for 6th half y.	\$967.38304 Amount for 3 half years = principal for 4th half y. 38.69532 Interest for 4th half year.
for 7th half y	\$1006.07836 Amount for 2 years = principal for 5th half year. 40.24313 Interest for 5th half year.

\$1088·17434 = Amount for 3 years required.

860 Given Principal.

\$1046.32149 Amount for 5 half years = principal for 6th half y. 41.85285 Interest for 6th half year.

\$228.1743 = Compound Interest required.

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Exercise 111-Page 261.

(1)

By the table the am't of \$1 at 6 per cent. for 11 years = \$1.8983. Then $$1.8983 \times 875 = $1661.0125 = Amount.$

875 Principal.

\$786.0125 = Interest.

(2)

By the table the am't of \$1 for the given time and rate = \$2.77247. Then $$2.77247 \times 643.98 = $1785.41523 = Amount.$

643.98 Principal.

\$1141.43523 = Interest.

(3)

By the table the am't of \$1 at 6 per cent. for 45 years=\$13.76461. Then $$13.76461 \times .01 = $.137646 = Amount$.

·01 Principal.

\$.127646 = Interest.

(4)

By the table the am't of \$1 for the given time and rate = \$2.28793. Then \$2.28793 \times 78.2 = \$178.916 = Amount.

78 2 Principal.

\$100.716 = Interest.

(5)

By the table the am't of \$1 for the given rate and time=\$2.40662Then $$2.40662 \times 777.77 = $1871.7968 = Amount.$

777.77 Principal.

\$1094.0268 = Interest.

(6)

£44 5s. 9d. = £44.2875,

By the table the am't of £1 at 6 per cent. for 11 years = £1.8983. Then £1.8983 \times 44.2875 = £84.07096 = £84 1 5 = Amount.

44 5 9 Principal.

£39 15 8 = Interest.

(7)

£32 4st 94d. = £32.240625.

By the table the amount of £1 for the given time and rate = £1.26532. Then £1.26532 \times 32.240625 =

£40.7947076 = £40 15 $10\frac{3}{4}$ nearly = Amount.

32 4 94 Principal.

£8 11 1 = Interest.

Exercise 112-Page 262.

1 (1)

Amount of \$1 for 7 years at 4 per cent. = \$1.31593. \$7439.87 \div 1.31593 = \$5653.697.

(2)

Amount of \$1 at 5 per cent. for 20 years = \$2.6533. $$9193.90 \div 2.6533 = 3465.081 .

(3)

£595 10s. 2_5^2 d. = £595·51

Amount of £1 at 6 per cent. for 3 years = £1·19102. £595·51 \div 1·19102 = £500.

(4)

Amount of \$1 at 6 per cent. for 7 years = \$1.50363. $$7111.11 \div 1.50363 = 4729.295 .

rears = \$1.8983. ant. sipal.

est.

rate=\$2.77247.
Amount.
Principal.

= Interest.

ount. . cipal.

erest.

rate=\$2.28793

nt. ipal.

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ime=\$2·40662 mount.

rincipal.

nterest.

(5)

£268 0s. $4\frac{1}{6}d$. = £268·02. Amount of £1 at 5 per cent for 6 years = £1·3401. £268·02 $\stackrel{?}{=}$ 1·3401 = £200.

Exercise 113-Page 263.

(1)

Here A = \$962, r = .04, and t = 1. Whence 1 + rt = 1.04.

Then $P = \frac{A}{1 + rt} = \frac{.962}{1.04} = 925 .

(2)

Here A = \$2202, r = .06, and t = 5.75. Whence 1 + rt = 1.345.

Then $P = \frac{A}{1+rt} = \frac{2202}{1\cdot 345} = \$1637\cdot 174.$

(3)

Here A = \$1003.50, r = .06, and $t = \frac{2}{3}$ year. Whence 1 + rt = 1.04.

Then $P = \frac{A}{1+rt} = \frac{1003.50}{1.04} = $964.9038.$

(4) by the transition

Here A = \$716, r = .08, and $t = \frac{7}{4}$ year. Whence $1 + rt = \frac{1.04\frac{2}{3}}{1.04\frac{2}{3}}$.

Then $P = \frac{A}{1+rt} = \frac{716}{1.04\frac{9}{3}} = $684.0764.$

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\$925.

ce 1 + rt =

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hence 1 + rt

64.9038.

nce 1 + rt =

764.

(5)

Here A = \$1342.50, r = .065, and $t = \frac{11}{12}$ year. Whence 1 + $rt = 1.022\frac{19}{13}$.

A 1342.50 Then . P . = _ $\frac{1+rt}{1+rt} = \frac{1\cdot 022\frac{1}{12}}{1\cdot 022\frac{1}{12}} = $1313\cdot 266.$

(6)

Here A = \$2400, r = .05, and t = 335 year. Whence 1 + rt $= 1.03 \frac{1}{3}$.

Then P = A 2400 $\frac{1}{1+rt} = \frac{1\cdot 03\frac{17}{3}}{1\cdot 03\frac{17}{3}}$ = \$2324.84.

(7)

Here A = \$2202, r = .05, and t = .75 year. Whence 1 + rt= 1.0375.

 $$2202 \div 1.0375 = $2122.40963 + = Present worth.$ \$2202 - \$2122.40963+ = \$79.59036 = Discount.

(8)

Here A=\$4360, r=0.06, and t=1.5. Whence 1+rt=1.085

A 4360 = \$4018.43317. Then $P = \frac{A}{A}$ 1 + rt 1.085

(9)

Here A = \$1647, r = .06, and $t = \frac{11}{12}$ year. Whence 1 + rt =1.055.

1647 Then P = - $\overline{1+rt} = \overline{1.055} = $1561.13744.$

(10)

Here A=\$2000, r=06, and $t=37_f$. Whence 1+rt=1.215

A 2000 ... Then $P = \frac{1}{1+rt} = \frac{1\cdot 215}{1\cdot 215}$ - = \$1646.09053.

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(11)

Here A = \$2070.90, r = .05, and t = 1.7. Whence $1 + rt = 1.07\frac{1}{12}$.

Then
$$P = \frac{A}{1+rt} = \frac{2070.90}{1.07\frac{1}{12}} = $1918.9806.$$

\$2070 - \$1918.9806 = \$151.019 = Discount required.

(12)

Here A = \$970.63, r = .08, and $t = \frac{1}{12}$ year. Whence $1 + rt = 1.07\frac{1}{3}$.

Then
$$P = \frac{A}{1+rt} = \frac{970.63}{1.07\frac{1}{3}} = $904.313.$$

(13)

Here in first case A = \$1512, r = .07, and t = .5 year. Whence 1 + rt = 1.035.

Then
$$P = \frac{A}{1+rt} = \frac{1512}{1\cdot 035} = $1460\cdot 8695.$$

Also A = 1512, r = .07, and t = 1. Whence 1 + rt = 1.07.

Then
$$P = \frac{A}{1+rt} = \frac{1512}{1\cdot 07} = $1413\cdot 0841.$$

\$1460.8695 + \$1413.0841 = \$2873.9536 = Present worth of whole amount.

\$3024 - \$2873.9536 = \$150.0464 = Discount required.(14)

Here in first case A = \$440, r = .08, and t = 1.25. Whence 1 + rt = 1.1.

Then
$$P = \frac{A}{1+rt} = \frac{440}{1\cdot 1} = $400$$

In second case A = \$896, r = .08, and t = 1.5. Whence 1 + rt = 1.12.

Then
$$P = \frac{A}{1+rt} = \frac{896}{1\cdot 12} = $800.$$

\$400 + \$800 = \$1200.

Exercise 114-Page 265.

(1)

Here the time the note has to run is 2 years 3 months 3 days. Interest of \$1 at 7 per cent. for 2 yrs., 3 m., 3-days = \$0.1580 \frac{5}{6}. Interest of \$986 at 7 per cent. for 2 years, 3 months, 3 days = \$0.1580 \frac{5}{6} \times 986 = \$155.8701.

(2)

(3)

Here the time the note has to run is 94 days = 3 months 4 days. Interest of \$1 at 6 per cent. for 3 months 4 days = $$0.015\frac{3}{3}$. Interest of \$563.80 at 6 per cent. for 3 months 4 days = $$0.015\frac{3}{3} \times 563.80$ =\$8.8328 and \$563.80—\$8.8328=\$554.967.

Exercise 115-Page 266.

(1)

Interest on \$1 for 93 days at 7 p. c. = \$0.0180\,\frac{2}{5}\$, and this taken from \$1 gives a remainder of \$0.9819\,\frac{1}{6} = present worth of \$1.

Then \$3755 \div 0.9819\,\frac{1}{6} = \$3824.15.

(2)

Interest on \$1 for 6 months 3 days at 5 per cent. = \$0:0254\footnote{1.5} and this taken from \$1 gives a remainder \$0.0745\footnote{1.5} = present worth of \$1.

Then \$1147.80 + 0.9745 = \$1177.734.

Thence 1 + rt =

51918 **-9**806.

unt required.

Whence 1 + rt

\$904.313.

5 year. Whence

1460 . 8695.

 $1+rt=1\cdot07,$

13.0841.

resent worth of

unt required.

1.25. Whence

5. Whence 1+

0.

Mario

(8)

Interest on \$1 for 48 days at 3½ per cent. = \$0.004¾, and this taken from \$1 gives a remainder \$0.9953½ = present worth of \$1.

Then \$713.90 \div 0.995 $\frac{1}{3}$ = \$717.2471.

Exercise 116-Page 268.

(1)	(2)
\$200 × 3 = 600	$\frac{1}{4}\times 0=0$
$150 \times 4 = 600$	1 × 3 = 1
250 × 6 = 1500	$\frac{1}{4} \times 6 = 1\frac{1}{4}$
600 600)2700(4½ months. 2400	$\frac{1}{1} \times 9 = \frac{21}{1}$
$\frac{300}{600}$ } = 1	41 months.

(3)	(4)
• •	

 $$50 \times 2 = 100$

$40 \times 5 = 200$	$1500 \times 1 = 1500$
30 × 7 = 210	$600 \times 3 = 1800$
A STATE OF S	$700 \times 5 = 3500$
120 120)510(44 months.	$1400 \times 7 = 9800$
480	5200 5200) 16600(3,5 months.
80) - ÎN PUNÎT	D 346 mont & " 15600
120} = 1 722	$\frac{1000}{5200}$ = $\frac{3}{6}$

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\$1000 × 0 =

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0 0(35 months.

Six months from 15th January = 15th July, and from 1st July to 15th July there are 14 days.

Six months from 10th February = 10th August, and from 1st July to 10th August there are 40 days.

Six months from 6th March = 6th September, and from 1st July to 6th September there are 67 days.

Six months from 8th June = 8th December, and from 1st July to 8th December there are 160 days.

Therefore the note must be made payable on the 61st day from the 1st of July, which is the 31st of August.

Exercise 117.—Page 269.

(1)

Whole stock : A's stock :: whole profit : A's profit. 1117×3000 That is, \$4300:\$3000::\$1117: --=\$779.302+=A's sh. 4300 \$1117 - \$779.302 + = \$337.697 = B's share,

(2)

Whole stock = \$6470 + \$3780 + \$9860 = \$20110. Whole stock : A's stock :: whole profit : A's profit.

 7890×6470

20110

Again, whole stock: B's stock: whole profit: B's profit. 7890×3780

That is,\$20110:\$3780::\$7890:———\$1483:053+=B's sh.

Lastly, whole stock: C's stock:: whole profit: C's profit. 7890×9860

That is,\$20110:\$9860::\$7890: _____\$3868.493+=C's sh.

(3)

Whole stock : B's stock :: whole gain : B's gain.

 80×120

That is, \$320 : \$120 :: \$80 : ____ = \$30 = B's gain.

Again, whole stock : C's stock :: whole gain : C's gain.

80 × 200

That is, \$320: \$200: \$80: ——— = \$50 = C's share.

(4)

20 hole stock : B's stock :: whole gain : B's gain.

 728×1200

That is, \$2800 : \$1200 :: \$728 : ____ = \$312 = B's gain.

Again, whole stock: C's stock: whole gain: C's gain.

728 × 1600

That is, \$2800; \$1600:: \$728; ____ = \$416 = C's gain.

Who

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900

900

\$1800

.

\$180

\$44.

0110. profit.

3+=A's sh.

3's profit.

3+=B's sh.

O's profit.

3+=C's sh.

gain.

= B's gain.

O's gain.

O's share.

gain.

= B's gain.

O's gain.

= C's gain,

(5)

Whole stock : B's stock :: whole amount to be divided : B's share

100×2 That is, \$3 : \$2 :: \$100 :- $-=$66.66\frac{2}{3}=B's share.$

Again, whole st'k: C's st'k:: whole amo't to be divided: C's sh'e 100 X 1

That is, \$3: \$1 :: \$100 : ___ $-=$33.33\frac{1}{3}=$ C's share.

(6)

 1100×500 £1400 : £500 :: £1100 :-=£392 $\stackrel{\circ}{=}$ B's share. 1400 £1100 — £392 $\frac{9}{7}$ = £707 $\frac{1}{7}$ = O's share.

casks. casks. 180 × 200

900 : 200 :: 180 : ---= 40 casks = B's loss.

180 × 300

900:300 :: 180:--= 60 casks = C's loss.

180 - (40 + 60) = 80 casks = D's loss.

(8

100×800 \$1800: \$800 :: \$100 :---= \$44.44 $\frac{1}{2}$ = B's snare.

1800

100×600 \$1800:\$600 :: \$100:----=\$33.33 = 0's share.1800

 $$44.44\frac{4}{9} + $33.33\frac{1}{9} = $77.77\frac{7}{9}$, and $$100 - $77.77\frac{7}{9} =$ \$22.223 = D's share.

\$35°

154

£

£350

£350

(9)

6:1:: 120:
$$\frac{120 \times 1}{6} = 20$$
6:2:: 120: $\frac{120 \times 2}{6} = 40$
6:3:: 120: $\frac{120 \times 3}{6} = 60$
(10)

Whole loss = \$900 - \$540 = \$360.
8:1:: \$360:
$$\frac{360}{8}$$
 = \$45 = B's loss.
8³: 2:: \$360: $\frac{360 \times 2}{8}$ = \$90 = C's loss.

8 \$45+90 = \$135, and \$360-135 = \$225 = D's loss.

(11)

\$12: \$6:: \$1320:
$$\frac{1320 \times 6}{12}$$
 = \$660 = B's gain.
\$12: \$4:: \$1320: $\frac{1320 \times 4}{12}$ = \$440 = C's gain.
\$12: \$2:: \$1320: $\frac{12}{12}$ = \$220 = D's gain.
(12)

. "75 + £29 = £64, and £110—£64 = £46 = D's profit. D's profit : B's profit :: D's stock : B's stock.

That is, £46: £35:: £1090: $\frac{1090 \times 35}{46}$ = £829 6s. $11\frac{1}{23}$ d = B's st.

Again, D's profit : C's profit :: D's stock : C's stock.

1090 × 29

That is, £46: £29: £1090: $\frac{1000 \times 20}{46}$ = £687 3s. 5\frac{1}{3}d. = C's st.

Exercise 118.—Page 271.

(1)

 $5257 \times 6 = 1785$ for one month = 6076 for one month. $154 \times 11 = 1694$ for one month) 347.20×1785 \$6076 : \$1785 :: \$347.20 : ____ 6076 347.20×2597 \$6076 : \$2597 :: \$347.20 : ----- = \$148.40.6076 1 1 Marketin & Str. 347.20 × 1694 \$6076 : \$1694 :: \$347.20 : ____ = \$96.80 6076 (2) $40 \times 6 = 240$ for one month $30 \times 5 = 150$ for one month $50 \times 1 = 50$ for one month = 440 for one month. 160×240 440 : 240 :: \$160 : == \$87.27131; B's share. 440 160×150 440: 150:: \$160: $\frac{}{440}$ = \$54.54 $_{11}^{6}$; C's share. 160 × 50 440: 50:: \$160: -== \$18.1812; D's share. (3) $\pounds 150 \times 6 = \pounds 900$ for one month $200 \times 3 = 600$ for one month $125 \times 16 = 2000$ for one month $25 \times 16 = 2000$ for one month £291 13s. 4d. ×900 £3500 : £900 :: £291 13s. 4d.:---3500 £291 13s. 4d. × 600 £3500; £600; £291 13s, 4d.: _______£50.

£3500 ; £2000 ;; £291 13s. 4d.:-

3500 alt : Atm Writes

=£166 13s. 4d.

£291 13s. 4d. × 2000

3500

loss. D's loss.

gain.

s gain.

s gain.

)'s profit.

 $1_{23}^{1}d = B's st.$

stock.

 $\frac{1}{3}$ d. = C's st.

(4)

 $\$4000 \times 12 = \48000 for one month $3000 \times 15 = 45000$ for one month $5000 \times 8 = 40000$ for one month = \$133000 for one month

\$133000 : \$48000 :: \$665 : $\frac{665 \times 48000}{133000}$ = \$240; B's share.

665×45000

\$133000 : \$45000 :: \$665 : ______ = \$225; C's shaze.

\$133000 : \$40000 :: \$665 : $\frac{665 \times 40000}{133000}$ = \$200 ; D's share.

(5)

 $56 \times 12 = 672$ for one day $64 \times 15 = 960$ for one day = 3072 for one day. $80 \times 18 = 1440$ for one day $= 320 \times 672$

3072:960::\$320:==\$100= " " 2nd "

3072:1440::\$320:————\$150= " " 3rd "

(7)

Sum of profits = 240 + 800 + 400 = \$1440.

Whole profit: A's profit:: Whole stock for 1 m.: A's st. for 1 m.

That is, 1440: 240:: 34560: ____ = 5760 = A's stock

for one month. Hence, since A's stock was in for 6 months, it will be \$5760 ÷ 6 = \$960.

(Continued on next page.)

Whole

EXBN

1440:

mon

Whole

1440:

mon

A's p B's pi C's p

Whole

133

133

133

\$0·12} \$0·09

\$0.03¹ ×

(7 Continued.)

Whole profit : B's profit :: Whole stock for 1 m. ; B's st. for 1 m.

34560×800

1440 : 800 :: 34560 : = 19200 = B's stock for one

month. And, since B's stock was in for 12 months, 19200.

Whole profit: C's profit:: whole stock for 1 m. : C's st. for 1 m.

1440: 400: 34560: $\frac{34560 \times 400}{1440}$ = \$9600 = C's stock for one

month, and hence his stock will be \$9600:15 = \$640.

(8)

A's profit was \$240 for 6 months = \$40 for 1 mouth. B's profit was \$800 for 12 months = $$66\frac{2}{3}$ for 1 month. C's profit was \$400 for 15 months = $$26\frac{2}{3}$ for 1 month.

Sum of profits for 1 month = \$133\frac{1}{3} Whole profit for 1 m.: A's profit for 1 m.:: whole stock: A's st.

133 $\frac{1}{3}$: 40 :: 3200 : $\frac{3200 \times 40}{133\frac{1}{3}}$ = \$960 = A's stock.

 $133\frac{1}{3}$: $66\frac{2}{3}$:: $3200 : \frac{3200 \times 66\frac{3}{3}}{133\frac{1}{3}} = $1600 = B's stock.$

133\frac{1}{26\frac{3}{2}}: 3200: \frac{3200 + 26\frac{3}{2}}{133\frac{1}{4}} = \$640 = C's stock.

Exercise 119-Page 275.

\$0.12 $\frac{1}{2}$ = selling price. \$1.20 = selling price \$0.09 = buying price. \$0.87 $\frac{1}{2}$ = buying price.

\$0.03\frac{1}{2} = gain per lb. \$0.03\frac{1}{2} \times 317 = \$11.095, \$0.32\frac{1}{2} \times 2138 = \$694.85,

r one month

's share.

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(3)

\$0.15×317×13=\$618.15=cost of 13 barrels at \$0.15 per 1b. \$735-618.15 = \$116.85 gain.

(4

\$3.15 \times 22 \times 17=\$1178·10 = price of 17 kegs at \$3.15 per gal. \$0.37\frac{1}{2}\times 1178·1=\$441.7875 = ad valorem duty. \$1178·10+\$441.7875+\$26.33=\$1646.2175=whole cost. \$1646.2175-\$1625 = \$21.2175 loss.

Exercise 120-Page 276.

(1)

Here for every \$1 I expend I wish to receive \$1.30, and hence the selling price will be $$3.25 \times 1.30 = $4.22\frac{1}{4}$.

Here for every \$1 I expend I wish to receive \$1.05, and hence the selling price will be $$1.05 \times 13420 = 14091 .

(3)

Here for every \$1 I expend I desire to receive \$1.15, and hence the selling price will be $$1.15 \times 11 = $0.1265 = 12\frac{1}{20}$ cents.

(4)

Here for every \$1 I expend I wish to receive \$1.23, and hence the selling price will be $$1.23 \times 15.25 = 18.75^3_4 .

(5)

Here for every \$1 I expend I am willing to receive \$0.89, and hence the selling price will be \$0.89 \times 7890 = \$7022.10.

80.15 per 1b.

1.15 per gal.

ty.

e cost.

30, and hence

05, and hence

15, and hence 213 cents.

23, and hence

ve \$0.89, and 3.10,

Exercise 121-Page 277.

(1)

Here the whole gain is \$0.871 - \$0.60 = \$0.271.

That is, \$0.60 gains \$0.271, and therefore 1 cent gains

 $f_{\text{Ag}} = \frac{1}{2}$ of a ceni.

And hence, the gain per cent = $\frac{11}{12} \times 100 = \frac{1100}{12} = 45\frac{5}{5}$ per cent.

(2)

Here the loss on each lb. is 2 cents.

That is, every 13 cents invested gives a loss of 2 cents.

Therefore every cent invested loses $\frac{1}{13}$ of $2 = \frac{9}{13}$ cents.

And hence, the loss per cent = $\frac{2}{13} \times 100 = \frac{200}{13} = 15\frac{5}{13}$ per c.

(8)

Here the gain on each barrel is \$1.60.

That is, every \$6.20 invested gives a gain of \$1.60.

Therefore every \$1 invested gains $\frac{1}{620}$ of $160 = \frac{8}{31}$ of a \$.

And hence, the gain per cent = $\frac{8}{31} \times \frac{100}{1} = 25.8 = 251$ p. c.

(4)

Here the gain on each yard is 35 cents.

That is, every \$2.75 invested gives a gain of 35 cents.

Therefore every \$1 invested gains $\frac{1}{275}$ of $35 = \frac{35}{275} \pm \frac{7}{55}$ of a dollar.

And hence the gain per cent = $\frac{7}{68} \times 100 = \frac{700}{68} = 12\frac{8}{10}$ p. c.

(5)

Here the gain on every bushel is 9 cents.

That is, every 47 cents invested gives a gain of 9 cents.

Therefore every cent invested gains $\frac{1}{47}$ of $9 = \frac{9}{47}$ cents.

And hence the gain per cent $=\frac{9}{47} \times 100 = \frac{900}{47} = 19\frac{7}{47}$ p. c.

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(6)

Here the loss on each lb. is $1\frac{1}{2}$ cents.

That is every 12 cents invested gives a loss of $1\frac{1}{2}$ cents.

Therefore every cent invested loses $\frac{1}{12}$ of $1\frac{1}{2} = \frac{1}{3}$ of a cent.

And hence, the loss per cent $= \frac{1}{4} \times 100 = \frac{100}{30} = 12\frac{1}{2}$ p. c.

(7)

Here the whole gain is \$127 — \$93 \pm \$34. That is, \$93 gain \$34, and therefore \$1 gains $\frac{34}{3}$ of a dollar. Hence, gain per cent = $\frac{334}{3} \times 100 = \frac{3400}{3} = 36\frac{53}{2}$ per cent.

(8)

Here the loss is $$6742 \cdot 50 - $6000 = $742 \cdot 50$.

That is, \$6742.50 loses \$742.50, and therefore \$1 loses $\frac{39}{674260}$ of $742.50 = \frac{39}{899}$ of a dollar.

Hence loss per cent = $\$\frac{99}{8999} \times 100 = \frac{99000}{8999} = 11\frac{11}{8999}$ per cent.

(9)

Here \$5700 + \$275 + \$1987.32 = \$7962.32 =whole sum expended.

Whole gain = $$8750 - $7962 \cdot 32 = $787 \cdot 66$.

That is, \$7962.32 gains \$787.68, and therefore \$1 gains $\frac{9846}{796232}$ of 787.68 = $\frac{9846}{99625}$ of a \$.

Hence gain per cent = $\frac{9846}{99529} \times 100 = \frac{984600}{99529} = 9.89$ or nearly 10 per cent.

(10)

 $\$4 \cdot 25 \times 723 = \$3072 \cdot 75 = \text{price of 723 yds. } 34 \cdot 25.$ $\$3072 \cdot 75 \times \cdot 07 = \$215 \cdot 0925 = \text{amount for Insurance.}$

 $$3072.75 \times .22 = $676.005 =$ amount for ad valorem duty.

Then whole cost = $$3072 \cdot 75 + $215 \cdot 0925 + $23 \cdot 70 + $2 \cdot 70 + $3 \cdot 16 + $676 \cdot 005 = $3993 \cdot 4075$.

Whole gain $= $5270 - $3993 \cdot 4075 = $1276 \cdot 5925$.

That is, \$8993 · 4075 gains \$1276 · 5925 . . \$1 gains 39934075 of \$1276 · 5925 = 41042 gains 39934075

Hence gain per cent = $\$_{1097363}^{510637} \times 100 = 81.96749$ or nearly \$2 per cent.

A Bloriage

Exercise 122-Page 278.

(1)

Loss on \$1 is 4 cents, or for every \$1 paid I receive \$0.96. Hence $cost = $24.60 \div 0.96 = 25.625 .

(2)

Loss on \$1 is 10 cents, or for every \$1 paid he receives \$0.90. Hence $cost = $2360 \div \cdot 90 = $2622 \cdot 22$.

(3)

Gain on \$1 is 11 cents, or for every \$1 paid he receives \$1.11. Hence $cost = $7400 \div 1.11 = 6666.666 .

(4)

Gain on \$1 is 17 cents, or for every \$1 paid he receives \$1.17. \$117: \$100:: \$3789.40: $\frac{3789.40 \times 100}{117}$ = \$3238.803.

(5)

Loss on \$1 is 13 cents, or for every \$1 paid I receive \$0.87. 2740×100 \$87: \$100 :: \$2740 : = \$3149.425.

Execuse 123-Page 279.

(1)

\$2 gains 50 cents.

Hence \$0.50: \$0.10:: \$2.00: $\frac{2.00 \times 10}{50}$ = 40 cents.

f 1½ cents. = $\frac{1}{8}$ of a cent. $\frac{10}{12}$ = 12½ p. c.

§ of a dollar.

\$1 loses 674260

syy per cent.

= whole sum

31 gains 7 9 6 2 3 2

 $\frac{500}{29} = 9.89$ or

\$4.25. urance.

valorem duty. $623 \cdot 70 + \$2 \cdot 70$

925.

ains 39934075

8749 or nearly

Ex

12] 17

361

(2)

 $$2.00:$2.80::$2.50:\frac{2.50\times2.80}{2.00}=$3.50.$

(3)

8 cents gain 5 cents in 9 months.

Hence 9 mo's: 6 mo's:: 5 cents: $\frac{5 \times 6}{9} = 3\frac{1}{3} = \text{gain for 6 mo's.}$

8 cts.: 12 cts.:: $3\frac{1}{3} \times 12 = 5$ cts. gain on 12 cts. for 6 mo's.

Therefore 12 + 5 = 17 cents = his selling price.

(4)

\$1.60: \$1.85:: \$0.55: $\frac{1.85 \times .55}{1.60}$ = \$0.6359375 = what L

ought to get in order to sell at the same profit as K. But L only gets 60 cents, therefore K has the advantage.

70 yds. of cloth at $1.85 = 1.85 \times 70 = 129.50$. $129.50 \div 60 = 215$.

(5)

5 tons of butter at \$102 = \$102 × 5 = \$510 10\frac{1}{2}\$ tons of tallow at \$135 = \$135 × 10\frac{1}{2}\$ = \$1417.50 Total value = \$1927.50

> Deduct ready money, \$600-30 \$1327-26

\$1327 · 20 - \$4 · 20 = 316 barrels.

3 . 50.

EXERCISE 124-Page 281.

(1)

(2)

k	for	6	mo's.	

cts. for 6 mo's.

75 = what L

as K.

vantage. \$129.50.

\$510

= \$1417.50

\$1927.50

, \$600.30

\$1327-26

						cara			2	gallons	@	14s.	=	28s.
121	66	X	21	=	262	u			1	- 16				128.
17							Poplar.		2	u				18s.
	4		4 /		-	• 1			4	- 46				32s.
361				361)569	"	y to the te	19.5	_			1000		
				2	2	и		1	9				9)	90s.
														_
				73)	1139	(15#4	carat	8.						10s.

(3)

(4)

EXERCISE 125-Page 283.

(1)

Prices. Differences. Prices.

$$125 = \begin{cases} 160 - 35 - 15 + 110 \\ 140 - 15 - 25 + 100 \end{cases} = 125$$

Prices. Differences. Prices.

$$125 = \left\{ \frac{166 - 35}{140 - 15} \right\} = \frac{15 + 110}{25 + 100} = 125$$

Ans. 35 bush. @ \$1.10, 15 @ \$1.60, 15 @\$1, and 25 @ \$1.40. 35 bush @ \$1.00, 15 @ \$1.40, 15 @ \$1.10, and 25 @ \$1.60.

(2)

Prices. Differences. Prices.

$$45 = \begin{cases} 60 - \overline{15} - \overline{3} + 42 \\ 50 - 5 - 7 + 38 \\ 15 + 30 \end{cases} = 45.$$

Prices. Differences. Prices.

$$45 = \begin{cases} 60 - 15 & 3 + 42 \\ 50 - 5 & 7 + 38 \\ 15 + 30 \end{cases} = 45.$$

Ans. 15 quarts @ 42 cents, 3 @ 60 cents, 5 @ 38 cents, 5 @ 30 cents, and 7 + 15 = 22 @ 50 cents.

15 quarts @ 38 cents, 3 @ 50 cents, 5 @ 42 cents, 15 @ 30 cents, and 7 + 15 = 22 @ 60 cents.

(3)

Prices. Differences. Prices.

$$12\frac{1}{2} = \begin{cases} 18 - 5\frac{1}{2} \\ 17 - 4\frac{1}{2} \\ 16 - 3\frac{1}{2} \\ 15 - 2\frac{1}{2} \\ 14 - 1\frac{1}{2} \end{cases} = 12\frac{1}{2}.$$

Ans. $\frac{1}{2}$ lb. @ 18 cents, $\frac{1}{2}$ @ 17 cents, $\frac{1}{2}$ @ 16 cents, $\frac{2}{2}$ @ 15 cents, $\frac{2}{2}$ @ 14 cents, $\frac{5}{2}$ + $\frac{4}{2}$ + $\frac{3}{2}$ = $\frac{13}{2}$ @ 12 cents, and $\frac{2}{2}$ + $\frac{1}{2}$ = 4 @ 10 cents.

(4)

Prices. Differences. Prices.

$$10 = \begin{cases} 13 - 3 - 3 + 7 \\ 12 - 2 - 5 + 5 \end{cases} = 10.$$

Ans. 3 lbs. @ 7d., 3 @ 13d., 2 @ 5d., and 5 @ 12d.

nts.

25

25.

25 @ \$1·40.

25 @ \$1·60.

TI

Exercise 126-Page 284.

(1)

By Case I we find that 17 quarts @ 31 cents, 6 @ 16 cents, 6 @ 19 cents, and 6 @ 23 cents will make a mixture worth 25 cents per quart.

Therefore 17 qts. : 87 qts. :: 6 qts. : $\frac{6 \times 87}{17} = 30\frac{18}{7}$ quarts @

16 cents, and as there are 6 lbs. at each of the other prices, the same statement may be used, and the answer is therefore 30 17 quarts @ each price.

(2)

To produce a mixture worth 75 cents per bushel, we require 45 bushels @ 80 cents, 5 @ 37 cents, and 5 @ 68 cents.

Therefore 45 bush. : 70 bush. :: 5 bush. : $\frac{5 \times 70}{45} = 7\frac{7}{9}$ bush. oats @ 37 cents.

45 bush. : 70 bush. :: 5 bush. : $\frac{5 \times 70}{45} = 75$ bush. barley @ 68 cents.

(3)

To produce a mixture worth 1s. per lb., we require $1\frac{1}{2}$ lbs. @ 16d., $1\frac{1}{2}$ @ 14d., and 6 @ $10\frac{1}{2}$ d.

Then 1½ lbs.: 50 lbs. :: 1½ lbs.: 50 lbs. brass @ 14d.
1½ lbs.: 50 lbs. :: 6 lbs.: 200 lbs. pewter @ 10¼ d.

(4)

By Case I we find that 1 oz. of 20 carats fine, 1 of 21 carats fine and 3 of 23 carats fine, will make a mixture 22 carats fine.

Then 1 oz.: 30 oz.: 1 oz.: 30 oz. of 21 carats fine. 1 oz.: 30 oz.:: 3 oz.: 90 oz. of 23 carats fine.

Exercise 127-Page 285.

(1)

To produce a mixture worth \$1.40 per lb., we require 20 lbs. @ \$1.00, 40 @ \$1.20, 40 @ \$1.60, and 20 @ \$1.80. But all of these added together, will make 120 lbs.

lbs. lbs. lbs. lbs.

Therefore 120 : 20 :: $168 : \frac{168 \times 20}{120} = 28$ lbs., the required quantity @ \$1.00.

120: 40:: $168: \frac{168 \times 40}{120} = 56$ lbs., the required quantity @ \$1.20.

120: 40:: $168: \frac{168 \times 40}{120} = 56$ lbs., the required quantity @ \$1.60.

120: 20:: 168: $\frac{168 \times 20}{120}$ = 28 lbs., the required quantity @ \$ 1.80.

(2)

To produce a mixture worth 4s. 4d. per lb., we require 10 lbs. @ 5s. and 8 @ 3s. 6d. But these added together make 18 lbs.

lbs. lbs. lbs. lbs.

Therefore 18: 10:: 27: $\frac{27\times10}{18}$ = 15 lbs., the required quantity of tea @ 5s.

18: 8:: 27: $\frac{27 \times 8}{18}$ = 12 lbs., the required quantity of tea @ 3s. 6d.

@ 16 cents, 6 ture worth 25

014 quarts @

her prices, the therefore 30+3

el, we require cents.

= 77 bush.

- == 7% bush.

re 11 lbs. @

@ 14d.

er @ 101d.

of 21 carats carats fine.
ts fine.
ts fine.

(3)

To produce a mixture worth \$2.70 per gallon, we require 20 gallons @ \$2.40, 10 @ \$2.60, 10 @ \$2.80, and 30 @ \$2.90. But all of these added together will make 70 gallons. Therefore gals. gals. gals.

70: 20:: 63: $\frac{63\times20}{70}$ = 18 gallons, the required quantity of brandy @ \$2.40.

70: 10:: 63: $\frac{63\times10}{70}$ = 9 gallons, the required quantity of brandy @ \$2.60.

70: 10:: 63: $\frac{63\times10}{70}$ = 9 gallons, the required quantity of brandy @ \$2.80.

70: 30: 63: $\frac{63\times30}{70}$ = 27 gallons, the required quantity of brandy @ \$2.90.

EXERCISE 128-Page 289.

(1)

1974.80 × 3 = £740.55 = £740 11s.

(2)

 $765 \cdot 43 \times \frac{2}{5} = £306 \cdot 172 = £306 \ 3s. \ 5\frac{7}{25}d.$

(3)

 $8172 \cdot 19 \times \frac{1}{4} = £2043 \cdot 0475 = £2043 0s. 11 \frac{2}{3}d.$

Exercise 129-Page 289.

(1)

£743 18s. 11d. = £743.94583 and 743.94583 $\div \frac{3}{10}$ = \$2479.8194.

\$ 300 tops & 150

n, we require 20 and 30 @ \$2.90. lons. Therefore

quired quantity

uired quantity

uired quantity

uired quantity

₹.d.

11§d.

=\$2479.8194.

(2)

£119 9s. 8\d. = £119.484375 and 119.484375 \div \frac{3}{2} = \$318.625.

(3)

£473 17s. 12d = £473.8572916, and 473.8572916 $\div \frac{7}{30}$ = \$2030.816964.

Exercise 130-Page 290.

(1)

 $1006 \cdot 90 \div 4 \cdot 867 = £206 \cdot 88309 = £206 178.7 d.$

(2)

 $916 \cdot 87 \div 4 \cdot 867 = £188 \cdot 38504 = £188 78.81d.$

(3)

2114·81 - 4·867 = £434·52023 = £434 10s. 42d.

Exenotse 131-Page 290.

(1)

£2043 11s. 3d. = £2043.5625 and 2043.5625 \times 4.867 = \$9946.01868.

(2)

£777 7s. 7d. = £777.37916 and 777.37916 × 4.867 = \$3783.50437.

(3)

£557 19s. 51d. = £557.972916 and 557.972916 × 4.867 = £2715.65418.

Exercise 132-Page 294.

(1)

 $$16785 \cdot 25 \times 5 \cdot 04 = 84597 \text{ francs } 66 \text{ centimes.}$

(2)

Commercial value of the marc banco = 35 cents.

Add 1 per cent 35

3535

Then $\$0.3535 \times 4000 = \1414 .

(3)

 $$35678 \times 1.0225 = $36480.755.$

(4)

The par value of 1 ruble = 75 cents.

Deduct 2 per cent $\frac{15}{735}$ Then $\$0.735 \times 2560 = \1881.60 .

(5)

Old commercial par of £1 sterling = \$4.444 = \$4.44444 Add 8 per cent .35555

\$4.79999

\$488

2580

=£

am

Then $\$4.79999 \times 800 = \$3839.999 = \$3840.00$.

the ...

ntimes.

cents.

Exercise 133-Page 295.

(1)

£1 = 420d.

191d. = 1 franc.

800 francs = 60 ducats.

1 ducat = 360 maravedis.

x = £1000.

R4

420×1×60×360×1000

-= 1564138 maravedis by cir. ex. 191×800

42½d. : £1000 :: 272 maravedis : -272×1000×20×12

424

16

272×1000×8×12

- =1536000 maravedis by direct exchange. XX

Difference = 1564138 - 1536000 = 28138 maravedis. 34)28138

8)827 reals 20 maravedis

103 piastres 3 reals 20 maravedis.

(2)

Old commercial par of £1 sterling = \$4.444

To which add 10 per cent. of itself = '4444

Gives price of £1 sterling = \$4.8884 \$4888.40:\$4.8884 = £1000 = amount of bill he receives if he remits direct to London.

\$1 = 515 centimes.) 515×4888·40

2580 cen. = £1 sterling. x = x = \$4888.40=£975.78526. 2580

=£975 15s. 84d.+=amount of bill he receives if he remits through Paris.

35 cents = 1 marc.

133 marcs = £i sterling.

x = \$4888.40.

4888.40 391072

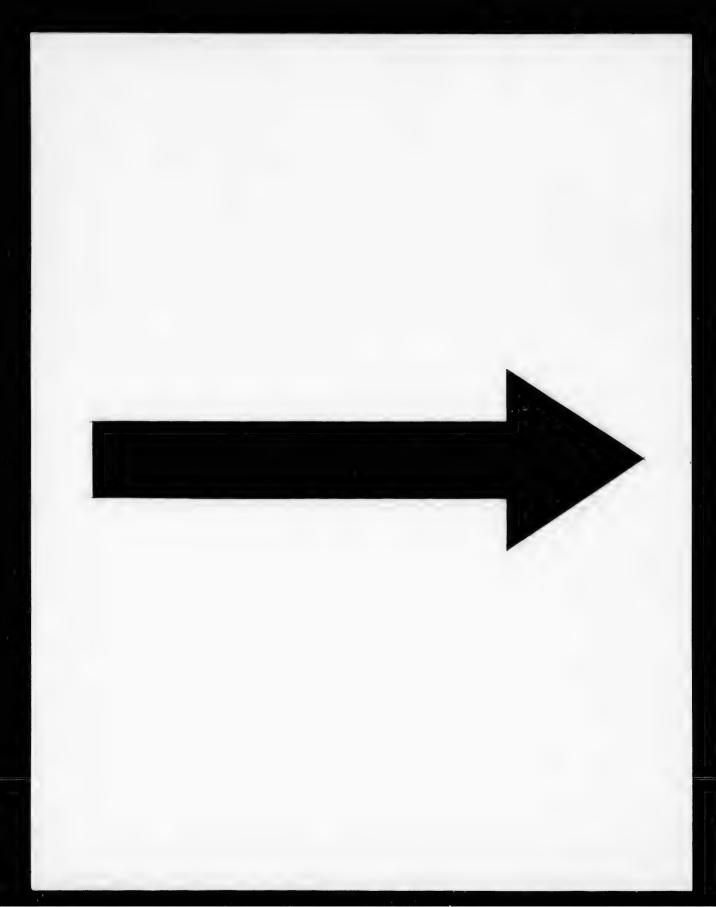
-= £1015·77142 = £1015 15s. 5d.+= 385

amount of bill he receives by remitting through Hamburg.

\$4.44444 .35555

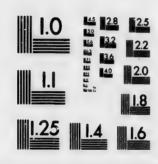
64.79999

.00.



11.25 M/A 14.6

IMAGE EVALUATION TEST TARGET (MT-3)



Photographic Sciences Corporation

23 WEST MAIN STREET WEBSTER, N.Y. 14580 (715) 872-4503 BILL GENERAL ON THE STATE OF TH



84)

882

(8)

18 cents. = 1 franc.
25 francs. = 240d.
180d. = 3 milrees,
5 milrees. = 18 marcs ban.
1200 marcs ban =
$$x$$

$$5 milrees. = 18 marcs ban.$$

= \$375 = circuitous exchange or sum he pays for 1200 marks. $1200 \times .35 = $420 =$ direct exchange or sum paid for 1200 marks. \$420 - \$375 = \$45 = gain by circuitous exchange.

Exercise 134-Page 298.

(1)

 $(3)^5 = 3 \times 3 \times 3 \times 3 \times 3 = 348.$

(2)

(3)

 $(1.05)^6 = 1.05 \times 1.05 \times 1.05 \times 1.05 \times 1.05 \times 1.05 \times 1.05 = 1.340095640625$

(4)

(1) = 1 × 1 × 1 × 1 × 1 × 1 × 1 = 7111.

(5)

(\$)" = \$ × \$ × \$ × \$ × \$ = 868.

(9)

118 = \$7. (\$7)* = \$7 × \$7 × \$7 = 345103 = 1481 48.

Exercise 135-Page 299.

$$4^2 \times 4^4 \times 4^5 \times 4^7 = 4^2 + 4 + 5 + 7 = 4^{18}$$

$$13^{11} \div 13^{8} = 13^{11} \stackrel{1}{\cdot} = 13^{9}.$$
 $(3^{3})^{5} = 3^{3 \times 5} = 3^{15}.$

(4)

$$\left\{ (7^4 \times 7^3) \div (7^2 \times 7^3) \right\}^6 = \left\{ (7^4 + 3) \div (7^2 + 3) \right\}^6 = \left\{ (7^4 + 3) \div (7^4 + 3) \right\}^6 = \left\{ (7^4 + 3) \div (7^4 + 3) \right\}^6 = \left\{ (7^4 + 3) \div (7^4 + 3) \right\}^6 = \left\{ (7^4 + 3) \div (7^4 + 3) \right\}^6 = \left\{ (7^4 + 3) \div (7^4 + 3) \right\}^6 = \left\{ (7^4 + 3) \div (7^4 + 3) \right\}^6 = \left\{ (7^4 + 3) \div (7^4 + 3) \right\}^6 = \left\{ (7^4 + 3) \div (7^4 + 3) \right\}^6 = \left\{ (7^4 + 3) \div (7^4 + 3) \right\}^6 = \left\{ (7^4 + 3) \div (7^4 + 3) \right\}^6 = \left\{ (7^4 + 3) \div (7^4 + 3) \right\}^6 = \left\{ (7^4 + 3) \div (7^4 + 3) \right\}^6 = \left\{ (7^4 + 3) \div (7^4 + 3) \right\}^6 = \left\{ (7^4 + 3) \div (7^4 + 3) \right\}^6 = \left\{ (7^4 + 3) \div (7^4 + 3) \right\}^6 = \left\{ (7^4 + 3) \div (7^4 + 3) \right\}^6 = \left\{ (7^4 + 3) \div (7^4 + 3$$

(5)

$$\left\{ (5^{3} \times 5^{4} \times 5^{11} \times 5^{9}) \div (5^{3} \times 5^{2} \times 5^{7} \times 5^{5}) \right\}^{3} =$$

$$\left\{ (5^{3+4+11+9}) \div (5^{3+2+7+5}) \right\}^{3} = \left\{ 5^{27} \div 5^{17} \right\}^{3}$$

$$\left\{ (5^{27-17})^{3} = (5^{10})^{2} = 5^{10} \times 3 = 5^{30} \right\}^{3}$$

Exercise 137-Page 304.

(1) (2) (0)

:	,		
195364(442	*0676(* 26 .		984064(992
16	4		81
	eddaid;		min.
84)353	46)276		189)1740
336	276		1701
882)1764		13e	1982)3964
1764		. ~	2004

= 1481 A.

· Set Min.

REXXXX

60 ×180×1200×5

for 1200 marks. n paid for 1200

us exchange.

 $\langle 20 \times 20 \times 20 \rangle$

× 1.06 =

10134

(5)

5-0000000000 00 2-236	06 -500000000000000000000000000000000000
42)1.00	· 1407)10000 9849
443)·1600 ·1329	14141)15100 14141
4466)27100 26796	1414206)9590000 8485236
447206)3040000 i 2683236	1104764
356764	
(6)	(7)
60.487129(7·777 49	79792266297612001(282475249
147)1148 1029	48)397 384
1547)11971 10829	562)1392 1124
15547)114229 108829	5644)26826 22576
5400	56487)425062 395409
(8)	564945)296539 7 2824725
·0000012321(·00111	6649502)14067261 11299004
21)23 21	56495044)276825720 225980176
221)221 221	564950489)5084554401 5084554401

(5)

00(-707108

Exercise 138-Page 304.

(1)

 $1 = \frac{1}{9}$ and $\sqrt{\frac{7}{9}} = \frac{1}{3}$.

(3)

5 = 5·142857142857 and $\sqrt{5\cdot142857142857}$ = 2·267786.

(4)

 $\frac{217}{318} = .4033457249$ and $\sqrt{.4033457249} = .63509$.

(5)

 $13\frac{1}{5} = 13.2$ and $\sqrt{13.2} = 3.63318$

Exercise 139—Page 305.

(1)

(2)

11333311(262 6	33233344(4344 24
46)433	123)523
411	413
552)2233	1304)11033 10024
5546)46611	13124)100544
46611	100544

01(282475249

17

(3)

(4)

4234·101230(43·412	\$88888-8880(888-88
31	71
133)1134	178)1788 1601
1414)130·10	1878)18788
122·21	16801
14231)2·3412	18878)1887·88
1·4231	1688·01
142322)·413130	188878)188·8780
·340144	168·8801
22431	18.8878

(5)

354 183)3264 2809

t867)657e t 62et 1

#8723)281969 281969

Exercise 140-Page 307.

(1)

100\$ = 10000 60\$ = 3600

Difference = 6400 and $\sqrt{6400}$ = 80.

0(888.88

80

78

(2)

.

 $50^{\circ} = 2500$ $80^{\circ} = 6400$

Sum = 8900 and $\sqrt{8900}$ = 94.34 nearly

(3)

 $24^2 = 576 \div 2 = 288$ and $\sqrt{288} = 16.97$,

(4)

 $36^{\circ} = 1296$

 $20^2 = 400$

Difference = 896 and $\sqrt{896}$ = 29.933.

(5)

 $\begin{array}{c} 40^2 = 1600 \\ 14^9 & 196 \end{array}$

Difference = 1404 and $\sqrt{1404} = 37.469$.

 $40^{9} = 1600$

 $26^2 = 676$

Difference = 924 and $\sqrt{924}$ = 30.397. 37.469 + 30.397 = 67.866 and $67.866 \div 3 = 22.622$.

(6)

1760 sq. yds. = 15840 sq. ft. and $\sqrt{15840}$ = 125.857.

(7)

 $\sqrt{141376} = 376.$

(8)

· — a

32 _ 8

Sum = 18 and $\sqrt{18}$ = 4.24264.

$$16^{\circ} = 256$$
 $12^{\circ} = 144$

Sum = 400 and
$$\sqrt{400}$$
 = 20

$$3^2 + 3^2 + 3^2 = 27$$
 and $\sqrt{27} = 5.196$.

$$(1_0^1)^2 = 1_0^1$$
 and $(1)^2 = 1$.

Then
$$\frac{1}{100}$$
: 1 :: 450 : $\frac{450}{\frac{1}{100}}$ = 45000.

(12)

1 sq. acre = 160 sq. perches.
$$160 \div 3.1416 = 50.929462$$
 and $\sqrt{50.929462} = 7.136$.

Exercise 141-Page 311.

(1)

		62712728317(397 3 27
3 ² ×300- 3×9×30= 9 ² =	2700 810 81	35712
	3591	32319
39°×300= 39×7×30= 7°	456300 8190 49	3393728
	464539	3251773
397°×300=47° 397×3×30= 3°=	282700 35730 9	141955317
• 1. 1 ja ng 1 47.	318439	141955317

0.929462 and

(8)

(8)

45025

1076890625(1025

225125

•

102°×300=3121200 15682625 102×5×30= 15300

5°= 25

3136525 15682625

(4)

·697864103(·887 512 $8^2 \times 300 = 19200$ 185864 8×8×30= 1920 82= 64 21184 169472 88°×300=2323200 16392103 88×7×30= 18480 72__ 49 1 2341729 16392103

(5)

102503-232(46.8 64 4º ×300= 4800 38503 4×6×30= 720 6º= 36 5556 33336 $46^2 \times 300 = 634800$ 5167-232 $46 \times 8 \times 30 = 11040$ 82= 645904 5167-232

[NAT. ARITE.

(6)

179597 . 069288 (56 . 42 125 5°×300= 7500 54597 5×6×30= 900 6°= 36 8436 50616 56°×300= 940800 3981 - 069 56×4×30= 6720 49= 16 947536 3790 - 144 $564^{\circ} \times 300 = 95428800$ 190 - 925288 564×2×30= 33840 22= 95462644 190 - 925288

(7)

483 - 736625(7 - 85 343 7 × 300= 14700 140 - 736 7×8×30= 1680 83= 64 16444 131 - 552 78°×300=1825200 9-184625 78×5×30= 11700 25 1836925

(-887

(46.8

165

(8)

8² × 300=19200 8×6×30= 1440 6²= 36

= 36

20676 124056

Execuse 14% -Page 312.

(1)

1 = ·105263157894+ and \$\sqrt{-105263157894} = ·4721.

(2)

 $\frac{2}{17} = \cdot 176470588235 + \text{ and } \sqrt[3]{\cdot 176470588235} = \cdot 5609.$

(3)

} of 2} = { = ·833333333+ and ₹ ·833333333 = ·941.

(4)

284 = 28.75 and \$\frac{1}{28.75} = 3.063

(6)

 $32\frac{1}{12} = 32 \cdot 72$ and $\sqrt{32 \cdot 72} = 3 \cdot 198$.

Expansis 143 .- Page 313.

(1) One million = 33233344 senary.

/		• • • • • • • • • • • • • • • • • • • •	
	*	83233344(244. 13	•
2°=4×3° 2×30=100×		21233	
	42= 24		
t	2424	14544	•
24°=1104×30	0=332000	2245344	
24×30=1200×	4= 5200 4°= 24		
	341224	2345044	
	(2)	-	
A CONTRACTOR OF THE PARTY OF TH		6131271 - 0000000 (1	65·32.
1°×300=	300	5131	
1×30×6=	220	0.04	
69=	44		
	564	4270	
16°=304×300=	111400	641271	•
16×30=520×5=	3220		**
5º=	31		
	114651	600115	
165 ² =32571×300= 165×30=5370×3=	12015300	41154-000	
32=	20300,		
	12035661	36131 • 423	
1653°=3272071×300=1	205625300	3022 - 355000	
1653 × 30=54010 × 2= 22=	130020		
1	205755324	2413 • 732650	
		406 · 422130	

[NAT. ARITE.

= -4721.

= ·5609.

33 = ·941.

(3)

1	1.	10221012 - 102000000
•	*	1 112.012=root.
1×1000=	1000	2221
1×1×100=	100	
	1	
# 5	1101	1101
11°=121×1000=	121000	1120012
11×100=1100×2=	2200	
in the many trans 19 3 =	11	
	200211	1101122
112 ⁸ =21021×1000=	21021000	11120 - 102
1120 ² =2102100×1000=	2103100000	11120 • 102000
1120×100=112000×1=	112000	
12=	1	. ,
	2102213001	2102 • 212001
112012=211010101×1000=3	11010101000	2010 - 112222000
11201×100=1120100×2=	10010200	
22=	11	
3)	11020111211	1122-111000122
4		111-001221101

(4)

	teteet.000000(e7.t2.
$e^{2} = t1 \times 300 = 26300$ $e \times 30 = 290 \times 7 = 1730$ $7^{2} = 41$	18eeet
27t71	167217
$e7^2 = e221 \times 300 = 2966300$ $e7 \times 30 = 2190 \times t = 24660$ $t^2 = 84$	249 t3 · 000
298e324	24154.764
$e7t^2 = e39544 \times 300 = 29e441000$ $e7t \times 30 = 2te60 \times 2 = 59e00$	84 t · 408000
22= 4	THE STEP STEP STEP STEP STEP STEP STEP STE
29e49 t e 04	57 t · 979 t08
	28 c · 64 t 1 e 4
(5)	
	421030·441200000(44·004 224
$4^{2}=31\times300=$ 14300 $4\times30=220\times4=$ 1430 $4^{2}=$ 31	142030
21311	141244
44°=4301×300= 2340300	231 • 441
440°=430100×300= 234030000	231 · 441200
4400^{9} = 43010000×300 = 23403000000 4400×30 = 242000×4 = 2123000 4^{2} = 31	231 • 441200000
23410123031	210 • 141102224

21.300042221

DATE ARETE

2·102000000 ·012=root.

-102

•102000

-212001

112222000

111000122

001221101

Exemples 144.—Page 314.

(2)

3°: 6 ° :: 41b. : Ans. = 32 lbs.

(3)

1*:-(1)3 :: \$120 : Ans. = \$5145.

(4)

(70)²: (⁶/₃²)³:: 180 lbs.: Ans. , 243000: ²⁴¹⁸/₂₄ ²⁴³/₂₄ :: 180: Ans. = 180 × ²⁴¹⁸/₂₅ ²⁴³/₂₅ × 243000 = 1015·1 lbs.

(5).

 $973^{\circ} = 921167317$ $45^{\circ} = 91125$

 $62^3 = 238328$

 $30^3 = 27000$

80° = 512000

 $20^3 = 8000$ 921167317 - (91125 + 238328 + 27000 + 512000 + 8000) =920290864 and $\sqrt[3]{920290864} = 972.69$.

(6)

8 feet 3 inches = 99 inches, 3 feet = 36 inches, and 2 feet 7 inches = 31 inches.

99 \times 36 \times 31 = 110484 and $\sqrt[8]{110484}$ = 47.9843.

(7)

After the first has wound off her portion, there will remain a of the thread.

Then the whole ball: part remaining:: cube of diameter of whole ball: cube of diameter of part remaining.

That is, $1:\frac{3}{4}::3^3:x^3$, and hence $x=3\times\sqrt[3]{4}=3\times\sqrt[3]{75}$ = 90856 \times 3 = 2.72568 = diameter of the ball after the first has wound off her portion.

Similarly after the second has wound off her portion, there will remain 1 of the ball, and after the third has taken her portion, 1 of the ball.

Hence 1: $\frac{1}{3}$:: 3³: x^3 , whence $x = 3 \times \sqrt[3]{5} = 3 \times \sqrt[3]{5}$

1: $\frac{1}{4}$:: 3^3 : x^3 , whence $x = 3 \times \sqrt[3]{4} = 3 \times \sqrt[3]{\cdot 25} = 3 \times \cdot 62996 = 1 \cdot 88988 =$ diameter after the third has taken her portion.

Hence 1st takes off 3 — 2.72568 = .27432 inches.

2nd " " 2.72568 — 2.38110 = .34458 "

3rd " " 2.38110 — 1.88988 = .49122 "

4th " " remaining 1.88988 "

Exercise 145-Page 315

(1)

 $\sqrt{19987173376} = 141376$, and $\sqrt{141376} = 376$.

(2)

 $\sqrt[8]{308915776} = 676$, and $\sqrt{676} = 26$.

(3)

 $\sqrt[4]{40353607} = 343$, and $\sqrt[4]{343} = 7$.

(4)

 $\sqrt[8]{287420489} = 730$. $\sqrt[8]{729} = 9$, and $\sqrt{9} = 3$.

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(5)

 $\sqrt[8]{134217728} = 512$, $\sqrt[8]{512} = 8$, and $\sqrt[8]{8} = 2$.

EXERCISE 148-Page 321.

(1) - Late plat of the finding a con-

The mantissa of the logarithm of 8193 (the first four digits) = .913443, and the next following mantissa is .913496.

Then from •913496 Subtract.. •913443

Difference, 53; and 53×217 (remaining digits of given number) = 11501, from which we cut off three digits, since we multiplied by a number of three digits, and since the highest digit cut off is not less than 5, weadd unity to the part retained, which gives us 12.

Then mantissa of logarithm of first four digits .913443 Add,

Mantissa of logarithm of given number, .913455

To which attach the characteristic 6 and required logarithm = 6.913455.

The mantissa of the logarithm of 7392 (the first four digits) = .868762, and the next following mantissa is .868821.

Then from .868821 Subtract. . .868762

Difference, 59; and 59 × 45 (remaining digits of given number) = 2655, from which we cut off two digits, since we multiplied by a number of two digits, and since the highest digit cut off is not less than 5, we add unity to the part retained which gives us 27.

Then mantissa of logarithm of first four digits, .868762 Add, 27

Mantissa of logarithm of given number, 868789

(Continued on next page.)

(1 continued.)

To which attach the characteristic 1 and required logarithm = 1.868789.

The mantissa of the logarithm of 8437 (the first four digits) = .926188, and the next following mantissa is .926240.

Then from .926240

Subtract.. . 926188

Difference, 52; and 52×42 (remaining digits of given number) = 2184, from which we cut off two digits, since we multiplied by a number of two digits, and since the highest digit cut off is not less than 5, we add unity to the part retained. which becomes 22.

Then mantissa of logarithm of first four digits .926188 Add, 22

Mantissa of logarithm of given number, .926210 To which attach the characteristic 1 and required logarithm = 1.926210.

(2)

The mantissa of the logarithm of 2345= .370143, and the next following mantissa is ·370328.

Then from •370328 Subtract. . . 370143

Difference, 185; and 185 \times 64 = 11840, from which we cut off two digits, since we multiplied by a number of two digits, which gives us 118.

Then mantissa of logarithm of 2345 = ·370143 Add,

Mantissa of logarithm of given number = .270261 To which attach the characteristic 4 an required legarithm = $\overline{4} \cdot 370261$.

(Continued on next page.)

four digits) 3496.

its of given its, since we the highest art retained.

ts .913443 12

.913455

garithm =

our digits) 21.

its of given s, since we ighest digit t retained.

868762 27

868789

(2 continued.)

The mantissa of the logarithm of 1007 = 003029, and the next following mantissa is .003461.

Then from .003461 Subtract....003029

Difference, 432; and $432 \times 013 = 5616$, from which we cut off three digits, since we multiplied by a number of three digits, and since the highest digit cut off is not less then 5, we add unity to the part retained, which gives us 6.

Then mantissa of logarithm of 1007 = .003029

Add,

Mantissa of logarithm of given number ·003035

To which attach the characteristic 3, and required logarithm == 3.003035.

(3)

Mantissa of logarithm of 5237	·719083
Difference from column D = 83; and 83 \times 6 = 498	110000
from which we cut off 1 digit and add	50
And also attach the characteristic 1, and required	
logarith m =	1.719133
Mantissa of logarithm of 1294	
Difference from column D = 335; and 335 \times 76 =	
25460 from which we cut off two digits and add,	255
And also attach the characteristic 2 and required	
logarithm =	2 · 112189

3029, and the

om which we aber of three as then 5, we

03029

_6

03035 logarithm ==

• 719083

50

8

đ .

1.719133

·111934

255

2.112189

· (4)

Mantissa of logarithm of .0004713 = .673297

P. P. corresponding to '00000009' =

P. P " to 000000008 = 74

Sum,= .6733874

Therefore required mantissa = $\cdot 673387$ and required logarithm = $\overline{4} \cdot 673387$.

Mantissa of logarithm of 9136000 = .960756

P. P. corresponding to 700 =

P. P. 1887 41 to 10 10 = 5

P. P. 10 10 10 to 10 2 = 617 (1) 9

Sum, = .96078959

Therefore required mantissa = .960790 and required logarithm = 6.960790.

(5)

Mantissa of logarithm of 4.23400 = .626751

P. P. corresponding to 20 = 20

P.P. 2500 1 10 10 to 3 10 1 9 = 300 92

Sum, = .6267802

Therefore required logarithm is 0.626780.

Mantissa of logarithm of 763-1 = '882581

P. P. corresponding to •02 = 11

P. P. " to .009 = 51

P. P. " to .0008 = 46

P. P. 12 you " or one to force 200009 = 132 200 40

Sum, = -882597600

Therefore required logarithm is 2.882598.

Ì

Exercise 149.—Page 323.

(1)

Given logarithm, ·137139

Next lower in table, ·137037 = log. of 1371.

Difference 102, Tabular difference = 316.

Then 1020000 ÷ 316 gives 3227 for digits in 5th, 6th, 7th, and 8th places.

Hence the digits of the natural number are 13713227; and since the characteristic is 4, i.e., one less than the number of digits to the left of the decimal point the required number is 13713-227.

Given logarithm, 718134

Next lower in table, .718086 = log. of 5225.

Difference, 48, Tabular difference = 83.

Then 48000 ÷83 gives 578 for digits in 5th, 6th, and 7th places.

Hence the digits of the natural number are 5225578, and since the characteristic is 0, i.e., one less than the number of digits to the left of the decimal point, the required number is 5.225578.

Given logarithm, 635421

Next lower in table, .635383 = log. of 4319.

Difference, 38, Tabular difference = 101.

Then 38000 - gives 376 for digits in 5th, 6th, and 7th places.

Hence the digits of the natural number are 4319376, and since the characteristic is $\overline{4}$, i.e., one more than the number of ciphers between the decimal point and the first figure to the right, the required number is $\cdot 0004319376$.

(2)

Given'log. .921686 = log. of 8350.

And since the characteristic is 2, i.e, one less than the number of digits to the left of the decimal point, the required number is 835.

Given logarithm, 922165

Next lower in table, 922154 = log. of 8359.

Difference = 11, Tabular difference = 52.

Then 11000 ÷ 52 gives 211 for digits in 5th, 6th, and 7th places.

Hence the digits of the natural number are 8359211; and since the characteristic is 1, i.e., one more than the number of ciphers between the decimal point and first figure to the right, the required number is 8359211.

(3)

Given logarithm, ·407968 Next lower in table, $-407901 = \log. \text{ of } 2558.$ Difference, = 67 Highest P. P. not greater than 67 = 51 corresponds to 3 for 5th place. 160 Highest P. P. not greater than 160 = 153 corresponds to 9 for 6th place. 70 Highest P. P. not greater than 70 = 68 corresponds to 4 for 7th place.

Therefore digits of required number are 2558394; and since the characteristic is 5, there must be six digits to the left of the decimal point.

Hence required number is 255839.4. (Continued on next page.)

ce = 316. th, 6th, 7th, and

13713227; and the number of ired number is

ce = 83.

and 7th places.

5578, and since nber of digits er is 5-225578.

e = 101:

6th, and 7th

376, and since ber of ciphers the right, the

(3 continued.)

Given logarithm,	* * * * * * * * * * * * * * * * * * *	•4	2888		
Next lower in tab	le,			= log. of 2560	•
Difference,	go, and total.	4118	146		
Highest P.P. not gr	eater than	146 =	136	corresponds to	0 8
	4	-		in 5th place.	ŧ
			100		
Highest P.P. not gre	ater than 1	100 =	85	corresponds to	
			150	an our prace	
Highest P.P. not gre	eater than	150 =	136 cc	orresponds to 8	}
and the second second in the second s	ander (T.). Frank Frank is	i nije	140	in 7th place.	
Highest P.P. not gre				orresponds to 8	
			*	- 44 OM DIRCE.	

Therefore digits of required number are 25608588; and since the characteristic is 7, there must be eight digits to the left of the decimal point.

Hence required number is 25608588.

Given logarithm,	•416369
Next lower in table,	·416308 = log. of 2608.
Difference, =	61
Highest P.P. not greater than 61 =	49 corresponds to 3
	in 5th place.

Therefore digits of required number are 26083; and since the characteristic is 3, there must be two ciphers between the decimal point and first figure.

Hence required number is .0026083.

log. of 2560.

orresponds to 8 in 5th place.

orresponds to 5 in 6th place.

responds to 8 7th place.

esponds to 8 in 8th place.

3588; and since its to the left of

log. of 2608.

orresponds to 3 in 5th place.

and since the

(4)

Given logarithm,	·877777
Next lower in table,	$\cdot 877774 = \log_{10} \text{ of } 7547$
Difference, = There is no P.P. not greater than 3	0 corresponds to 0 in 5th place.
Highest P.P. not greater than 30 =	= 29 corresponds to 5 in 6th place,
Highest P.P. not greater than 10 =	6 corresponds to 1 in 7th place.
Highest P.P. not greater than 40 =	35 corresponds to 6 in 8th place,
· Commence of the second	50
Highest P.P. not greater than 50 =	= 46 corresponds to 8 in 9th place.

Therefore digits of required number are 754705168; and since the characteristic is 4, there must be five digits to the left of the decimal point.

Hence required number is 75470.5168.

Given logarithm, Next lower in table,		55555 = log. of 3593.
Difference, =	1021 101	98.
Highest P.P. not greater the	in 98 =	98 corresponds to 8 in 5th place.

Therefore digits of required number are 35938; and since the characteristic is 0, there must be one digit to the left of the decimal point.

Hence required number is 3.5938.

Exercise 150.—Page 324.

(1)

(2)

10 - 5.631642 = 4.368358.

 $10 - \overline{3.123456} = 12.876544.$

10 - 0.714000 = 9.286000.

 $10 - \overline{7} \cdot 213149 = 16 \cdot 786851$.

(8)

10 - 6.124357 = 3.875643 and $10 - \overline{2}.000837 = 11.999163$.

Exercise 151.—Page 325.

(1)

Logarithm of 61 = 1.785330

" 22 = 1·342423

4 65 = 1.812918

Snm = 4.940666 = logarithm of 87230.

(3)

Logarithm of 52 = 1.716003

.44 = 2.865696

4 6 = 0.778151

Sum = 5-359650

5.359835 = logarithm of 229000

Ans. 229008

= 12.876544.

= 16.786851.

11.999163.

(3)

Logarithm of 35.86 = 1.554610

" 2·1046 = 0·323169

" ·8372 = 1.922829

" $00294 = \overline{3} \cdot 468347$

=Sum = 1-268955

1.268812 = logarithm of .185706

143 = 100 1000 61

Ans. ·185761

(4)

Log. of $\cdot 00008764 = \overline{5} \cdot 942702$

" ·86359 = 1·936308

Sum = 5.879010

5-878981 = logarithm of .000075680

29 -

. 5

Ane: 000075685

Exercise 152 .- Page 326.

(1)

logarithm of .6734 = 1.828273

·· ·0009278 = 4.967454

Difference = 2.860819

2.860817 = logarithm of 725.8000

2 = 1 4

Ans. 725-8033

9000

â000

-8

29008

(2)

Logarithm of 437.89 = 2.041365

62.735 = 1.797510

Difference = 843855 = logarithm of 6.98

(3)

Logarithm of 93.217 = 1.969495

 $-0007132 = \overline{4.853211}$

Difference = 5.116284

5·116276 = logarithm of 136700·0

8 = 2.4

Ans. 130702·4

(4)

Logarithm of 23 = 1.361728

" = 2.276462

2.748 = 0.439017

Sum = 4.077207

Logarithm of 9835267 = 6.992786

4.077207

Difference = 2.915579

2.915558 = logarithm of 823.300

21 =

. 39

Ans. 823-339

Exercise 153.—Page 326.

(1)

Logarithm of 5 = 0.698970. Then $0.698970 \times 5 = 3.494850 = logarithm of 3125$.

(2)

Logarithm of 1.073 = $\cdot 030600$. Then $\cdot 030600 \times 6 = \cdot 183600 = \text{logarithm of } 1 \cdot 5261$.

(3)

Logarithm of $\cdot 0279 = \overline{2} \cdot 445604$. Then $\overline{2} \cdot 445604 \times 4 = \overline{7} \cdot 782416 = \text{logarithm of } \cdot 00000060592$.

(4)

Logarithm of 1-111 = $\cdot 045714$. Then $\cdot 045714 \times 11 = \cdot 502854 =$ logarithm of 3-1831.

Exercise 154.—Page 327.

(1)

Logarithm of 913426000 = 8.960673. 8.960673 \div 7 = 1.2800961 = logarithm of 19.0588.

(2)

Logarithm of 1.61342 = .207747. $\cdot 207747 \div 11 = .01888609 = logarithm of <math>1.0444$.

(3)

Logarithm of $\cdot 000007139 = \overline{6} \cdot 853637 = \overline{10} + 4 \cdot 853637$. $\overline{(10 + 4 \cdot 853637)} \div 5 = \overline{2} \cdot 970727 = \text{logarithm of } \cdot 0934817$.

(4)

Logarithm of $\cdot 002147 = 3.331832 = 7 + 4.331832$. $(7 + 4.331832) + 7 = 1.6188331 = logarithm of \cdot 41575$.

6.98

of 130700-0

2.4

s. 130702·4

23.300

39

23.339

3125.

Exercise 155.—Page 328.

(1)

 $14000 = 7 \times 2 \times 1000 \therefore \log. 14000 = (\log. 7) + (\log. 2) + (\log. 1000).$

Log. 7 = 0.845098

Log. 2 = 0.301030

Log. 1000 = 3

Sum, $= 4.146128 = \log. 14000$

 $4.9 = 7^{2} \div 10 \cdot \log 4.9 = (\log 7) \times 2 - (\log 10).$

Log. $7 = 0.845098 \times 2 = 1.690196$

Log. 10 = 1 - 1 - 1 - 1 - 1 - 1

Difference = $\cdot 690196 = \log_{\bullet} 4.9$

 $.00196 = 49 \times 4 \div 100000 = 7^2 \times 2^2 \div 100000$

 $\log 0.0196 = (\log 7) \times 2 + (\log 2) \times 2 - (\log 100000)$

 $Log. 7 = 0.845098 \times 2 = 1.690196$

Log. $2 = 0.301030 \times 2 = 0.602060$

Sum = 2:292256

Log. of 100000 = 5 and $2.292256 - 5 = \overline{3.292256} = \log of .00196$.

Since $5 = 10 \div 2$, the logarithm of $5 = \log 10 - \log 2 = 1 - 0.301030 = 0.698970$.

 $1750 = 5^2 \times 7 \times 10$... log. $1750 = (\log. 5) \times 2 + (\log. 7)$ + $(\log. 10)$

Log. $5 = 0.698970 \times 2 = 1.397940$

Log. 7 = -84509

Log. 10 = The state of the last

Sum, = $3.243038 = \log \cdot of 1750$

 $1428.571428 = \frac{1}{7} \times 10000$... log. $1428.571428 = (\log \frac{1}{7}) + \log 10000$.

The realist

(1 continued.)

Log. $\frac{1}{7} = (\log. 1) - (\log. 7) = 0 - 0.845098 = 1.154902$ Log. 10000

 \therefore log. of 1428·571428 = sum = 3·154902

 $00000112 = 2^4 \times 7 \div 100000000 \cdot \cdot \cdot \log \cdot \cdot 00000112 =$ $(\log. 2) \times 4 + (\log. 7) - (\log. 100000000)$ $Log. 2 = 0.301030 \times 4 = 1.204120$

Log. 718 8 2 43 = 0.845098

> Sum = 2.049218 = and log. 1000000000 = 8 $2.049218 - 8 = \tilde{6}.049218 = \log..00000112$

 $3.0625 = 1\% \cdot \log \cdot 3.0625 = (\log \cdot 49) - (\log \cdot 16) =$ $(\log. 7) \times 2 - (\log. 2) \times 4.$

> $Log. 7 = 0.845098 \times 2 = 1.690196$ $Log. 2 = 0.301030 \times 4 = 1.204120$

> > Difference = $0.486076 = \log_{10} \text{ of } 3.0625$.

(2)

 $49\frac{1}{2} = \frac{90}{2} = 3^2 \times 11 \times \frac{1}{2} \therefore \log. 49\frac{1}{2} = (\log. 3) \times 2 + (\log 11)$ $+ (\log, \frac{1}{2}).$

 $Log. 3 = 0.477121 \times 2 = 0.954242$ Log. 11 = 1.041393Log. 1 = 1.698970

Sum = $1.694605 = \log_{10} of 49\frac{1}{2}$.

 $363 = 11^2 \times 3$: log. $363 := (\log. 11) \times 2 + (\log. 3)$. $Log. 11 = 1.041393 \times 2 = 2.082786$ Log. 3 = 0.477121

Sum = 2.559907 = log. of 363.

Log. 5 or $\frac{1}{2} = 1.698970$, and by altering the characteristic we get 0.698970 for log. of 5.

(Continued on next page.)

 $+ (\log. 2) +$

14000 (log. 10).

 $= \log.4.9$

og. 100000).

196

1060 256

 $256 = \log of$

 $-\log_{10} 2 = 1$

 $2 + (\log. 7)$

log. of 1750

 $(\log, \frac{1}{2}) +$

th

(2 continued.)

$$4.09 = 4_{11}^{1} = \frac{15}{11} = 3^{9} \times 5 \div 11 \cdot \log \cdot 4.09 = (\log \cdot 3) \times 2 + (\log \cdot 5) - (\log \cdot 11).$$

$$Log. 3 = 477121 \times 2 = 0.954242$$

$$Log. 5 = 698970$$

$$1.653212$$

Log. 11 = 1.041393 and 1.653212 - 1.041393 = 0.611819 = log. of 4.09.

 $2\cdot 4 = 2\frac{4}{9} = \frac{2}{9} = 11 \times 2 \div 9 \cdot \log 2 \cdot 4 = (\log 11) + (\log 11)$ 2) — $(\log. 3) \times 2$. Log. $2 = (\log. 10) - (\log. 5) = 1 - 0.698970 = 0.301030$. Log. 11 = 1.041393

Log. 2 = 0.301030

1.342423

Log. $3 = 0.477121 \times 2 = 0.954242$ and 1.342423 - 0.954243 $= 0.388181 = \log_{10} \text{ of } 2.4.$

 $392.72 = 3923^8 = 433^9 = 24 \times 3^3 \times 10 \div 11 \cdot ... \log. 392.72$ $= (\log. 2) \times 4 + (\log. 3) \times 3 + (\log. 10) - (\log. 11).$ Log. $2 = 0.301030 \times 4 = 1.204120$ Log. $3 = 0.477121 \times 3 = 1.431363$ Log. 10

Sum = 3.635483

Log. 11 = 1.041393 and 3.635483 - 1.041393 = 2.594090 =log. of 392,72.

 $293333\frac{1}{3} = \frac{880000}{3} = 2^3 \times 11 \times 10000 \div 3 \cdot ... \log. 293333\frac{1}{3}$ $= (\log. 2) \times 3 + (\log. 11) + (\log. 10000) - (\log. 3)$. Log. $2 = 0.301030 \times 3 = 0.903090$ Log. 11 = 1.041393Log. 10000

Sum = 5.944483

(Continued on next page.)

(2 continued.)

Log. 3 = 0.477121 and $5.944483 - 0.477121 = 5.467362 = log. of <math>2933333\frac{1}{3}$.

$$19.965 = 11^{3} \times 5 \times 3 \div 1000 \therefore \log. 19.965 = (\log. 11) \times 3 + (\log. 5) + (\log. 3) - (\log. 1000).$$

$$Log. 11 = 1.041393 \times 3 = 3.124179$$

$$Log. 5 = 0.698970$$

$$Log. 3 = 0.477121$$

Sum = 4.300270

Log. 1000 = 3 and $4.300270 = 3 = 1.300270 = \log$ of 19.965.

Exercise 156-Page 336.

(1)

Here we have given the first term 4, the number of terms 17 and the sum of the series 884, to find l, the last term.

Then
$$l = \frac{2r}{n} - a = \frac{884 \times 2}{14} - 4 := 104 - 47 = 100.$$

(2)

Here we have given the first term 21, the last term 497 and the number of terms 41, to find the common difference.

When
$$d = \frac{l-a}{n-1} = \frac{497-21}{41-1} = \frac{476}{40} = \frac{119}{10} = 11_{10}^9$$
.

(3)

Here we have given a, l, and d, to find n, and since a = 12, l = 96, and d = 6, we have

$$n = \frac{l-a}{d} + 1 = \frac{96-12}{6} + 1 = \frac{96}{6} + 1 = 24 + 1 = 15.$$

 $(\log.3) \times 2$

1242 970

212

= 0.611819 =

g. 11) + (log.

= 0.301030.

3 - 0.954242

·. log. 392·72 — (log. 11).

3

= 2·594090 **=**

log. 2933333 — (log. 3).

Ex

He

l =

E

l =

H

d =

8 =

H

a =

(4)

Here we have given l, d, and s, to find n, and since l = 14, d = 1, and s = 105, we have

$$n = \frac{2l+d}{2d} + \sqrt{\left(\frac{2l+d}{2d}\right)^2 - \frac{2s}{d}} = \frac{2\times 14+1}{2\times 1} + \sqrt{\left(\frac{2\times 14+1}{2\times 1}\right)^2 - \frac{2\times 105}{1}} = 14\frac{1}{2} + \sqrt{\left(\frac{2\times 14+1}{2}\right)^3 - 210} = 14\frac{1}{2} + \sqrt{\frac{2}{3}} = 15.$$

(5)

Here we have given a, d, and s, to find l, and since $a = \frac{c}{3}$, $d = \frac{a}{3}$, and s = 1180, we have

(6)

Here we have given a, l, and s, to find d, and since a=8, l=170, and s=4895, we have

$$d = \frac{(l+a)(l-a)}{2s-l-a} = \frac{(170+8)(170-8)}{2\times 4895 - 170 - 8} = \frac{178\times 162}{9790 - 178} = \frac{28836}{9612} = 3.$$

(7)

Here we have given a, l, and d, to find n, and since a = 5, $l = 27\frac{1}{2}$, and $d = 2\frac{1}{4}$, we have

$$n = \frac{l-a}{d} + 1 = \frac{27\frac{1}{2} - 5}{2\frac{1}{4}} + 1 = \frac{22\frac{1}{4}}{2\frac{1}{4}} + 1 = \frac{4}{2} + 1 = 10 + 1 = 11$$

,

nd since l = 14,

$$=\frac{2\times14+1}{2\times1}+$$

$$(2^{9})^{2} - 210 =$$

.

15.

and since $a = \frac{9}{3}$,

$$-\frac{1}{3}$$
 of $\frac{9}{3}$ +

$$47_3^{20} + (\frac{1}{3})^2 =$$

$$\frac{110}{3} = \frac{118}{3} = 391.$$

and since a = 8,

$$178 \times 162$$

nd since a = 5,

(8)

Here we have given a, l, and n, to find s, and since a = 2, l = 478, and n = 86, we have

$$s = (a + l)^{\frac{\alpha}{2}} = (2 + 478)^{\frac{\alpha}{2}} = 480 \times 43 = 20640.$$

(9)

Here we have given a, l, and d, to find s, and since a = 2, l = 998, and d = 6, we have

$$s = \frac{(l+a)(l-a)}{2d} + \frac{l+a}{2} = \frac{(998+2)(998-2)}{2 \times 6} + \frac{998+2}{2} = \frac{1000 \times 996}{2}$$

$$\frac{1000 \times 996}{12} + \frac{1000}{3} = 83000 + 500 = 83500.$$

(10)

Here we have given a, n, and d, to find l, and since a = 5, n = 11, and $d = 2\frac{1}{4}$, we have

$$l = a + (n-1)d = 5 + (11 - 1)2\frac{1}{4} = 5 + (10 \times 2\frac{1}{4}) = 5 + \frac{45}{5} = \frac{55}{274}.$$

(11)

Here we have given l, d, and n, to find s, and since l = 199, d = 11, and n = 19, we have $s = \begin{cases} 2l - (n - 1)d \\ n = 12 \end{cases}$

$$s = \left\{2l - (n-1)d\right\}_{\frac{n}{2}}^{n} = \left\{2 \times 199 - (19 - 1)11\right\}_{\frac{n}{2}}^{10} = \left\{398 - (18 \times 11)\right\}_{\frac{n}{2}}^{10} = 200 \times \frac{10}{2} = 1900.$$

(12)

Here we have given s, a, and l, to find n, and since s = 39840, a = 2, and l = 478, we have

$$n = \frac{2s}{l+a} = \frac{2 \times 39840}{478+2} = 72880 = 166$$

(13)

Here we have given s, l, and a, to find d, and since s=83500 l=998, and a=2, we have

$$i = \frac{(l+a)(l-a)}{2s-l-a} = \frac{(998+2)(998-2)}{(2\times83500)-998-2} = \frac{1000\times996}{167000-1000} = \frac{1000\times996}{167000-1000}$$

(14)

Here we have given s, a, and d, to find n, and since s = 360, a = 2, and d = 2, we have

$$n = \frac{d - 2a}{2d} + \sqrt{\frac{2s}{d}} + \left(\frac{2a - d}{2d}\right)^{2} = \frac{2 - (2 \times 2)}{2 \times 2} + \sqrt{\frac{2 \times 260}{2} + \left(\frac{(2 \times 2) - 2}{2 \times 2}\right)^{2}} = -\frac{1}{2} + \sqrt{260 + (\frac{1}{2})^{2}} =$$

 $-1 + \sqrt{260\frac{1}{4}} = -1 + 16.13226 = 15.63226$ days = 15 days, 15 hours, 10 minutes, 27.264 seconds.

(15)

Here we have given s, a, and d, to find l, and since s = 83500, a = 2, and d = 6, we have

$$\begin{array}{c} l = -\frac{1}{4}d + \sqrt{2ds} + (a - \frac{1}{4}d)^2 = -\frac{1}{4} \times 6 + \\ \sqrt{2 \times 6 \times 83500 + (2 - \frac{1}{4} \times 6)^2} = -3 + \sqrt{1002000 + (2 - 3)^2} \\ = -3 + \sqrt{1002001} = -3 + 1001 = 998. \end{array}$$

(16)

Here we have given s, n, and l, to find a, and since s = \$1125, n = 18, and l = 120, we have

$$a = \frac{2s}{n} - l = \frac{2 \times 1125}{18} - 120 = 125 - 120 = 5.$$

He = 2

EXH

Her one st

Then

n = 2

Her = 1

a =

Here a=4,

 $i = \{i$

Here

and n :

(17)

Here we have given a, l, and n, to find d, and since a = 5, l = 27l, and n = 11 we have

$$d = \frac{l-a}{n-1} = \frac{27\frac{1}{2}-5}{11-1} = \frac{22\frac{1}{2}}{10} = 2\frac{1}{2}.$$
(18)

Here we have a, d, and n given, to find s, and since to deposit one stone he must walk 5 yards, and the distance travelled for each succeeding stone is 5 yards, therefore a = 5, d = 5, and s = 220.

Then
$$s = \{2a + (n-1)d\}\frac{n}{2} = \{2 \times 5 + (220 - 1)5\}\frac{2}{2}$$

= $\{10 + (219 \times 5)\}110 =$
 $1105 \times 110 = 121550 \text{ yards} = 69\frac{1}{16} \text{ miles.}$

(19)

Here we have s, n, and l given, to find a, and since s = 39840, s = 166, and l = 478, we have

$$a = \frac{2s}{n} - l = \frac{2 \times 39840}{166} - 478 = 480 - 478 = 2.$$

(20)

Here we have n, a, and d given, to find s, and since n = 12, s = 4, and d = 2, we have

$$i = \left\{ 2a + (n-1)d \right\}_{\frac{n}{2}}^{\frac{n}{2}} = \left\{ 2 \times 4 + (12-1)2 \right\}_{\frac{n}{2}}^{\frac{n}{2}} = \left\{ 8 + (11 \times 2) \right\}_{6}^{\frac{n}{2}} = \left\{ 8 + (11 \times 2) \right\}_{6}^{\frac{n}{2}}$$

(21)

Here we have given a, l, and n, to find s, and a = 1, l = 24, and n = 24.

Then
$$s = (a + l)^{*}_{\frac{1}{2}} = (1+24)^{\frac{4}{2}} = 25 \times 12 = 300$$
,

d since s = 83500

ad since s = 360,

$$= \frac{2 - (2 \times 2)}{2 \times 2} + \frac{60 + (\frac{1}{2})^2}{2 \times 2}$$

days = 15 days,

since s = 83500,

$$6 + \frac{1000 + (2 - 3)^2}{= 998.}$$

ince s = \$1125,

120 = 5.

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Exercise 157-Page 842.

(1)

Here n = 11, a = £1024, and $r = 1\frac{1}{4}$. Then $l = ar^{2} - \frac{1}{2} = 1024 \times (\frac{3}{4})^{10} = 1024 \times \frac{59049}{1024} = £59049$ $= \frac{rl - a}{r - 1} = \frac{\frac{3}{2} \times 59049 - 1024}{\frac{3}{2} - 1024} = \frac{\frac{177147}{1024} - 1024}{\frac{3}{2} - 1024} = \frac{175099}{\frac{3}{2} - 1} = \frac{1775099}{\frac{3}{2} - 1024} = \frac{177509}{\frac{3}{2} - 1024} = \frac{177509}{\frac{3} - 1024} = \frac{177509}{\frac{3} - 1024} = \frac{177509}{\frac{3} - 1024} = \frac{177509$

(2)

Here a = 7, l = 1240029 and s = 1860040. Then $r = \frac{s-a}{s-l} = \frac{1860040-7}{1860040-1240029} = \frac{1860043}{650011} = 3$.

(3)

Here n = 12, a = £1, and l = £2048.

Then
$$r = {l \choose a}^{\frac{1}{s}-\Gamma} = {2048 \choose 1}^{\frac{1}{12}-\Gamma} = \sqrt[1]{2048} = 2$$

$$s = \frac{rl - a}{r - 1} = \frac{(2 \times 2048) - 1}{2 - 1} = 4096 - 1 = £4095.$$

(4)

Here $r = \frac{3}{2}$, n = 8, and $l = 106\frac{4}{6}\frac{9}{2}$. Then $s = \frac{l(r^{n} - 1)}{(r - 1)r^{n-1}} = \frac{106\frac{4}{6}\frac{9}{2} \times [(\frac{3}{2})^{8} - 1]}{(\frac{3}{2} - 1)(\frac{3}{2})^{7}} = \frac{\frac{4}{5}\frac{9}{4}\frac{7}{2} \times \frac{6}{2}\frac{3}{6}\frac{6}{6}}{\frac{1}{2} \times \frac{6}{12}\frac{3}{6}} = \frac{25 \times 6305}{512} = 307\frac{4}{6}\frac{1}{2}$. 1014 = £59049

5.

447±×6305

1X°187

(5)

KEY

Here a = 1, n = 7, and r = 8.

Then
$$s = \frac{a(r^2-1)}{r-1} = \frac{1 \times (3^7-1)}{3-1} = \frac{2136}{r} = 1093.$$

(6)

Here a = 1, l = 10077696, and n = 10.

Then
$$s = \frac{\vec{l} - \vec{1} - \vec{a}^{\frac{1}{2-1}}}{\vec{l}^{\frac{1}{2-1}} - \vec{a}^{\frac{1}{2-1}}} = \frac{(10077696)^{\frac{10}{10}} - 1^{\frac{10}{10}}}{(10077696)^{\frac{10}{10}} - 1^{\frac{10}{10}}} =$$

$$\sqrt[6]{(10077696)^{10}} - 1 = \sqrt[8]{(216)^{10}} - 1 = 6^{10} - 1 = 60466176 - 1$$

$$\sqrt[7]{10077696} - 1$$
 $\sqrt[7]{216} - 1$ 6-1 5 $-\frac{6046}{5}$ 12093235.

(7

Here a = 6, l = 3072, and s = 6138.

Then
$$r = \frac{s-a}{s-l} = \frac{6138-6}{6138-3072} = \frac{6138}{2088} = 2.$$

(8)

Here r = 2, n = 11, and s = 20470.

Then
$$l = \frac{(r-1)sr^{n-1}}{r} = \frac{(2-1)\times 20470\times 2^{10}}{r} = \frac{20470\times 1024}{r}$$

$$r^{*}-1$$
 $2^{11}-1$ 2047 $= 10240$.

18

(9)

Here
$$a = 1s$$
, $n = 12$, and $r = 3$.
$$a(r^{n}-1) = 1 \times (2^{1s}-1) = 4005$$
Then $s = \frac{1}{r-1} = \frac{2-1}{2} = 4005s$.

(10)

Here
$$a = 1$$
 farthing, $r = 2$ and $n = 32$.

$$a(r^n - 1) \qquad 1 \times (2^{32} - 1)$$
Then $s = \frac{1}{r - 1} = \frac{2 - 1}{2 - 1} = 4294967295$ far. $= \frac{44473924}{2} 5s$, $32d$.

(11)

Here
$$a = 4$$
, $l = 78732$, and $n = 10$.
Then $r = \left(\frac{l}{a}\right)^{\frac{1}{n-1}} = \left(\frac{78732}{4}\right)^{\frac{1}{10-1}} = \sqrt[9]{19683} = 3$.

(12)

Here
$$a = 5$$
, $r = 2$, and $n = 7$.
Then $l = ar^{n-1} = 5 \times 2^{7-1} = 5 \times 2^6 = 5 \times 64 = 320$.

(13)

Here
$$a = 5$$
, $l = 327680$, and $r = 4$.
$$\frac{rl - a}{r} = \frac{(327680 \times 4) - 5}{r - 1} = \frac{1310715}{2} = 436905.$$

409Fs.

967295 far. =

₹19683 = 3.

(14)

Here a = 1, r = 2, and n = 64.

Then
$$s = \frac{a(r^m-1)}{r-1} = \frac{1 \times (2^{64}-1)}{2-1} = 18446744073709551615 \text{ gr.}$$

 $18446744073709551615 \div (7680 \times 64) = 37529996894754$ bush. $\$1 \cdot 50 \times 37529996894754 = \56294995342131

(15)

Here r = 3, n = 10, and s = 295240.

Then
$$l = \frac{(r-1)sr^{n-1}}{r^n-1} = \frac{(3-1)\times 295240\times 3^9}{3^{10}-1} = \frac{2\times 295240\times 19683}{59048}$$

= 196830.

(16)

Here a = 1, l = 2048, and n = 12.

Then
$$s = \frac{\overline{l_{n-1}} - \alpha^{\frac{n}{n-1}}}{\overline{l_{n-1}} - \alpha^{\frac{1}{n-1}}} = \frac{2048^{\frac{12}{2}-1} - \frac{1}{12}}{2048^{\frac{1}{2}-1} - \frac{1}{12}} = \frac{1}{2048^{\frac{1}{2}-1} - \frac{1}{12}}$$

$$\frac{\sqrt[1]{(2048)^{12}-1}}{\sqrt[1]{2048-1}} = \frac{2^{12}-1}{2-1} = 2^{12}-1 = 4095.$$

17)

Here a = 5, r = 4, and n = 9. Then $l = ar^{n-1} = 5 \times 4^{9-1} = 5 \times 4^8 = 5 \times 65536 = 327680$.

 \times 64 = 320.

Exercise 158.—Page 344.

(1)

Here $a = \frac{2}{7}$, and $r = \frac{3}{8}$.

Then
$$s = \frac{a}{1-r} = \frac{3}{1-\frac{1}{2}} = \frac{3}{2} = \frac{3}{2}$$
.

(2)

Here a = 14, and $r = \frac{1}{4}$,

Then
$$s = \frac{a}{-r} = \frac{4}{1-1} = \frac{4}{1} = 8$$

(8)

Here $a = \frac{79}{100}$, and $r = \frac{1}{100}$.

Then
$$s = \frac{\alpha}{1-r} = \frac{70\sigma}{1-\frac{1}{10\sigma}} = \frac{70\sigma}{10\sigma} = \frac{70\sigma}{10\sigma}$$

(4)

Here $a = \frac{1234}{10000}$, and $r = \frac{1}{10000}$.

Then
$$s = \frac{a}{1-r} = \frac{\frac{1234}{10000}}{1-\frac{10000}{10000}} = \frac{\frac{1234}{10000}}{\frac{2022}{10000}} = \frac{1234}{10000}$$

Exercise 159.—Page 345.

(1)

Since there are 9 means and 2 extremes the number of terms is 11.

Then
$$d = \frac{l-a}{n-1} = \frac{92-2}{11-1} = \frac{98}{18} = 9.$$

1st term = 2; 2nd = 2 + 9 = 11; 3rd = 11 + 9 = 23; 4th = 20 + 9 = 29; 5th = 29 + 9 = 38; 6th = 38 + 9 = 47; and so on.

And series is 2, 11, 20, 29, 38, 47, 56, 65, 74, 83, 92.

(2)

Since there are 4 means and 2 extremes the number of terms is 6.

Then
$$d = \frac{l-a}{n-1} = \frac{50-7}{6-1} = \frac{15}{5} = 8\frac{3}{5}$$
.

1st term = 7; $2nd = 7 + 8\frac{3}{6} = 15\frac{3}{6}$; $3rd = 15\frac{3}{6} + 8\frac{3}{6} = 24\frac{1}{6}$; $4th = 24\frac{1}{6} + 8\frac{3}{6} = 32\frac{4}{6}$; $5th = 32\frac{4}{6} + 8\frac{3}{6} = 41\frac{2}{6}$; and $6th = 41\frac{2}{6} + 8\frac{3}{6} = 50$.

And series is 7, 153, 241, 324, 413, 50.

(3)

Since there are 8 means and 2 extremes the number of terms is 10.

Then
$$r = \left(\frac{l}{a}\right)^{\frac{1}{n-1}} = \left(\frac{1}{4086}\right)^{\frac{1}{10-1}} = \left(\frac{1}{318}\right)^{\frac{1}{9}} = \frac{1}{4}$$
.

1st term = 4096; 2nd = $4096 \times \frac{1}{4} = 2048$; 3rd = $2048 \times \frac{1}{4}$ = $1024 \times \frac{1}{4} = 512$; 5th = $512 \times \frac{1}{2} = 256$, and so on.

And the means are 2048, 1024, 512, 256, 128, 64, 32, and 16.

_ 23.

= 1384:

(4)

Since there are 7 means and 2 extremes the number of terms is 9.

Then
$$r = \left(\frac{l}{a}\right)^{\frac{1}{n-1}} = (23.5 \frac{146.94}{14.694})^{\frac{1}{9-1}} = (1679616)^{\frac{1}{8}} = 6.$$

1st term = 14; 2nd = $14 \times 6 = 84$; 3rd = $84 \times 6 = 504$; 4th = $504 \times 6 = 3024$; 5th = $3024 \times 6 = 18144$, and so on.

And the means are 84, 504, 3024, 18144, 108864, 653184, and 3919104.

EXERCISE 160.—Page 347

(1)

Assume 4 to be the number of men.

Then $2 \times 4 = 8 =$ number of women.

And $8 \times 3 = 24 =$ number of children.

6d. \times 4 = 24d. = amount received by the men.

4d. × 8 = 32d. = " " women.

2d. × 24 = 48d. = " " children.

Sum, = 104d., but it-should, by question, = 78d.

 78×4

Then $104:78::4:\frac{}{104}=3=\text{number of men.}$

3×2=6=number of women, and 6×3=18=number of child-[ren.

(2)

Assume £8 to be the price of the harness.

Then £8 \times 2 = 16 = price of horse.

And £8+£16 = £24 \times 2 = 48 = " chaise.

Sum, = £ 72, but it should by question = £60.

 8×60

Then £72: £60:: £8: $\frac{13}{72}$ = £6 13 4 = price of harness.

£6 13 $4 \times 2 = 13$ 6 8 = " herse.

£6 13 4 + £13 6 8 = £20 \times 2 = 40 0 0 = " chaige.

should by the question = 72.

aber of terms

 $79616)^{\frac{1}{8}} = 6.$

0010)- __ 0

 $4 \times 6 = 504$; 4, and so on.

, 653184, and

men.
women.
children.

= 78d.

men.

ber of child-

he harness.

estion = £60.

ce of harness.

horse.

EXEMPLES 100, 100,

(3)

Assume 20 as C's age.

Then $20 \times 3 = 60 = B$'s age.

And $60 \times 2 = 120 = A$'s age.

Sum = 200, but by question it should = 140.

 20×140

Then 200: 140:: 20: $\frac{}{200}$ = 14 = C's age.

 $14 \times 3 = 42 = B$'s age, and $42 \times 2 = 84 = A$'s age.

(4)

Assume 100.

One fourth of 100 = 25 and remainder = 100 - 25 = 75. One fifth of 75 = 15 and remainder = 75 - 15 = 60, but it

Then 60: 73:: 100: $\frac{100 \times 72}{60}$ = 120.

(5)

A can do the work in 7 days .. he will do } of it in 1 day.

Then all working together will do $\frac{1}{7} + \frac{1}{8} + \frac{1}{6} = \frac{10}{2}\frac{7}{6}$ in 1 day.

Therefore to do the whole work it will take them $\frac{107}{107} = \frac{210}{107} =$

1103 days.

(6)*

A and B working together can do it in 10 days ... they will do 10 of it in 1 day.

A can do it in 15 days .. he will do 15 of it in 1 day.

Therefore $\frac{1}{10} - \frac{1}{10} = \frac{1}{10} =$ amount done by B in 1 day.

Then if he does 10 in 1 day, it will take him 30 days to do the whole.

^{*}The mode of working these questions by position is so simple that they cannot trouble any one; it has therefore been thought advisable to work them by simple analysis.

The

(7)*

The first pipe empties the whole of it in 1 hour.

The second pipe empties 1 of it in 1 hour.

The third pipe empties } of it in 1 hour.

Then all these pipes running together will empty $1 + \frac{1}{3} + \frac{1}{3} = \frac{1}{3}$ in 1 hour.

Therefore to empty the cistern it will take $1 \div \frac{11}{6} = \frac{6}{11}$ hours.

(8)

Assume 84

One third of 84 = 28

One sixth of 84 = 14

One seventh of 84 = 12

Sum = 54, but by question it should = 27.

84×27

Then 54: 27:: 84: $\frac{64 \times 27}{54} = 42$

(9)

All 5 mills working together will grind 7 + 5 + 4 + 3 + 1 = 20 bushels in 1 hour.

Therefore to grind 500 bushels it will take them 500 - 20 = 25 hours.

(10)*

One pipe fills $\frac{1}{12}$ of the cistern in I hour, and the other empties $\frac{1}{18}$ of it in I hour.

Then $\frac{1}{18} - \frac{1}{18} = \frac{1}{80} = \text{part of the cistern filled in 1 hour when both are left open.}$

And if 30 of it is filled in 1 hour, the whole will be filled in

_ = 36 hours.

1

^{*} See note on page 227.

hours.

d = 27.

+3+1

0 - 20 =

he other

n 1 hour

filled in

Exercise 161.—Page 352.

I was to get (1) from the Assume 60 for father's age the

	TOL IMBIE	rs age,	then	10
5	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		* .****,	5
5)55	. TH			10
11 10				

Assume 100 for father's age, then 25 = son's.

5		b ugo,	5	HOU.
5)95	** *	: · ·	· 20	
19 20				
+1				
	Errors.		d numbers	ı.

+1 60 60

Sum of errors = 2 Sum of products = 160 Therefore result required = $160 \div 2 = 80 =$ father's age, and 2 of 80 = 20 = son's age.

(2)

Assume 80				ų 1	*	Assum	e 44 34
46	* *					· ·	10
138 80	, \$ ₁ ,						30 44
$\frac{1}{4}$ of 80 = $\frac{58}{20}$	Ŷ,	•			,	‡ of 44 =	- 14 - 11
+ 38	(Con	tipu	ed (on r	ex	page,)	-25

Therefore result required $= 3672 \div 63 == 58\frac{3}{7}$.

(4)

Assume 18 and 7

One half of 18 ==
$$\frac{9}{9}$$
 2 × 7= $\frac{14}{4}$

Assume 22 and 3

One half of 22 = $\frac{6}{11}$ 2 × 3 == $\frac{6}{14}$

Errors. Assumed numbers.

-5 × 22 == 110

+5 × 18 == 90

Sum of errors = 10 Sum of products = 200Then $200 \div 10 = 20$ one number and 25

Then 200 : 10 = 20 = one number, and 25 - 20 = 5 = other number.

•		(5)	
A.	B. "	A	В.
Suppose 8	6	Suppose 6	6
221	9	221	9
	12		12
180	15	· 135	15
132	18	81	18
-	21	,	21
8)48	24	6)54	_
-	27		81
+ 6	-	+ 9	
. 6	132	8	
,		-	
36		72	
72			
3)36			
		•	
12			

9 - 6 = 3 =difference of errors.

Exe

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NAT. ARITH

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72

87.

(7)

Assume 30.

 $\frac{1}{8}$ of 30 = 15; $\frac{1}{8}$ of 30 = $7\frac{1}{8}$; $\frac{1}{8}$ of 20 = 6; and $\frac{1}{8}$ of 30 = 5; 15 $\frac{1}{8}$ $\frac{7}{8}$ $\frac{1}{8}$ $\frac{1$

Assume 60.

 $\frac{1}{8}$ of 60 = 30; $\frac{1}{8}$ of 60 = 15; $\frac{1}{8}$ of 60 = 12; and $\frac{1}{8}$ of 60 = 10. 30 × 15 × 12 × 10 = 54000. 54000 - 6998 $\frac{1}{8}$ = + 47001·6 = error. 30⁴ = 810000, and 60⁴ = 12960000 - 3623·4 × 12960000 = 46959264000 + 47001·6 × 810000 = 38071296000

Sum = 50625 Sum = 85030560000 85030560000 ÷ 50625 = 1679616 4th root = square root of square root.

 $\sqrt{1679616} = 1296$, and $\sqrt{1296} = 36 = \text{required number}$.

NOTE.—For reason why we multiply by the 4th powers of the assumed numbers and then take the 4th root of the quotient, see Arith. page 858, Example 11.

It may, however, perhaps be clearer from the following illustration: Let x = the number required.

> > (8)

Suppose A had 9s. at first.

Then 9+1=10; $10 \div 2=5$; 5+1=6= what B had at first.

6+1=7, but should =9-1=8.

Error = 7 - 8 = -1.

Suppose A had 11s. at first.

Then 11 + 1 = 12; $12 \div 2 = 6$; 6 + 1 = 7 = what B had at first.

7+1=8, but should = 11-1=10. Error = 8-10=-2.

(Continued on next page.)

20 = 5

(8 continued.)

Errors.

$$\begin{array}{ccc}
-2 \times 9 &=& 18 \\
-1 \times 11 &=& 11
\end{array}$$

Diff.
$$= 1$$
 diff. $= 7$

 $7 \div 1 = 7 =$ shillings A had at first.

7+1=8; $8 \div 2=4$; 4+1=5= shillings B had at first

(9)

Assume 24 and 6.

$${}_{2}^{4} + {}_{3}^{4} + {}_{6}^{2} = 24.$$
 ${}_{2}^{6} + {}_{3}^{4}$ of $6 + {}_{2}^{6} = 9$.

 $\frac{6}{2} + \frac{3}{4}$ of $6 + \frac{6}{4} = 9$. 24 - 9 = +15 = error.

Assume 20 and 10.

$${}^{20}_{2} + {}^{20}_{3} + {}^{20}_{6} = 20.$$
 ${}^{1}_{2} + {}^{3}_{4} \text{ of } 10 + {}^{1}_{4} = 15.$
 ${}^{20}_{2} - 15 = + 5 = \text{error.}$

Errors.

$$+15 \times 20 = 300$$

 $+5 \times 24 = 120$

Diff. = $10 \, \text{diff.} = 180$

 $180 \div 10 = 18 =$ one number.

30 - 18 = 12 = other number.

(10)

Suppose 1st horse to be worth £20.

20 + 50 = 70; $70 \div 2 = £35 =$ value of 2nd horse.

$$35 + 50 = 85$$
, but it should equal 60, i. e. (20×3) .

Then 60 - 85 = -25 = error.

Suppose 1st horse to be worth £60.

£60 + £50 = £110; £110 \div 2 = £55 = worth of 2nd horse.

55 + 50 = 105, but it should equal 180, i.e. (60 × 3).

180 - 105 = +75 = error.

Errors.

 $3000 \div 100 = £30 =$ value of 1st horse.

£30 + £50 = £80; £80 \div 2 = £40 = value of 2nd horse,

EFER

Suppo 11 ×

11 X

Sup 12 X

 $12 \times$

Dif

Here . Then

= E

Here:

The

1

Here

Then

(11)

KEY.

Suppose there were 11 beggars.

$$11 \times 4 = 44$$
; $44 + 6 = 50 =$ number of pence he had.

$$11 \times 6 = 66$$
; $66 - 12 = 54 =$ " " $54 - 50 = +4 = \text{error.}$

Suppose there were 12 beggars.

$$12 \times 4 = 48$$
; $48 + 6 = 54 = pence he had.$

$$12 \times 6 = 72$$
; $72 \div 12 = 60 = \text{pence he had.}$
 $60 - 54 = + 6 = \text{error.}$

Errors.

$$+6\times11=66$$

$$+4 \times 12 = 48$$

Diff. = 2 diff. = 18, and $18 \div 2 = 9 = \text{number of beggars}$,

Exercise 162.—Page 357.

(1)

Here P = \$713.29, r = .045, and t = 14.

Then $A = P(1+r)^t$, or log. $A = \log P + \log (1+r) \times t$ $= 2.853267 + (.019116 \times 14) = 3.120891 = \log_{10} \text{ of } Ans.$ Hence amount = \$1320.96.

(2)

Here n = 7, r = .015.

log. n. ·845098 Then t == 130.698 payments, and $\log_{10}(1+r)$.006466

 $130.698 \div 4 = 32.674 \text{ years} = 32 \text{ years } 8 \text{ months } 2 \text{ days.}$

(3)

Here $\mathcal{A} = $1111 \cdot 11$, $P = 111 \cdot 11$, and r = .08.

Then
$$t = \frac{1}{\log_2(1+r)} = \frac{1}{033424} = \frac{1}{033424} = \frac{1}{29.918}$$
 years = 29 years 11 months.

had at first

[NAT. ARITH

d 10. = 20.

 $+\frac{10}{4} = 15.$ 5 = error.

and horse.

d horse.

Ext

Her

The

28.

He

For

He

(4)

Here
$$A = $3333\cdot33$$
, $P = $222\cdot22$, and $t = 120$.
Then $r = \sqrt[4]{\frac{A}{P}} - 1$; or log. $(1+r) = \frac{\log A - \log P}{t} = \frac{3\cdot522878 - 2\cdot346783}{120} = \frac{1\cdot176095}{120}$. Hence $1+r = 1\cdot0228$, $r = \cdot0228$, and rate per cent. $= 2\frac{7}{858}$

(5)

Here n = 2 and r = .07. Then $t = \frac{\log n}{\log (1+r)} = \frac{0.301030}{0.029234} = 10.2446$ years = 10 yrs. 2 months 28 days.

(6)

Here
$$A = \$100$$
, $r = .0225$, and $t = 28$.
Then $P = \frac{A}{(1+r)^t}$, or $\log P = \log A - \log (1+r) \times t$.
Log. $P = 2 - (0.009664 \times 28) = 2 - 0.270592 = 1.729408$.
Hence $P = \$53.63$.

(7)

Here $P = \$2468\cdot13$, $r = \cdot0375$, and t = 26. Then $\mathcal{A} = P(1+r)^t$, or log. $\mathcal{A} = \log P + \log (1+r) \times t$. Log. $\mathcal{A} = 3\cdot392368 + (0\cdot015988 \times 26) = 3\cdot392368 + 0\cdot415688 = 3\cdot808056$. Hence $\mathcal{A} = \$6427\cdot705$.

(8)

Here $\mathcal{A}=\$7137\cdot40$, $r=\cdot0425$, and t=22.

Then $P=\frac{\mathcal{A}}{(1+r)^t}$, or log. $P=\log \mathcal{A}-\log (1+r)\times t$.

Log. $P=3\cdot853540-(0\cdot018076\times22)=3\cdot853540-0\cdot397672=3\cdot455868$.

Hence $P=\$2856\cdot723$.

(16)

Here n = 19, and r = .0525.

log.
$$(1+r)$$
 0.022222
28.7722 years = 28 years 9 months 8 days.

Exercise 163 .- Page 360.

(1)

Here r = .03, a = 500, A = 8365.

$$\sqrt{\frac{8rA}{a} + (2-r)^2} - (2-r)$$

Formula IV. $t = \frac{a}{a}$

$$\sqrt{\left\{\frac{8\times \cdot 03\times 8365}{500} + (2-.03)^{\frac{2}{2}}\right\} - (2-.03)}$$

$$\sqrt{\left\{\frac{2007.6}{500} + 3.8809\right\} - 1.97}.$$

•06

$$=\frac{\sqrt{(4.0152+3.8809)-1.97}}{.06}=\frac{\sqrt{7.8961-1.97}}{.06}$$

$$= \frac{2.81 - 1.97}{.06} = \frac{.84}{.06} = \frac{.84}{.06} = 14 \text{ payments} = 7 \text{ years.}$$

(2)

Here a = 112.50, r = .015, t = 44.

Formula I.
$$A = at \left(1 + \frac{(t-1)r}{2}\right)$$

$$= 112.50 \times 44 \left(1 + \frac{(44-1) \times .015}{2}\right) = 4950 \times 1.3225$$

$$= \$6546.375.$$

log. P

Hence 1 + r

ars = 10 yrs.

 $1+r)\times t$

= 1.729408.

 $(1+r) \times t$

38 **+** 0·415688

 $+r) \times t$

0 - 0.397672

EX

Her

The

H

90

.04

Here

Here

(3)

Here a = 300, A = 1680, and t = 5.

Formula III.
$$r = \frac{2(A-at)}{at(t-1)} = \frac{2\{1680 - (300 \times 5)\}}{300 \times 5(5-1)}$$

= $\frac{2(1680 - 1500)}{300 \times 5 \times 4} = \frac{2 \times 180}{6000} = \frac{360}{6000} = \cdot 06$
 \therefore Rate per cent = $\cdot 06 \times 100 = 6$.

(4)

Here A = 2080, $\tau = .04$, and t = 16.

Formula II.
$$a = \frac{2 A}{t\{2 + (t - 1) r\}} = \frac{2 \times 2080}{16\{2 + (16 - 1) \cdot 04\}}$$

$$= \frac{4160}{16 \times \{2 + (15 \times \cdot 04)\}} = \frac{4160}{16 \times 2 \cdot 6} = \frac{4160}{41 \cdot 6} = \frac{4160}{416}$$

$$= \$100 = 1 \text{ payment or rent for half a year, hence yearly}$$

$$\text{rent} = \$100 \times 2 = \$200.$$

Exercise 164.—Page 366.

(1)

Here r = .04, and v = \$3000. Then $a = vr = 3000 \times .04 = 120 .

(2)

Here
$$a = 563$$
, and $v = 11260$
Then $r = \frac{a}{v} = \frac{563}{11260} = \frac{1}{20} = .05$, and hence rate per cent. = 5.

Comment Same

(3)

Here
$$a = 75$$
, $r = .05$, and $s = 14$.
Then $v = \frac{14}{75}$

 $r = \frac{1 \cdot r}{r \cdot (1+r)s} = \frac{\cdot 05 \times (1 \cdot 05)^{14}}{\cdot 05 \times (1 \cdot 05)^{14}}$ $= \frac{\log \cdot r}{1 \cdot 875061} = \frac{1 \cdot 875061}{1 \cdot 675061} = \frac{1 \cdot 875061$

... v = nat. number corresponding to the logarithm 2.879445, which is \$757.608.

(4)

Here
$$a = \$90$$
, $r = \cdot 04$, $t = 12$, $s = 7$, and $\cdot \cdot \cdot s + t = 19$.

Formula VIII. $v = \frac{a}{r} \left\{ \frac{1}{(1+r)^t}, \frac{1}{(1+r)^{s+t}} \right\}$

$$= \frac{90}{\cdot 04} \left\{ \frac{1}{(1\cdot 04)^{19}}, \frac{1}{(1\cdot 04)^{19}} \right\} = \frac{9000}{4} \left\{ \frac{1}{1\cdot 60101}, \frac{1}{2\cdot 10682} \right\}$$

$$= 2250 \times (\cdot 624605 + \cdot 474649) = 2250 \times \cdot 149956$$

$$= \$337 \cdot 401$$

(5)

Here a = 1500, and r = .05.

Formula IX. $v = \frac{a}{r} = \frac{1500}{.05} = \frac{150000}{5} = 30000 , $= 20 \times 1500$ or 20 years' purchase.

(6)

Here a = 22, v = 308.64166, and r = .04.

Then Formula VII. $t = \frac{\log a - \log (a - vr)}{\log a - \log (a - vr)}$

log. 22 — log. $(22 - 308.6416 \times 04)$

log. (1·04) 1·342423 — log. (9·65425) 1·342423 — 0·354707

- 06

0 × 5)}

2080

 $=\frac{41600}{416}$

ce yearly

0.

ce rate

Here
$$a = 154$$
, $t = 19$, and $r = .05$.

Formula V. $v = -\frac{a}{r} \left\{ 1 - \frac{1}{(1+r)^4} \right\}$

$$= \frac{154}{.05} \times \left\{ 1 - \frac{1}{(1.05)^{19}} \right\} = \frac{15400}{5} \times \left\{ 1 - \frac{1}{2.5269} \right\}$$

$$= 3080 \times (1 - .39574) = 3080 \times .60426 = $1861.12 + (8)$$

Here
$$A = 600$$
, $t = 40$, and $r = .0375$.

Formula II.
$$a = \frac{Ar}{(1+r)!-1} = \frac{600 \times .0375}{(1.0375)^{40}-1} = \frac{22.5}{4.36034-1} = \frac{3.36034}{2250000} = \frac{336034}{336034} = £6.6957 = £6 13s. 1034 +.$$
(9)

Here
$$a = 8$$
, $A = 187.315625$, and $r = .03$:

Formula IV.
$$t = \frac{\log. (Ar + a) - \log. a}{\log. (1 + r)}$$

 $\log. (187.315625 \times 0.3 + 8) - \log 8$

$$\frac{\log 1.03}{0.012837} = \frac{0.012837}{0.012837} = 18.$$
(10)

Here
$$a = 74$$
, $r = .04$, and $t = 30$
Formula I. $A = a\{(1+r)^5 - 1\}$ $74 \times \{(1.04)^{30} - 1\}$

EXER

\$7580 D is 1

f

\$6139

A is

\$4604

A atheref
A b

hour. The is

£17 \$718.9 \$ Exercise 165-Page 367.

EXAMINATION PROBLEMS.

FIRST SERIES.

(2)

\$7580 × ·19 = \$1440·20, and \$7580 — \$1440·20 = \$6139·80. D is to have one third as much as A, B, and C together, therefore he will have one-fourth of the whole. \$1534·95 = D's share.

\$6139.80 — \$1534.95 = \$4604.85 = amount to be divided among A, B, and C.

B is to have \$90.90 more than C.

A is to have \$111.11 + \$90.90 = 202.01 " "

\$292.91

\$4604.85 - \$292.91 = \$4311.94 =three times C's share.

 $$4311.94 \div 3 = $1437.31\frac{1}{3} = \text{C's share.}$

 $$1437\cdot31\frac{1}{3} + $90\cdot90 = $1528\cdot21\frac{1}{3} = B's share.$

 $$1528 \cdot 21\frac{1}{3} + $111 \cdot 11 = $1639 \cdot 32\frac{1}{3} = A's share.$

(3)

A and B working together can do the work in 96 hours, therefore in one hour they will do $\frac{1}{96}$ of it.

A by himself can do the work in 192 hours; therefore in 1 hour he can do $_{T_9^1 Z}$ of it. $_{9_6^1} - _{T_9^1 Z} = _{T_9^1 Z} = _{T_9^1 Z} = _{part}$ B can do in one hour. Therefore he will require as many hours to finish it as $_{T_9^1 Z}$ is contained times in the whole, i. e. $1 \div _{192} = 192$ hours. Then $192 \div _{14} = 13_7^5$ days.

(4)

£179 14s. $8\frac{2}{4}d$. = \$718.94 $\frac{1}{2}$ = \$718.94583. \$718.94583 \div .00000048 = \$7189458333333 \div 48 = \$1497803819.4444.

(5)

77 | \$\frac{44.18.30.77.56.27}{30 | \$4.18.80 | \$8.27} 36 | \$2.8 | \$4.27 77 \times 30 \times 36=83160 = 1.c.m.

 $\frac{1}{2.5269}$ \$1861.12 +

800 × ·03 75

·0375) ⁴⁰—1 0 — 4

3090

 $04)^{30} - 1$

= \$4150-142

4 per cent.

Es

Dif

\$89

5 13 27

24 11 x

(6)

Here n = 20, and r = .0525. Then $t = \frac{n-1}{r} = \frac{20-1}{.0525} = \frac{19}{.0525} = 361 .9048$ years = 361 years 10 months 25 days.

(7)

7342163 octenary = 710e57 duodenary, and 61351 nonary = 1e454 duodenary.
710e57 ÷ 1e454 = 40.38 duodenary.

(8)

$$783\frac{1}{3} = 3\frac{1}{2} + 10 \times 8 + 10 \times 10 \times 7.$$
1bs. oz. dwt. grs.
43 8 17 11 × 3\frac{1}{2} = 151 7 11 2\frac{1}{2}
$$10$$

$$433 2 14 14 \times 8 = 3465 9 16 16$$

$$10$$

$$4332 3 5 20 \times 7 = 30325 11 0 20$$

$$33943 4 8 14\frac{1}{4}$$

(9)

Here
$$a = 1$$
, and $r = \frac{1}{2}$.
Then $S = \frac{a}{1 - r} = \frac{1}{1 - \frac{1}{2}} = \frac{1}{\frac{1}{2}} = 2$

(10)

$$\frac{2\frac{1}{3}}{3} = 64 \div \frac{\frac{6}{3}}{3} = 64 \div \frac{\frac{6}{3}}{\frac{2}{3}} = 64 \div \frac{\frac{6}{3}}{\frac{2}{3}} = 64 \div \frac{\frac{6}{3}}{\frac{2}{3}} = 64 \div \frac{\frac{6}{3}}{\frac{2}{3}} = \frac{64}{3} \times \frac{\frac{6}{3}}{\frac{2}{3}} = \frac{64}{3} \times \frac{\frac{6}{3}}{\frac{2}{3}} = \frac{129 \cdot \frac{2}{3}}{\frac{2}{3}}$$

48 years =

nonary =

(11)

Logarithm of 129140163 = $8 \cdot 111061$. 8·111061 \div 17 = ·477121 = logarithm of 3.

Suppose 48 18	(12) Suppose	36 18
66 84	SAME TO SAME TO SAME	54 63
- 18		- 9

Errors. Assumed numbers. $-18 \times 36 = 648$

 $-9 \times 48 = 432$

Difference of errors = 9 9)216 = sum of products.

SECOND SERIES.

(13)

B is to have \$69.18 more than C. A is to have \$69.18 + \$93.40 = \$162.58 " " "

\$231.76

\$897.43 - \$231.76 = \$665.67 =Amount to be divided equally amongst A, B, and C.

 $$665 \cdot 67 \div 3 = $221 \cdot 89 = 0$'s share.

 $\$221 \cdot 89 + \$69 \cdot 18 = \$291 \cdot 07 = B's$ " $\$291 \cdot 07 + \$93 \cdot 40 = \$384 \cdot 47 = A's$ "

(14)

			()		1	
lbs.	wheat	= 9	lbs. rye	1	z = z	
44	rye	= 8	" oats	İ	5 = 8	
"	oats	= 21	" buckwheat		18 = 31	T
" }	ouckwhe	at= 20	" barley	8	24 = 26	4
11	parley	= 26	" peas	3	24 = 26	2
" 1	peas	= 35	" potatoes	1	11 ==35	
"]	potatoes	= 16	" wheat		x = 16	
	" " " "	" buckwhe " barley " peas	" rye = 8 " oats = 21 " buckwheat= 20 " barley = 26 " peas = 35	lbs. wheat = 9 lbs. rye " rye = 8 " oats " oats = 21 " buckwheat " buckwheat= 20 " barley	lbs. wheat = 9 lbs. rye " rye = 8 " oats " oats = 21 " buckwheat " buckwheat= 20 " barley " barley = 26 " peas " peas = 35 " potatoes	lbs. wheat = 9 lbs. rye " rye = 8 " oats " oats = 21 " buckwheat " buckwheat = 20 " barley " barley = 26 " peas " peas = 35 " potatoes $x = x = x = x = x = x = x = x = x = x =$

Ans.
$$\frac{4 \times 2 \times 35 \times 16}{3 \times 11} = \frac{4480}{33} = 135\frac{3}{3}\frac{5}{3}$$
.

16

grs.

20 141

64 ÷ = \frac{6}{27}

(15)

 $\frac{2}{3}$ of $\frac{4}{3}$ of $\frac{74}{5}$ of $\frac{9}{19\frac{1}{3}}$ of $\frac{5}{9}$ of 3 oz. 4 drs. 2 scr. 5 grs. = $\frac{2}{3}$ of $\frac{9}{2}$ of $\frac{19}{3}$ o

(16)

Dissimilar. Similar and Coterminous.

 $623 \cdot 42793 = 623 \cdot 42793793 = 623 \cdot 42793793793$ $93 \cdot 4267192 = 93 \cdot 4267192 = 93 \cdot 42671929292$

Difference = 530 · 00121864500

(17)

\$1.00 - \$0.046 = \$0.954, and $$7493 \div 0.954 = 7854.29 .

36: 20 weeks

6: 5 days

9: 11 hours
11: 24 cellars

20: 22 feet long

16: 22 feet wide

5: 4 feet deep

86× 6×9×11×30×16× 5

$$=\frac{11 \times 22}{9} = 26\frac{5}{9}.$$

(19)

 $\frac{1}{3}$ of $\frac{3}{3}$ of $\frac{1}{3} = \frac{6}{35}$; and if $\frac{6}{35}$ of a certain number $= \frac{72}{35}$, $\frac{1}{35} = \frac{12}{35}$ and $\frac{3}{35} = \frac{12}{35} \times 35 = 12$.

 $([[([(12 \times 12]) + 31] \times 3] - 33) \times 300] \div 17] \times 9)$ = 81000

(20)

1176 | 480... 768... 348... 1176 32 | 26... 32... 29 145 | 5 | 29 1176 × 32 × 145 = 5456640. 175

Ex

As with

\$120

\$2500

(21)

KEY.

838)171347(204 1676 3747 3352 395)838(2 17598)46090(2 35196 790 10894)17598(1 48)395)8 10894 384 6704)10894(1 11)48(4 6704 44 4190)6704(1 4)11(2 4190 2514)4190(1 3)4(1 2514 1673)2514(1 1)3 1676 839)1676(2

As no number greater than unity will divide all of them without a remainder, they have no G. C. M.

1676

(22)

 $$12000 + $8000 = $20000 \times 4 = 48000 \$88000 = product of A's stock and time. $$25000 \times 3 = 75000 $$25000 - $10000 = $15000 \times 3 = 45000 \$120000 = product of B's stock and time.

> $$35000 \times 2 = 70000 Continued on next page.)

= 3 of 3 of

T. ARITH.

7 of -121

rminous.

3793

9292

500

4.29.

 $2\times22\times4$

X

 $\frac{1}{36} = \frac{12}{36}$

7} × 9)

13.

```
(22 continued.)
 \$ of $35000 = $10000. $35000 - $10000 = $25000 \times 4 = 100000
                                                       $170000
                = product of C's stock and time.
$88000 + $120000 + $170000 = $378000 = sum of the pro-
                    ducts of stocks and times.
                                    15000 \times 88000
Then $378000 : $88000 :: $15000 : -
                                                   =$3492.06
                                        378000
                        = A's share.
                                15000 × 170000
$378000 : $170000 :: $15000 : -
                                               - = $6746 \cdot 03
                                    378000
                        = C's share.
$15000 - ($3492.06 + $6746.03) = $4761.91 = B's share.
                              (23)
A's gain in 5 months = $125 .. his gain for 9 months
    = 1 $ × $125..... = $225
B's gain in 6 months = $125.. his gain for 9 months
    =11 \times \$125.... = \$187\frac{1}{3}
C's gain in 9 months..... = $125
                                             Sum = $5371
                            400 \times 225
Then $5371 : $225 :: $400 : -
                                       -=$16718 = A's stock.
                                5371
                            400 × 1871
    $5371: $1871:: $400: -
                                      -= $13913 = B's stock.
                                 5371
                            400 \times 125
    $537\frac{1}{2}: $125:: $400:
                                       = $93\frac{1}{4} = C's stock.
                                5371
                             (24)
\frac{1}{6} + \frac{1}{4} + \frac{1}{10} + \frac{1}{12} = \frac{57}{120} = \frac{1}{48} = \text{part of the cistern filled in}
    one hour when the four pipes are left open.
```

 $\frac{1}{6} + \frac{1}{6} + \frac{1}{4} + \frac{1}{3} = \frac{1}{12} = \frac{2}{12} =$ part of the cistern emptied in one hour when the four are left open. $\frac{2}{6} - \frac{1}{4} = \frac{1}{4} =$ part of the cistern which remains filled after the eight pipes have been left open for one hour. And if $\frac{1}{4} = \frac{1}{6} = \frac{1}{12} = \frac{1}{6} = \frac{1}{12} = \frac{1}{6} =$

for Th

17

17

17

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Her

The

\$1.0

Her

The

4=100000

of the pro-

=\$3492.06

\$170000

1

THIRD SERIES.

(26)

As often as the first receives 4 the second receives 3, therefore as often as the first receives 6 the second receives $4\frac{1}{4}$. Then $6+4\frac{1}{4}+7=17\frac{1}{4}$.

loaves.

$$2310\times 6$$

$$2310 \times 4\frac{1}{2}$$

(27)

To produce a mixture worth 8 cents a pound, we require 4 lbs. @ 12 cents, 4 @ 4 cents, 1 @ 5 cents, and 3 @ 9 cents, or 3 lbs @ 12 cents, 1 @ 4 cents, 4 @ 5 cents, and 4 @ 9 cents, lbs.lbs.lbs.

Then 4:72::4:72 lbs. @ 4 cts. or 3:72::1:24 lbs. @ 4 cts. 4:72::1:18 lbs. @ 5 cts. 3:72::4:96 lbs. @ 5 cts. 4:72::3:54 lbs. @ 9 cts. 3:72::4:96 lbs. @ 9 cts.

(28)

Here
$$A = $4444.44$$
, $r = .0444$, and $t = 4.34$

Then P =
$$\frac{A}{1+rt} = \frac{\$4144\cdot44}{1+(\cdot0444\times4\cdot3\frac{4}{9})} = \frac{\$4444\cdot44}{1\cdot19289\frac{1}{3}} = \$3725\cdot764.$$

(29)

$$$1.00 - $0.0225 = $0.9775.$$
 $$23470 \div 0.9775 = $24010.23.$

(30)

Here
$$A = $7493.47$$
, $r = .07$, and $t = 8$.

Then
$$P = \frac{A}{1+it} = \frac{7493 \cdot 47}{1+(\cdot 07 \times 8)} = \frac{7493 \cdot 47}{1 \cdot 56} = $4803 \cdot 5064.$$

\$6746.03

share.

s = \$225

= \$187½ = \$125

= \$5371

=A's stock.

= B's stock.

C's stock.

rn filled in

emptied in

filled after ir. And if

take 1 ÷

EXED

of a

3% of

35 of

 $=\frac{49}{246}$ of

19.5 =

log. 5

1125 =

(31)

 $17460 \div 1.03125 = 16930.909 = \text{sum to be invested.}$

16930.909 ÷ 2.95 = 5739.29 yds. cloth.

 $16930.909 \times .021 = $423.27272 = ad valorem duty.$

\$17460 + \$1347.90 + \$479.40 + \$169.83 + \$423.27272 = \$19880.40272 = whole cost.

\$25000 - \$19880.40272 = \$5119.59728 =whole gain.

5119·59728 × 100

Then \$19880.40272:\$100::\$5119.59728: - 25.75 = 25\frac{3}{2} per cent.

19880-40272

(32)

	•		
v .	III.	VIII.	XII.
134234 =	= 21122021	== 12701	== 3281
5 + 5 + 5	3 ., .,	8	12
- P			_
8 3 4 2 3 4	7	10	38
5	3	8 ·	12
44 30 306 4	22	87	464
5 10 10 10 10 10 10 10 10 10 10 10 10 10	3	8 2 4	12
222	68	696	5569 den.
5 m 18 m 19 m	3 10 (2) (2)	· //	A par 14 表现数型
1113	206	5569 den.	er in er Er in er
5	3		1. 1
5569 den.	618	Marian State	- 1
	3		
	1856		Markey of Markey
	3		
	5569 den.		

(33)

 $\frac{9}{4}$ of $\frac{9\frac{3}{4}}{20}$ of $\frac{1}{16}$ of $\frac{7}{9}$ of £43 18s. 11\frac{1}{4}d. £43 18s. 11\frac{1}{4}d. = \$175.79\frac{1}{6}.

(Continued on next page.)

VAT. ARITH.

ed.

272 **—**

in.

× 100

272

XII.

3281

12

8

12

2

9 den.

111d. =

(33 continued.)

$$\frac{9}{7} \text{ of } \frac{9}{2} \text{ of } \frac{34^{2}}{10^{3}} \text{ of } \frac{7}{16} \text{ of } \frac{7}{3} \text{ of } \$175 \cdot 79\frac{1}{6}, = \frac{3}{7} \text{ of } \frac{9}{2} \text{ of } \frac{15}{1} \text{ of } \frac{1}{16} \text{ of } \frac{9}{9}$$
of \$175 \cdot 79\frac{1}{6} = \frac{3}{2} \text{ of } \\$175 \cdot 79\frac{1}{6} = \\$263 \cdot 6875.

 $3\frac{8}{9}$ of $\frac{1}{17\frac{1}{2}}$ of .56 of 1.75 of $6\frac{1}{2}$ times \$97.18 =

 $^{35}_{9}$ of $^{1}_{100}$ of $^{175}_{100}$ of 61 times \$97.18; 61 times \$97.18 = \$631.67.

$$\frac{35}{9} \text{ of } \frac{2}{35} \text{ of } \frac{13}{100} \text{ of } \frac{135}{100} \text{ of } $631.67 = \frac{49}{9 \times 25} \text{ of } $631.67$$

$$\frac{30}{30} \frac{25}{25}$$

= 249 of \$631.67

 $\frac{49}{226}$ of \$631.67 = \$137.5636.

Then \$263.6875 - \$137.5636 = \$126.1239 = difference.

 $\gamma_3^1 = \frac{1}{2} \div 13$.: $\log_{10} \gamma_3^1 = \log_{10} 1 - \log_{10} 13 = 0 - 1.113943$ = $\frac{1}{2} \cdot 886057$.

 $19.5 = 3 \times 13 \times 5 \div 10$... log. $19.5 = \log. 3 + \log. 13 + \log. 5 - \log. 10$.

 $\log_{10} 3 = 0.477121$

log. 13 = 1.113943log. $5 = \log \cdot 10 - \log \cdot 2 = 1 - 0.301030 \cdot \cdot \cdot \log \cdot 5 = 0.698970$

Sum = 2.290034

From which take $\log 10 = 1$

Rem. = 1.290034

=log. 19.5. 1125 = $5^3 \times 3^2$: log. 1125 = (log. 5) \times 3 + (log. 3) \times 2.

 $\log. 5 = 0.698970 \times 3 = 2.096910$

 $\log 3 = 0.477121 \times 2 = 0.954242$

Sum = 3.051152 = log. of 1125.

(Continued on next page.)

$$28\cdot 16 = 28\frac{1}{6} = \frac{16^{2}}{6} = 13^{2} \div 6 \cdot \cdot \cdot \log. \ 28\cdot 16 = (\log. \ 13) \times 2 - (\log. \ 2 + \log. \ 3.)$$

$$\log. 13 = 1.113943 \times 2 = 2.227886$$

$$(\log. 2 + \log. 3) = (0.301030 + 0.477121) = 0.778151$$

$$\text{Diff.} = 1.449735$$

 $= \log. 28.16.$

$$65000 = 13 \times 5 \times 1000$$
 ... \log . $65000 = \log$. $13 + \log$. $5 + \log$. 1000 .

$$\log. 13 = 1.113943$$

$$\log. 5 = 0.698970$$

$$\log 1000 = 3$$

Sum =
$$\frac{4.812913}{1}$$
 = log. of 65000.

log.
$$\cdot 0005 = \log.5$$
 with characteristic changed to -4 = $4 \cdot 698970$.

$$152 \cdot 1 = 3^{\circ} \times 13^{\circ} \div 10 \therefore \log. 152 \cdot 1 = (\log. 3) \times 2 + (\log. 13) \times 2 - \log. 10.$$

$$\log 3 = 0.477121 \times 2 = 0.954242$$

$$\log 13 = 1.113943 \times 2 = 2.227886$$

$$Sum = 3.182128$$

From which take
$$\log$$
. $10 = 1$

Diff. =
$$2.182128 = \log. 152.1$$

$$8.112 = 2^4 \times 13^2 \times 3 \div 1000 \cdot \log. \ 8.112 = (\log. 2) \times 4$$

 $\div (\log. 13) \times 2 + \log. 3 - \log. 1000.$

$$\log_{10} 2 = 0.301030 \times 4 = 1.204120$$

$$\log. 13 = 1.113943 \times 2 = 2.227886$$

$$Sum = \overline{3.909127}$$

Diff. =
$$0.909127 = \log.8.112$$
.

t 8 t²

1+12-38 —

a of

25 of : ... 9 y ... 9 y

If 9 ye

Assum $\frac{1}{6} + \frac{1}{12}$

21 ∴ he ! log. 13) × 2

2.227886

0·778151 1·449735

13 + log. 5

00. 1 to — 4

g. 3) × 2

log. 152·1

 $\log. 2) \times 4$

. .

g. 8·112.

(35) XII. 871tet-72 (t8:12 # × 300 = 210006e4 $t \times 8 \times 30 = 1800$... 83 == 54 179tet 159768 22854 \$ 82 × 300 = 245400020352720 $t 8 \times t \times 30 =$ 22800 84 2476884 1et372e4 $t 8 t^2 \times 300$ = 249961000517428000 t8t x 2 x 30 = 54500 2499e5504 4977ttt08 3e8391e4

 $\frac{1}{6} + \frac{1}{12} + \frac{1}{7} + 5$ years = $\frac{1}{23}$ of life time + 5 years = age at birth of son. $\frac{3}{23} = -(\frac{1}{23} + 5) = \frac{17}{23}$ of his life time — 5 years = time he lived after birth of son.

(36)

17 of father's life time — 5 years — 4 years = age of son = 1 father's age.

 $\frac{17}{28}$ of father's life time — 9 years = $\frac{1}{4}$ father's age.

.. 9 years is the difference between 17 and 14 of father's age.

... 9 years is equal to 3 of father's age.

If 9 years is $\frac{3}{28}$ of his age, $\frac{1}{28}$ will be the $\frac{1}{3}$ of 9 which is 3 years. If $\frac{1}{28}$ is 3 years, $\frac{28}{28}$ or the whole age will be $3\times28=84$ years.

Or by Position.

Assume 42 for father's age at death, the son's age =21.

 $\frac{1}{6} + \frac{1}{12} + \frac{1}{7} + 5 = \frac{1}{28} + 5$; $\frac{1}{28}$ of $42 = 16\frac{1}{2}$ and $16\frac{1}{2} + 5 = 21\frac{1}{2} = \text{age of father when son was born.}$

.. he lived after birth of his son 42 - 211 = 201 years.

(Continued on next page.)

EXPRO

(36 continued.)

By the question he lived 21 + 4 = 25 years. The error 25 - 201 = -41.

Assume 98 for father's age, then son's age = 1 of 98 = 49. $\frac{1}{6} + \frac{1}{1} + \frac{1}{7} + 5 = \frac{1}{28} + 5$; $\frac{1}{28}$ of $98 = 38\frac{1}{2}$, and $38\frac{1}{2} + 5 = 43\frac{1}{2}$ = age of father at birth of son.

 \therefore he lived after birth of his son 98-431=541 years.

But by the question he lived 49 + 4 years = 53 years. Then $53 - 54\frac{1}{2} = + 1\frac{1}{2} = \text{error.}$

Errors.

$$-4\frac{1}{2} \times 98 = 441$$

$$+1\frac{1}{2} \times 42 = 63$$
Sum = 6
$$504 \div 6 = 84 = \text{father s age.}$$

(37)

m.	fur. per. yds. ft. in.	far.	per.	vđa
63		io 7	23	
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12		60129		
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(Continued on next page.)

8 = 49.

ears.

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1+5=431

(37 continued.)

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(38)

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200 remainder.

yds.

(4) (4) (40) (40) (40) (5)

{ yds. : 613 yds. :: \$19 : \$ × 19 × 19 = 1478 = \$5.482.

(40)

 $I = Prt. = $4237.71 \times .065 \times 1.67 = $460.0034205.$

(41)

(42)

By Table, page 260, the amount of \$1 for 14 payments at 4 per cent. is \$1.73168.

Then \$1.73168 × 813.71=\$1409.0853328=Amount.

Subtract 813-71

Difference = 595.3753328=Interest.

(43)

			130	,
\$300	×	.: 0	=	11 44 0
700	×	4	=	2800
750	X	4. 7	=	5250
850	×	9	=	7650
400	×	13	=	5200
1300	X	. 19	==	24700
				-

45600 (10 months 18 days. 4300

80

78000 == days. 4300 35000 34400

49198

23 — \$96 D tog

\$1078 Ded be div

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+ \$78 \$181 Tha to \$21

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5.482.

Б.

258 years =

ments at 4

18-0 days.

(44)

23 per cent. of \$4200 = $\frac{23}{100}$ of 4200 = \$966.00, and \$4200 - \$966.00 = \$3234.00. E has half as much as A, B, C, and D together; therefore E has one-third of \$3234.00, which is \$1078.00.

Deducting E's share, \$1078, from \$3234, the whole sum to be divided, there remains \$2156 to be divided among A, B, O and D. Now D gets a certain amount; C gets \$42·11 more than D; B gets \$61·34 (42·11 + 19·23) more than D; and A gets \$78·44 (61·34 + 17·10) more than D. Together they get, then, four times D's share, together with \$42·11 + \$61·34 + \$78·44, or, in other words, four times D's share, together with \$181·89.

That is, four times D's share, together with \$181.89 is equal to \$2156.

Hence \$2156.00 - \$181.89 = \$1974.11 =four times D's share. Then $$1974.11 \div 4 = $493.5275 =$ D's share.

$$P = \frac{A}{1+rt} = \frac{\$3786 \cdot 80}{1+1.76} = \frac{3786 \cdot 80}{2.76} = \frac{378680}{276} = \$1372 \cdot 02898 + \frac{378680}{276} = \frac{\$1372 \cdot 02898}{276} + \frac{378680}{276} = \frac{$$

$$\{(3^{3}_{7}-2_{1}^{7}_{6})\times \cdot 46 \div \frac{2}{5} \text{ of } \cdot 142857\} \div 81 \text{ times } (1+\frac{1}{7}+\frac{1}{6}-\frac{3}{23}\frac{3}{10})$$

$$\left\{ \left(\frac{95}{95} \times \frac{12222}{99000} \div \frac{979}{7} \right) + \frac{3}{7} + 9\frac{3}{7} + 17\frac{4}{15} \right\} \div 27.4922077$$
(Continued on next page.)

 $[*]rt = .16 \times 11 = 1.76$.

(46 continued.)

$$\left\{ \left(\frac{11}{16} \times \frac{5}{5}, \frac{7}{500} \right) \times \frac{7}{5}, \frac{9}{8} + 27 \frac{1}{3}, \frac{5}{8} \right\} \div 27 \cdot 4922077$$

$$\frac{391}{5} \times \frac{7}{5} \times \frac{3}{5}, \frac{1}{8}$$

$$(1_0^1 + 27_{386}^{10}) \div 27.4922077$$

$$27_7^3 7_0^3 \div 27.4922077$$

$$= \frac{1}{27.4922077 \div 27.4922077} = \frac{1}{1} = 1$$

(47)

312312302 quaternary = 224690 decimal scale. 2312132 | quaternary = 11678 decimal scale.

Sum = 236368

4234 quinary == 569 decimal, and 569 \times 23011 == 13093259. 236368 \times 13093259 == 3094827443312.

555 + 444 + 333 + 222 + 111 senary = 2553 senary == 645 decimal.

3094827443312 - 645 = 3094827442667.

6542 septenary == 2333 decimal.

 $3094827442667 \div 2333 = 1326544124\frac{1375}{333}$ den.

$$1326544124 = 11704272374$$

$$1375 = 2537$$

 $\therefore 1326544124\frac{335}{335} = 11704272374\frac{27}{375}$

(48)

$$1 = \frac{1}{10}$$
 and $(\frac{1}{10})^2 = \frac{1}{100} = 01$

$$^{1} = \frac{1}{9}$$
 and $(\frac{1}{9})^{2} = \frac{1}{9} = .012345679$.

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7-4922077

093259.

ary == 645

FIFTH SERIES.

(50)

Assume 27 2...2...48 and 81, strike out 2, 9 and 16
16 3 since they are contained as factors in the others.

The l. c. m. = $27 \times 16 \times 3 = 1296$.

(51)

$$t = \frac{\log n}{\log (1+r)} = \frac{\log 7}{\log (1.06)} = \frac{0.845098}{0.025306} = 33.395 \text{ years.}$$
(52)

20 miles = 1267200 inches; and 14 ft. 10 in. = 178 inches. $1267200 \div 178 = 7119\frac{9}{44}$ times.

(53)

 $1749600 = 2^{6} \times 3^{7} \times 5^{8}$; increasing each index by unity and multiplying, we have $6 \times 8 \times 3 = 144$.

(54)

$$\begin{array}{c} \frac{96}{8} \cdot \frac{\frac{1}{2} \cdot \frac{1}{3!}}{\frac{3!}{8}} = \frac{2}{3} \times \frac{\frac{96}{4}}{8} \div \frac{\frac{1}{3!}}{\frac{3!}{8}} = \frac{2}{3} \times \frac{576}{13} \div \frac{\frac{1}{3}}{\frac{1}{3}} \\ = \frac{2}{3} \times \frac{576}{5} \div \frac{26}{13} = \frac{2}{3} \times \frac{576}{5} \times \frac{13}{23} = 35\frac{23}{23}. \end{array}$$

(55)

A can do the whole work in 12 days, therefore he can do $\frac{1}{12}$ in 1 day. A and B together can do the work in 5 days, therefore they can do $\frac{1}{6}$ in 1 day. Therefore B can do $\frac{1}{6}$ — $\frac{1}{12}$ = $\frac{7}{60}$ in 1 day, and he will require as many times 1 day to do the whole work as $\frac{7}{60}$ is contained times in 1, i. e. 1 $\frac{1}{60}$ = $\frac{40}{60}$ = 8 $\frac{1}{60}$ days.

40

F

F

B

Th

He

(56)

$$P = \frac{A}{(1+r)^{5}}; \log P = \log A - \log (1+r) \times t = \log 8899.77$$

$$- \log (1.06) \times 22 = 3.949378 - 0.025306 \times 22$$

$$= 3.949378 - 0.556732 = 3.392646, \text{ and } \log 3.392646$$

$$= $2469.71.$$

By Table, page 260, amount of \$1 at 6 per cent. for 22 payments = 3.60354.

Then \$8899.77 ÷ 3.60354 = \$2469.73 nearly.

(57)

Let the 1st number be 2. Then
$$2 \times 2 = 4$$

 $1\frac{1}{4} \times 3 = 4$

$$10 - (2 + 1\frac{1}{3}) = 10 - 3\frac{1}{3} = 6\frac{2}{3} \times 4 = 26\frac{2}{3}$$
, but it should equal 4.

Therefore $26\frac{1}{3}-4=+22\frac{3}{3}=$ error.

Let
$$1\frac{1}{2}$$
 be the 1st number; then $1\frac{1}{2} \times 2 = 3$

$$1 \times 3 = 3$$

$$10 - (1\frac{1}{4} + 1) = 10 - 2\frac{1}{4} = 7\frac{1}{4} \times 4 = 30$$
, but it should = 3.
Therefore $30 - 3 = +27 = \text{error}$.

Errors.

$$+27 \times 2 = 54$$

 $+22\frac{5}{3} \times 1\frac{1}{2} = 34$

Diff. =
$$4\frac{1}{3}$$
 diff. = 20, and 20 \div $4\frac{1}{3}$ = $4\frac{8}{13}$ = 1st number.
 $4\frac{8}{13} \times 2 = 9\frac{3}{12} = 1$ st product.

Second number =
$$9_{13}^{3} \div 3 = 3_{13}^{1} \times 3 = 9_{13}^{3} = 2$$
nd product.
 $10 - 7_{13}^{9} = 2_{13}^{1} \times 4 = 9_{13}^{3} = 3$ rd product.

(58)

Suppose A has 40; then B has 110 - 40 = 70, and C has 130 - 70 = 60.

A and C together have 40 + 60 = 100, but it should be 120. Therefore 100 - 120 = -20 = error.

Suppose A has 80; then B has 110 - 80 = 30, and C has 130 - 30 = 100.

A and C together have 80 + 100 = 180, but they should have 120. Therefore 180 + 120 = +60 = error.

(Continued on next page.)

(58 continued.)

Errors.

$$+60 \times 40 = 2400$$

 $-20 \times 80 = 1600$
Sum = 80 Sum = 4000

4000 + 80 = 50 = number A has.

Then B has 110 - 50 = 60, and C has 130 - 60 = 70.

= 60 = each man's share when equally divided.

(59)

Formula I, p. 333. $l = a + (n - 1) d = 7 + (47 - 1) \times 4$ $= 7 + (46 \times 4) = 7 + 184 = 191.$

Formula VI, p. 333. $s = \left\{ 2a + (n-1) d \right\} \frac{n}{2}$ $= \left\{2 \times 7 + (93 - 1) \times 4\right\} \cdot \frac{93}{4} = \left\{14 + (92 \times 4)\right\}^{\frac{93}{4}}$ $=(14+368)\times \frac{23}{3}=-$

(60)

log. n log. 21 1.322219= 44.997 years. $\log. (1+r) \log. (1.07)$ 0.029384

BIXTH SERIES.

(61)

B gets \$196.87 more than C, and A gets \$387 + \$196.87 = \$583.87 more than C, therefore together they get three times C's share, together with \$196.87 + \$583.87, i. e. three times C's share, together with \$780 · 74; but together they get \$3700.

Therefore \$3700 = three times C's share, together with \$780.74, or \$3700 - \$780 · 74 = \$2919 · 26 = three times C's share.

Hence $\$2919 \cdot 26 \div 3 = \$973 \cdot 08\% = C's share.$

Add 196.87

Sum = \$1169.95} = B's share. Add 387.00

Sum = \$1556.95% = A's share.

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(62)

(63)

$$\{(17_{17} - 10_{60}^{59}) - (4 + \frac{1}{6} + 9 - \frac{1}{4})\} \div (8378 \div \frac{1}{6} \text{ of } 31)$$

•6322632
$$\times \frac{1}{3}$$
 of $9\frac{1}{4} \div (\frac{1}{6})$ of $4\frac{1}{6}$ of $\frac{1}{11}$ of $85\frac{1}{2}\frac{6}{7} \div 101$)

$$= \frac{}{{}^{31}_{1}^{61} \times {}^{37} \times {}^{4} \times {}^{4} \times {}^{37} \times {}^{37}_{167} \times {}^{191}_{14}}$$

$$14 \times 37 \qquad 14 \times 37$$

$$= \frac{5}{\frac{1}{4 \times \frac{5}{4} \times \frac{37}{4}}} = \frac{5}{5 \times 37} = \frac{69}{25} = 2\frac{9}{25}.$$

(64)

Each child gets 1 child's share, ... 17 children get 17 shares.

Each woman gets three times a child's share, ... 4 women get 12 shares.

Each man gets six times a child's share, .: 3 men get 18 shares.

And together they get 47 times a child's share.

Therefore \$7200 \div 47 = \$153.19 $\frac{3}{17}$ = a child's share.

 $$153 \cdot 19_{37} \times 3 = $459 \cdot 57_{37}$

 $$153 \cdot 19 \frac{7}{4} \times 6 = $919 \cdot 1447$.

(65)

 $25400 = 2^3 \times 5^3 \times 127$. Adding unity to each index and multiplying the results, we get $4 \times 3 \times 2 = 24$.

(66)

(67)

(68)

$$\frac{67.432 = 67 \frac{138}{138} = \frac{6758}{111}}{990} = \frac{66758}{9990} \times \frac{111}{990} \times \frac{7410138}{111} = 8.5318452.$$

16

of 31)

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shares.

x and

(69)

9 per. 9 yds. 7 ft. 120 in. = 365628 inches 3 of 3 of 35 acres 2 roods = $\frac{3}{5}$ of 35 acres 2 roods = $\frac{3}{5}$ of 222678720 inches

	THE PROPERTY	
365628	2559398	•
of 222678720	122607020	= 0.019156118.
22 or ashototan	133607232	

(70)

Dissimilar.	Similar.
17.0342	17.03424242
27.06357	27 • 06357575
98 • 123456	98 • 123456456
829 • 6423	829 -642342342
986 · 1234298	986.1234298429
9.876342	9 · 876342876342

813-9864234567 813-9864234567 Similar and Coterminous,

17-03424242424242424242

#7 · 063575757575757575

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829 · 642342342342342342

986 • 123429842984298429

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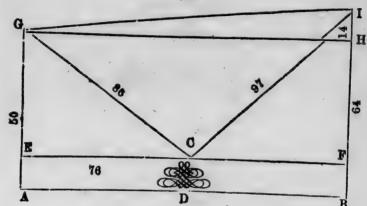
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18.

(71)





E G =
$$\sqrt{86^2 - 76^2} = \sqrt{1620} = 40.249$$
 feet

Height of Statue $GD = AG - EG = 50 - 40 \cdot 249 = 9 \cdot 751$ ft. = $BF = 64 - 9 \cdot 751 = 54 \cdot 249$ feet

 $CF = \sqrt{CI^2 - FI^2} = \sqrt{97^2 - 54 \cdot 249^2} = \sqrt{6466 \cdot C45999} = 80 \cdot 411 \text{ feet}$

GH = EF = EC + 6F = 76 + 80.411 = 156.411 feet and HI = 64 - 50 = 14 feet

 $GI = \sqrt{GH^2 + HI^2} = \sqrt{156 \cdot 411^2 + 14^2} = \sqrt{24660 \cdot 400921}$ = 157 \ \text{036 feet.}

(72)

The mixture = spirits + water = $\frac{1}{2}$ of mixture + 25 gal. + $\frac{1}{3}$ of mixture - 5 gal. = $\frac{1}{2}$ + $\frac{1}{2}$ + 20 gal. = $\frac{5}{6}$ + 20 gal. Then 20 gal. = $\frac{1}{6}$ of the mixture, and therefore the mixture contained $6 \times 20 = 120$ gal.

Then' $\frac{1}{2}$ of 120 = 60 + 25 = 85 gal. = spirits $\frac{1}{2}$ of 120 = 40 - 5 = 35 gal. = water

Lo

SEVENTH SERIES.

(73)

(74)

330024

Suppose father's age = 60, the son's age now = $60 \div 5 = 12$, and son's age four years ago = 12 - 4 = 8. But the son's age four years ago should, by the question, have been $60 \div 7 = 84$.

Therefore 8-84=-4= error.

Suppose father's age = 35; then son's age now = $35 \div 5 = 7$, and age four years ago = 7 - 4 = 3.

But son's age four years ago should, by question, have been 35 \div 7 = 5.

Therefore 3-5=-2= error.

Errors.

$$-2 \times 60 = 120$$

 $-4 \times 35 = 20$
diff. 1% diff. = 100

 $100 \div 10 = 10 = 10$ father's and son's age = $70 \div 5 = 14$.

(75)

(76)

Logarithm of $97294764\cdot372$ is $7\cdot988089$ $7\cdot988089 \div 11 = 0\cdot726189$ Log. $0\cdot726189 = 5\cdot32341 = 11$ th root of $97294764\cdot372$.

(77)

Assume 431 for the greater number

$$7\frac{1}{4}: 3\frac{1}{4}:: 43\frac{1}{4}: \frac{43\frac{1}{4} \times 3\frac{1}{4}}{7\frac{1}{4}} = 21 \text{ the less}$$

 $43\frac{1}{4} - 21 = 22\frac{1}{4} \text{ but it should} = 30$

Therefore error $= 22\frac{1}{4} - 30 = -7\frac{1}{4}$.

Assume 721 for the greater number

$$7\frac{1}{1}: 3\frac{1}{1}: 72\frac{1}{1}: \frac{72\frac{1}{1} \times 3\frac{1}{1}}{7\frac{1}{1}} = 35 = \text{the less}$$

 $72\frac{1}{2} - 35 = 37\frac{1}{2}$, but it should = 30

Therefore error = $37\frac{1}{4}$ - 30 = + $7\frac{1}{4}$.

Errors.

$$\begin{array}{c} + 7\frac{1}{2} \times 43\frac{1}{2} = 326\frac{1}{2} \\ - 7\frac{1}{2} \times 72\frac{1}{2} = 543\frac{3}{2} \end{array}$$

$$7\frac{1}{4}:3\frac{1}{4}::58:\frac{58\times3\frac{1}{4}}{7\frac{1}{4}}=28$$
 less.

(78)

1. c. m, = $35 \times 16 \times 9 \times 31 = 156240$.

en 60 ÷

-5 = 12, the son's

 $\div 5 = 7,$

been 35

= 14

(79)

Here
$$a = 1$$
, $d = 6$, $n = 101$,

$$a = \begin{cases} 2a + (n-1)d \end{cases} = \begin{cases} 2 \times 1 + (101 - 1) \times 6 \end{cases} = \begin{cases} 101 \\ 2 \times 1 + (101 - 1) \times 6 \end{cases} = (2 + 600) = \begin{cases} 101 \\ 2 \times 101 \\ 2 \times 101 \\ 2 \times 101 \end{cases} = 30401.$$
(80)

$$\frac{\left(\left\{(9\frac{1}{6}+4\frac{1}{1}\frac{1}{6}+3\frac{1}{7}-16\frac{3}{3}\frac{1}{6}\right)\times \cdot 54\right\} \div 14\right)\times 35 \text{ times } \cdot 142857}{\left\{\begin{array}{c} \cdot 9^{\frac{1}{7}}\times \cdot 24378 \times (1\frac{1}{4}\times 4\frac{4}{4}6\frac{1}{7})\right\}\times (4\frac{3}{17}-2\frac{1}{17})\\ \left(\left\{(16\frac{2}{3}\frac{2}{3}\frac{1}{7}-16\frac{1}{3}\frac{2}{6}\frac{1}{7})\times \frac{3}{5}\times \frac{1}{7}\right)\times 35\times \frac{1}{7}\\ \hline \\ \frac{85\times \frac{4}{3}\frac{1}{3}\frac{3}{6}\frac{1}{7}}{4\frac{2}{5}\frac{1}{7}\times \frac{1}{7}}\times \frac{3}{7}\times \frac{1}{7}\times \frac{3}{7}\times \frac{1}{7}\times \frac{3}{7}\times \frac{1}{7}\\ \hline \\ \frac{12}{3}\frac{1}{7}\times \frac{1}{7}\frac{1}{3}\frac{1}{7}\times \frac{1}{7}\times \frac{1}{7}\times \frac{3}{7}\times \frac{1}{7}\times \frac$$

(83)

Suppose the hour hand moves over 4 minutes, then since the minute hand moves 12 times as fast, it will have travelled over 48 minutes. But in order to overtake the hour hand, the minute hand must traverse the entire circle, 60 minutes, plus the 4 minutes we have supposed the hour hand to have moved forward, i. e. 64 minutes. Then 48 should equal 64, for we should find the same number by each process; 48 - 64 = -16 error.

Suppose hour hand moves over 6 minutes, the minute hand moves over $6 \times 12 = 72$ minutes. But minute hand moves over 60 + 6 = 66 minutes.

Then 72 - 66 = +6 error.

(Continued on next page.)

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Simple 1

Int.

(83 continued.)

ERT.

Errors.

- 16 × 6 = 96 + 6 × 4 = 24

Sum 22 Sum 120

120 + 22 = 5 h min. = minutes passed over by the hour hand, hence space passed over by the minute hand = $5A \times 12$ = 65_{11}^{h} min. = 1 hour 5_{11}^{h} min. = time.

Log. $\delta = \log_1 10 - \log_2 2 = 1 - 0.301030 = 0.698970$ $3850000 = 5 \times 7 \times 11 \times 10000$.

 \therefore Log. 3850000 = log. 5 + log. 7 + log. 11 + log. 10000 = 0.698970 + 0.845098 + 1.041393 + 4 = 6.585461.

 $3181.81 = 31.81 \times 100 = 31 \div \times 100 = 4.0 \times 100$

 \therefore Log. 3181.81 = log. 5 + log. 7 + log. 1000 - log. 11 = 0.698970 + 0.845098 + 3 - 1.041393 = 3.502675 $0000154 = 2 \times 7 \times 11 \div 10000000$

 \therefore Log. $\cdot 0000154 = \log \cdot 3 + \log \cdot 7 + \log \cdot 11 - \log \cdot 10000000$ = 0.301030 + 0.845098 + 1.041393 - 7 = 5.187521

 $\log_{10} \frac{1}{1} = \log_{10} 1 - (\log_{10} 7 + \log_{10} 11) = 0 - (0.845098)$ +1.041393) = 0 - 1.886491 = 2.113509.

1.571428 - 14 - 4.

 L_{0g} . 1.571428 = log. 11 - log. 7 - 1.041393 - 0.845098 - 0.196295

 $93.17 = 9317 \div 100 = 11^{\circ} \times 7 \div 100$

 \therefore Log. 9317 = 3 times log. 11 + log. 7 - log. 100 = 1.041393 $\times 3 + 0.845098 - 2 = 1.969277$

EIGHTH SERIES.

(85)

Simple Interest = $Prt = $700 \times .045 \times 3 = 94.50 .

Amount Compound Interest = $P(1+r)^s = $700 \times (1.045)^s$ = \$700 \times 1·14116 = \$798·814—\$700 = \$98·814 = Comp Int.

\$98,814 - \$94.50 = \$4.314.

101

C. ARTES

1: 1617.

142857 214)

44)

ince the led over minute he 4 miorward. uld find

ror. te hand moves (86)

X's gain = $\frac{1}{12}$, and Z's = $\frac{1}{2}$; .. Y's gain = 1 - $(\frac{1}{12} + \frac{1}{2})$ = $1 - \frac{1}{12} = \frac{5}{12}$.

X's gain is $\frac{18}{18}$ for 3 months, therefore for 1 month it is $\frac{1}{36}$. Y's gain is $\frac{1}{19}$ for 9 months, " " " $\frac{108}{36}$. Z's gain is $\frac{1}{19}$ for 4 months, " " " $\frac{108}{3}$. $\frac{1}{3}$: $\frac{1}{36}$:: \$3024: \$3024 × $\frac{1}{36}$ × $\frac{2}{3}$ = \$672 = X's stock. $\frac{1}{3}$: $\frac{1}{36}$:: \$3024: \$3024 × $\frac{1}{198}$ × $\frac{2}{3}$ = \$1120 = Y's stock.

(87)

 $\frac{1}{8} \times \sqrt{1\frac{7}{9}} \div (\frac{1\frac{1}{2}}{9})^3 = \frac{1}{8} \times \sqrt{\frac{16}{9}} \div (\frac{1}{8})^3 = \frac{1}{8} \times \frac{4}{9} \times \frac{4}{9} = \frac{4}{97}$

(88)

5169 15507

43 × 2 = 86 × 30 = 2580 43 × 2 = 86 × 30 = 4

557284 1114568 432² = 186624 × 300 = 55987200 56000161

56000161 56000161

(89)

 $7 = \left\{8 - 1 \frac{3+4}{1+6}\right\} = 7$

4 lbs. at 8d. 1 lb. at 4d. Make a mixture of 6 lbs. at 7d. 1 lb. at 6d.

6: 112:: 4: $\frac{112 \times 4}{2}$ = 743 at 8d.

(Continued on next page.)

Assum Since And 1

And 2

And 3

Assum Since 1 And 1s

And 21
And 3r

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(4 + 1)

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321 cubert

(89 continued.)

6: 112:: 1:
$$\frac{112 \times 1}{6}$$
 = 18\frac{2}{3} at 4d.

6: 112:: 1:
$$\frac{112 \times 1}{6}$$
 = 18% at 6d. (90)

Assume 40 as the sum of the three numbers. Since 1st + 2nd + 3rd = 40.

And 1st $+ \frac{1}{2}$ (2nd + 3rd) = 34 ... $\frac{1}{2}$ (2nd

And 2nd $+\frac{1}{3}$ (1st + 3rd) = 34 $\cdot \cdot \cdot \cdot \cdot \cdot \cdot$ (1st + 3rd = 9

And 3rd + $\frac{1}{4}$ (1st + 2nd) = 34 ... $\frac{2}{4}$ (1st

Adding, $2 \times (1st + 2nd + 3rd) = 29$

.. 1st + 2nd + 3rd = 141.

But the sum should equal 40. Hence $14\frac{1}{2} - 40 = -25\frac{1}{2}$.

Assume 48 as the sum of the three numbers.

Since 1st + 2nd + 3rd = 48.

And 1st + $\frac{1}{2}$ (2nd + 3rd) = 34 .. $\frac{1}{2}$ (2nd

+ 3rd) = 14.....2nd + 3rd = 28

And 2nd + 1 (1st + 3rd) = 34 ... 1 (1st

And 3rd + $\frac{1}{4}$ (1st + 2nd) = 34 .. $\frac{2}{4}$ (1st

Adding, $2 \times (1st + 2nd + 3rd) = 67$ \therefore 1st + 2nd + 3rd = 33%

But the sum should equal 48.

Hence $33\frac{5}{6} - 48 = -14\frac{1}{6} = \text{error.}$

Errors.

 $-251 \times 48 = 1224$

 $-141 \times 40 = 3663$

Diff. = 111 Diff. = 6571 $657\frac{1}{3} \div 11\frac{1}{3} = 58 =$ the sum of the three numbers.

(Continued on next page.)

\$10 :

\$40 :

\$87.

Form

(90 continued.)

1st + 1 (2nd + 3rd) = 34 ... 1 (2nd + 3rd) = 53 - 34 = 24 \therefore 2nd + 3rd = 48.

 $2nd + \frac{1}{2}(1st + 3rd) = 34$.. $\frac{2}{3}(1st + 3rd) = 58 - 34 = 24$ \therefore 1st + 3rd = 36.

1st + 2nd + 3rd = 58, and 2nd + 3rd = 48. 1st = 10. 1st + 2nd + 3rd = 58, and 1st + 3rd = 36. 2nd = 22. 2nd + 3rd = 48, and $2nd = 22 \cdot \cdot \cdot 3rd = 26$.

(91)

4 means + 2 extremes = 6 terms.

l-a40 - 1 39Formula IX, p. 333. d = n - 16-1

1, 81, 163, 243. 321, 40.

(92)

t = 1860040, l = 1240029, and r = 3.

Formula XI, p. 340. $a = rl - (r - 1) s = 1240029 \times 3$ $-(2 \times 1860040) = 3720087 - 3720080 = 7.$

(93)

6 apples + 7 pears cost 33 pence .. 2 apples + 21 pears cost 11 pence.

10 apples + 8 pears cost 44 pence .. 2 apples + 12 pears cost 8% pence.

Subtract, and 21 - 13 pears cost 11d. - 84d.

That is, to of a pear costs 21d.

If \$\frac{1}{16} \cost \frac{1}{6}\d., \frac{1}{16} \text{ will cost } \frac{1}{16} \cost \frac{1}{6}\d., \text{ which is \$\frac{1}{6}\d.} \text{2} \d. = 3\d.

6 apples + 7 pears cost 33 pence, and 7 pears cost 21d. .. 6 apples cost 12d. and 1 apple costs 2d.

$$= \frac{1}{4} \times \frac{8}{4} \times \frac{8}{2} \times \frac{19}{12} \times \frac{2}{8} \times \frac{2}{4} \times \frac{2}{4} = \frac{19}{2 \times 4 \times 3 \times 2} = 19$$

- 34 = 24

-34 = 24

1st = 10.

2nd = 22.

 40029×3

pears cost

pears cost

21d. . . 6

14.

(95)

\$10 = \(\frac{2}{4} \) of 2nd rem. - \$20 \(\cdots \). \(\frac{2}{4} \) of 2nd rem. \(\dots \) \$30 \(\cdots \). 2nd rem. \(\dots \) \$40.

\$40 = 1 of 1st rem. - \$30 ... 1 of 1st rem. = \$70 ... 1st rem. = \$70.

\$87.50 = 1 of original sum = \$50 \therefore 1 of original sum = \$137.50 \therefore original sum = \$137.50 \times 2 = \$275.

(96)

$$a = 60, n = 17, \text{ and } d = 4.$$
Formula VI, p. 333. $s = \begin{cases} 2a + (n-1)d \end{cases} \frac{n}{3}$

$$= \begin{cases} 2 \times 60 + (17-1) \times 4 \end{cases} \frac{17}{2} = (120 + 64) \times \frac{17}{2}$$

$$= \frac{184 \times 17}{2} = \$1564 = \text{sum received for 17 years.}$$

Formula I, p. 333. $l = a + (n-1) d = 60 + (17-1) \times 4$ = 60 + 64 = \$124 = wages for 17th year.

NINTH SERIES.

(98

£749 168. 5\frac{1}{2}d. = £749.823958; £1 sterling = \$4 867 £749.823958 \times 4.867 = \$3549.3932.

(99)

2)177408			
2)88704			
2)44352			2)138
2)22176			3)693
2)11088			3)231
2)5544			7)77
2)2772		. 4	111
2 × 34 ×	Tix	11.	

 $\frac{}{\times 2} = 18$

(100)

Formula III, page 354, $r = \sqrt[t]{\overline{A}}$ $t | \overline{A}$

 $Log. (r+1) = (log. A - log. P) \div t$

That is, $\log \cdot (r+1) = (\log \cdot 11111 \cdot 11 - \log \cdot 704) \div 11$ = $(4.045757 - 2.847573) \div 11$ = $1.198184 \div 11 = 0.108925$

Therefore r + 1 = natural number corresponding to the logarithm 0.108925 which is 1.285.

Since r + 1 = 1.285, r = .285 =rate per unit and rate per cent. = $.285 \times 100 = 28\frac{1}{4}$.

(101)

If 9 be $\frac{1}{13}$, $\frac{13}{13}$ or the whole will equal $9 \times 13 = 117$.

(102)

3 gal. + 4 gal. + 7 gal. = 14 gal.

Hence 14 gal. : 292 gal. :: 3 gal. : $\frac{292 \times 3}{292 \times 3} = 624$ of 1st kind.

292 × 4

14 gal. : 292 gal. :: 4 gal. : — = 83; gal. of 2d. "

292 × 7

(103)

 $\mathfrak{L}_{1}+\mathfrak{L}_{1}+\mathfrak{L}_{1}+\mathfrak{L}_{2}=\mathfrak{L}_{1}$

Then £1\frac{17}{60}: £500 :: £\frac{1}{2}: £500 \times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2}

=£194 16s. 149d.

£117 : £500 :: £1 : £500 × 1 × $99 = \frac{£10000}{77}$

=£129 178. 49∤d.

 $\pounds1\frac{1}{6}$: £500 :: £\frac{1}{2} : £500 \times \frac{1}{2} \times \frac{7}{7} = \frac{£7500}{77}

= £97 8s. 049d.

 $\pounds1\frac{1}{67}:\pounds500::\pounds_{\frac{1}{6}}:\pounds500\times\frac{1}{6}\times\frac{49}{77}=\frac{\pounds6000}{77}$

=£77 18s. 533d.

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(104)

By Table, page 363, present value of annuity of \$1 at 6 per cent. for 23 payments = \$12.30838.

Hence present value of \$100 = \$12.30338 \times 100 = \$1230.338.

By Formula V, page 361,
$$v = \frac{a}{r} \left\{ 1 - \frac{1}{(1+r)^t} \right\}$$

$$= \frac{100}{.06} \times \left(1 - \frac{1}{(1\cdot06)^{23}} \right)^* = \frac{10000}{6} \times (1 - 0\cdot261795)$$

$$= \frac{10000}{6} \times 0\cdot738205 = \frac{738205}{6} = \$1230\cdot34$$

(105)

Since each loses 1 hour per day for 24 days, the whole hours $lost = 24 \times 25$.

Also, 5 men working 1 hour per day for 12 days make up 5×12 $\times 1 = 60$ hours.

Hence they will each have to work as many hours per day as 60 hours is contained times in 24×25 hours, i.e. $\frac{24 \times 25}{25} = 10$ hours.

n 24 \times 25 hours, i.e. $\frac{100}{60}$ = 10 hours.

a = 5, s = 161 and d = 6

Then Formula II, p. 333. $l = -\frac{1}{2} d + \sqrt{2} ds + (a - \frac{1}{2} d)^2 = -\frac{1}{2} \text{ of } 6 + \sqrt{2} \times 6 \times 161 + (5 - \frac{1}{2} \text{ of } 6)^2 = -3 + \sqrt{1932 + 4} = -3 + \sqrt{1936} = -3 + 44 = 41 \text{ years.}$

 $6^3: 10^3:: 1 \text{ day}: \frac{10^3 \times 1}{6^3} = \frac{1000}{216} = 4 \cdot 629 \text{ days}.$

* Log.
$$\frac{1}{(1.08)^{8.3}} = \log_2 1 - \log_2 1 \cdot 06 \times 23 = 0 - 0.025306 \times 28$$

= $0 - 0.582038 = \overline{1.417962}$

(1:06)23 = natural number corresponding to the logarithm

1-417962, which is 0-261795

÷ 11

the loga-

rate per

7.

1st kind.

. of 2d. "

L of 3d.44

£15000

77 £10000

77 £7500

77

£6000

77

(108)

For 12 months he was to receive £8 and a suit of clothes; for 7 months he received £2 13s. 4d. and the suit of clothes; ... for 5 months he would have received the difference between £8 and £2 13s. 4d., which is £5 6s. 8d.

Hence for 1 month he would have received £5 6s. 8d. ÷ 5, which is £1 1s. 4d., and hence his wages for the year would have been, in money alone, £1 1s. 4d. \times 12, i.e., £12 16s. Therefore the suit of clothes was valued at £12 16s. — £8

= £4 16s.

TUNTH SERIES.

(109)

 $\frac{1}{2} + \frac{1}{2} + \frac{1}{4} = \frac{13}{2}$; if $\frac{13}{2}$ of a number = 48, $\frac{1}{12}$ will = 48÷13=3 $\frac{13}{12}$ If $3\frac{9}{13} = \frac{1}{12}$, $\frac{12}{12}$, or the whole number = $3\frac{9}{13} \times 12 = 44\frac{4}{13}$.

(110) 600×8^{3} 600 × 512 63:83 :: 600:-= 1432 · 2 lbs. 216 (See Art. 33, sec. X.)

(111)

Part of ball remaining after 1st has taken off her share = 1 Then whole ball : remainder :: cube of diameter of whole : cube of diameter of remainder

1: \frac{1}{2}:: 5^3: x^3 hence $x = \sqrt[8]{3} \times 125 = \sqrt[8]{3} = \sqrt[8]{93 \cdot 75} = 4.542$... Part taken off by 1st = 5 in. -4.543 in. = 0.458 in. After 2nd had taken off her portion } of the ball remained.

1: $\frac{1}{3}$:: 5^3 : x^3 , hence $x = \sqrt[3]{125} = \sqrt[3]{125} = \sqrt[3]{62 \cdot 5} = 3.968$ in.

... Part taken off by 2nd = 4.542 - 3.963 = 0.574 in.

After 3rd had taken off her share there remained } of the ball.

1: $\frac{1}{4}$:: 5^3 : x^3 , hence $x = \sqrt[3]{4} \times 125 = \sqrt[3]{31 \cdot 25} = 3 \cdot 149$ in. ... Part taken off by 3rd = 3.968 - 3.149 = 0.819 inches

Remainder - 3.149 - part taken on by 4th.

7121 1234

be 6 or

lst

2nd

88; for 7 clothes; ence be-

T. ARITH

3d. ÷ 5, r would £12 16s. s. - £8

13=313 3.

e: eube

= 4.542

ed. 968 in.

e ball. n.

108

72734 62831 88033 87625 5570 • 238552(71 • 118 = sq.	
6700E 8d. 11.118 = 8d	
	rt.
3070·0 151) 170 2468·4 151	
50°·50 1521) 18·23 371·36 15·21	- 141
118·130 15221) 3·0285 111·067 1·5221	the bar
7·0520 152228)1·406452 6·2831 1·360051	, , , , , , , , , , , , , , , , , , ,
·65780 ·62831 ·028480	.1

Note. - Unless the quotient is carried out to six places of decimals, i.e., twice as many as are required in the root, the last figure in the root will

·024684 .003685

log. 16

log. 1.05

1.204120

0.021189

1204120

21189

-= 56.827 years.

TORRES .

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(113 continued).
           $400 × 48 =
                          $19200
           $500 \times 42 =
                            21000
           $500 \times 36 =
                            18000
           $500 \times 30 =
                            15000
           $500 \times 24 =
                            12000
3rd
                                     = $103200 for 1 month.
           $500 \times 18 =
                            9000
          $500 × 12 =
                            6000
          $500 \times 6 =
                            3000
                Sum = $103200
          $900 \times 40 =
                          $36000
          $900 × 34 =
                           30600
          $900 \times 28 =
                           25200
          $900 × 22 =
                           19800
4th
          $900 × 16 =
                           14400
                                     = $138600 for 1 month.
          $900 \times 10 =
                            9000
          $900 × 4 =
                            3600
                8um = $138600
 $43280
                            4 years at $1.25 per day
 104400
                  = $1.25 \times 4 \times 365 = $1825 = share of 5th.
 103200
 138600
$389480 for one month.
$20000 - $1825 = $18175 = sum to be divided among the four.
$389480 : $18175 :: $43280 : $2019.651 = share of 1st.
$389480 : $18175 :: $104400 : $4871·803 =
                                                      2nd.
$389480 : $18175 :: $103200 : $4815 · 805 =
                                                      3rd.
$389480 : $18175 :: $138600 : $6467·739 =
                                                      4th.
                            (114)
                                        n-1
                                                 16 - 1
                                                            15
Simple Interest, formula IX, p. 248. t = -
                                                   -05
                                                            .05
           = 300 years.
                                                log. n
Compound Interest, formula V, p. 354.
                                             \log_{\bullet}(1+r)
```

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25 -

165 334 165

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F. ARTEN

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2nd. 3rd.

4th. - 1

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- r)

rs.

(115)

For every \$1 the first gave, the second gave \$3, and the third \$6. \$1 + \$3 + \$6 = \$10.

Hence the 1st gave \$1, the second \$3, and the third \$6 as often as \$10 is contained times in \$9202, which is 9201 times.

 $$1 \times 920\frac{1}{3} = $920 \cdot 20 = \text{payment of 1st person.}$

 $$3 \times 920\frac{1}{8} = $2760.60 = "2nd"$

 $\$6 \times 920 = \$5521 \cdot 20 = 4$ 3rd 4

(116)

25 + 22 = 47 = whole number of men.

165 ÷ 47 = 337 = acres cleared by each man.

 $3\frac{3}{4} \times 22 = 77\frac{1}{4}$ acres = acres cleared by company of 22 men.

165 acres — 7714 acres = 8734 acres = acres cleared by company of 25 men.

1st company contains 3 more men than 2nd company and receives \$86 more.

Therefore \$86 pays 3 men. Hence each man gets \$86 \div 3 = \$28.66\frac{2}{3}.

Each man clears $3\frac{24}{1}$ acres, and receives $$28.66\frac{2}{3}$ for it; therefore cost of 1 acre = $$28.66\frac{2}{3} \div 3\frac{24}{1} = $8\frac{82}{490}$.

(117)

 $15^2 = 225$; 346 - 225 = 121 = square of the less. Hence less = $\sqrt{121} = 11$.

(118)

Formula V, page 248, A=P (1+rt)=\$1200×1.95=\$2340.00.

(119)

24: 496

9: 11

465 : 3371 :: 51

33 : 53 24 : 31

(Continued on next page.

.7=

713

The

121

The

33 (

97 0

81 6

(119 continued.)

$$\times \frac{8}{-} \times \frac{8}{-} = 11 \times 4 \times 3 = 132 \text{ days.}$$

 $[\]frac{67}{60}$: $\frac{1}{60}$: $\frac{1}{3}$: $\frac{1}{3}$ × $\frac{49}{60}$ × $\frac{99}{60}$ = $\frac{39}{60}$ = $\frac{39}{60}$ of $\frac{36213}{60}$ = $\frac{32180}{60}$.

 $[\]frac{67}{60}$:: $\frac{1}{4}$: $\frac{1}{4}$ × $\frac{66}{80}$ × $\frac{69}{89}$ = $\frac{14}{4}$ = B's true share which is therefore = $\frac{1}{4}$ of \$6213 = \$1635.

 $[\]frac{27}{67}$: $\frac{1}{6}$: $\frac{1}{6}$: $\frac{1}{6}$ × $\frac{6}{6}$ × $\frac{6}{6}$ × $\frac{6}{2}$ = $\frac{1}{6}$ = C's true share which is therefore = $\frac{1}{6}$? of \$6213 = \$1308.

MLEVENTH SERIES.

(121

·7=7; ·83=\$3; ·727=7\$7; ·91325=°\$\$\$\$50°=\$\$\$\$8=4\$\$\$\$.

8·671347=8⁶⁷13475²=8\$71388=81318\$.

(122)

713 unden. = 861 den.; 291 unden. = 342 den.; 311 unden. = 474 den.

291

Then $713 \frac{1}{3t}$ under $= 861 \frac{3}{4} \frac{1}{4}$ den $= 861 \frac{1}{4} \frac{7}{6}$ den.

12123 quat. = 411 den; 11223 quat. = 363 den.; 100000 quat. = 1024 den.

Then $12123_{1000000}^{11223_3} = 411_{1024}^{363}$ den.

(123)

 3_3^3 of 2_5^1 of 7_{20}^{11} of £1 = $\frac{27}{3}$ of $\frac{11}{5}$ of $\frac{151}{20}$ of £1

 $=\pounds^{4}_{800}^{4547}...$ $=\pounds^{56}$ 1 $2\frac{1}{10}$

 $9\frac{3}{7}$ of $3\frac{8}{9}$ of 1s. $=\frac{66}{7}$ of $3\frac{6}{9}$ of 1s. $=\frac{110}{3}$ s.... = 1 16 8

 $8\frac{1}{8}$ of $4\frac{1}{8}$ of $1d. = \frac{3}{8}$ of $1d. = \frac{10}{3}\frac{3}{8}2d... = 0$ 2 $10\frac{1}{3}\frac{1}{8}$

Sum = £58 0 8_{160}^{21}

 $\frac{11}{12}$ of $\frac{5}{14}$ of $\frac{3}{8}$ of $3\frac{1}{2}$ d. $=\frac{11}{12} \times \frac{5}{14} \times \frac{3}{8} \times \frac{7}{4} = \frac{45}{128}$ d.

£58 68. $8_{160}^{21}d. = \frac{22288501}{160}d.$

 $\begin{array}{c} {}^{2228501} \div {}^{55}_{126} = {}^{2328501} \times {}^{128}_{16} = {}^{202521}_{16} \times {}^{4}_{1} = {}^{8102364}_{25} \\ = 32414.56. \end{array}$

(124)

24 : 90 2½ : 4½ 12½ : 9¾ 47 : 4⅓ :: 139¾ : #

31 : 21

(Continued on next page.)

18 =

87

57

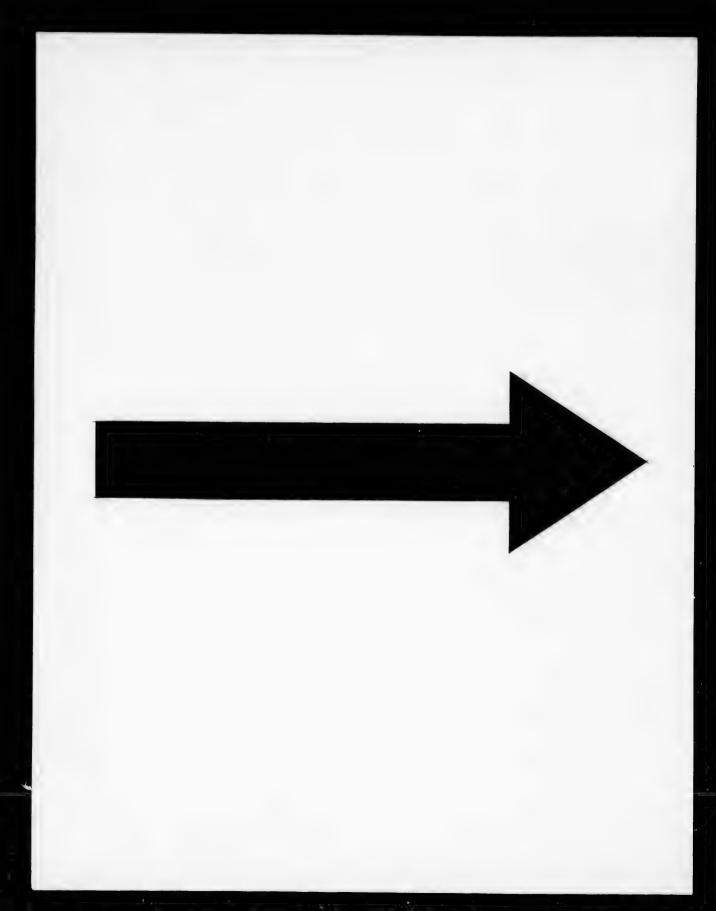
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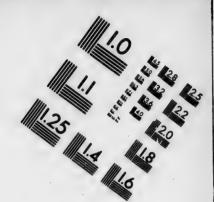
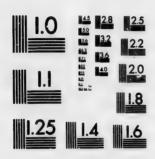


IMAGE EVALUATION TEST TARGET (MT-3)



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(124 continued.)

(125)

\$182 is $\frac{91}{100}$ of buying price ... \$182 \div 91 = \$2 = $\frac{1}{100}$ of buying price = \$2 × 100 = \$200.

To realize a profit of 7 per cent., he must receive \$1.07 for every \$1 the goods cost; but they cost him \$200, therefore he must sell for $$1.07 \times 200 = 214 .

(126)

Simple Interest
$$t = \frac{n-1}{t} = \frac{111-1}{.06} = \frac{10.5}{.06} = \frac{1050}{.06}$$

Compound Interest
$$t = \frac{\log n}{\log (1+r)} = \frac{\log 11\frac{1}{4}}{\log 1.060698} = \frac{1060698}{25306} = 41.914 \text{ years.}$$

(127)

An acre contains 4 roods = 160 sq. perches. .: 160 ÷ 151 = 1010 perches = length.

(128)

35 yards = 32 metres .. 1 yd. = 3% of a metre.

69 % miles = 69 1 × 1760 yards = 69 1 × 1160 × 35 metres

$$= \frac{\frac{1519}{1519} \times \frac{1989}{1} \times \frac{32}{1}}{\frac{32}{15}} = 217 \times 16 \times 32 = 111104 \text{ metres.}$$

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Par 1 :

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1 sh Six 116871 (199)

f means + 2 extremes = 9 terms.

Formula XIII, p. 340.
$$r = \left(\frac{l}{a}\right)^{\frac{1}{2}} = \left(\frac{19683}{2}\right)^{\frac{1}{2}} = \left(6561\right)^{\frac{1}{2}} = 3$$
Hence means are 9, 27, 81, 243, 729, 2187, and 6561.

Formula XXI, p. 344.
$$s = \frac{\alpha}{1-r} = \frac{7}{1-\frac{1}{2}} = \frac{7}{\frac{1}{2}} = \frac{28}{3} = 9\frac{1}{2}$$

(181)

Part remaining after 1st has received his share = \$.

1:
$$\frac{1}{4}$$
 :: $60^{\frac{1}{3}}$: $x^{\frac{3}{3}}$; whence $x = \sqrt{3600} \times \frac{1}{4} = \sqrt{900} \times \frac{3}{3}$
= $30\sqrt{3} = 1.732 \times 30 = 51.96$ inches,

Hence 1st ground off 60 - 51.96 = 8.04 inches.

Part remaining after 2nd had taken off his share = 1.

1:
$$\frac{1}{3}$$
 :: 60° : x° ; whence $x = \sqrt{3600 \times \frac{1}{3}} = 30 \sqrt{2}$
= $1.4142 \times 30 = 42.426$.

Hence 2nd ground off 51.96 - 42.426 =: 9.534 inches.

Part remaining after the 3rd had taken off his share = 1.

1: $\frac{1}{4}$:: $60^{\frac{1}{2}}$: x^2 ; whence $x = \sqrt{3600 \times \frac{1}{4}} = \sqrt{900} = 30$ inches. Hence 3rd ground off 42.426 - 30 inches = 12.426 inches, and the 4th ground off remaining 30 inches.

I guinea

1 half guinea = 101s.

1 crown = 5s.

100 guiness = 2100 shillings.

1 half crown = 21s.

2100 - 401 = 51 times and remainder, 69 half-shillings.

1 shilling = lg. Sixpence 45.

69 half-shil. = 49s. = £28 = 128.

Bum = 401s.

metres

of buy-

1.07 for 0, there-

1050

.060698

.025306

metres.

1

88

TWELFTH SERIES.

(133)

$$\frac{8}{11} \frac{2}{9} \frac{4}{17} = \frac{8}{561}; \frac{2\frac{1}{2}}{4\frac{1}{4}} \frac{2}{5} = \frac{10}{17} \frac{2}{5} = \frac{4}{17}$$

$$\frac{8}{561} : \frac{4}{17} :: \$12\frac{4}{17} : \$12\frac{4}{17} \times \frac{4}{17} \times \frac{561}{8} = \frac{200}{88} \times \frac{4}{17} \times \frac{88}{8} = \frac{200}{17} \times \frac{4}{17} \times \frac{88}{17} \times \frac{1}{17} \times \frac{1}{1$$

(134)

... 1 + r = nat. num. corresponding to the logarithm 0.075899 which is 1.19, ... r = .19 = rate per unit, and hence rate per cent. = 19.

(135)

Having paid 10 per cent. he had 90 per cent. remaining. 10^{90}_{100} or 10^{9}_{100} of his salary = \$1250, $10^{9}_{100} = 12^{90}_{100} = 1385 . If \$1385 = 10^{9}_{100} , the whole = \$1385 \times 10 = \$1388-888.

(136)

21 children receive 21 times a child's share

21 women " 42 " "
21 men " 63 " "

22

0.075899

nce rate

1388. 88.

(137)

A gets 1 time A's share

B " 1 " A's ".

O " 2 " A's "

D . # 4 . # A's #

Together they get 8 times A's share.

\$200 \div 8 = \$25 = A's share; \$25 = B's share.

\$25 + \$25 = \$50 = 0's share; \$25 + \$25 + \$50 = \$100= D's share.

(138)

 $\sqrt[8]{3} = \frac{1}{2}\sqrt[8]{18} = \frac{1}{2}$ of $2 \cdot 62074 = \cdot 87358$

 $\sqrt{3} = \frac{1}{2} \sqrt{6} = \frac{1}{2} \text{ of } 2.44948 = .81649$

Difference = .05709

(139)

3872 when each term is divided by 121, becomes 767.

 $17_{15} + _{15} + _{144} + _{161} + _{161} + _{16} + _{16} + _{16} + _{16} + _{16} + _{161} + _{166} + _{166}$

 $+\frac{339}{120} = 161 + \frac{327}{120} = 161 + 1\frac{37}{120} = 162\frac{37}{120} = 162\frac{39}{120}$ $2\frac{1}{3}\frac{3}{5} - \frac{1}{1}\frac{7}{5} = 2\frac{65}{175} - \frac{1}{1}\frac{19}{5} = 1\frac{1}{7}\frac{19}{5} - \frac{1}{1}\frac{19}{5} = 1\frac{1}{7}\frac{19}{5}.$

> 15 21 54 $-\circ f - \circ f - \circ f - \circ f - = -$

> ¥ % 15 11 23 253

 $6347 \div 23 = \frac{6347}{1} \div \frac{1}{1} = \frac{6347}{1} \times \frac{4}{1} = 2308.$

(140)

884736 (96= cube root.

729

 $9^{9} = 81 \times 300$ = 24300155736

 $9 \times 6 = 54 \times 30 = 1620$

62 =

155736 25956

 $95951\frac{1}{2}\frac{1}{2}$ = $95951 \cdot 2576$.

(Continued on next page.)

B

C

N

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(140 continued.)

95951 · 2576 (309 · 76 = square root.

618-7)470-25 27)209 433 - 09 189

619 • 46) 37 • 1676 34.6)2076 37.1676 2076

250

300

400

500

$$\frac{$520 \times 250}{1450:250:$520:} = $89\frac{19}{1450} = contrib. on 1st village.$$

\$520×300 1450:300:: \$520:-

---=\$107\d3= 1450

\$520×400

1450:400:: \$520:--=\$14313= 3rd 1450

\$520×500

1450:500::\$520:--=\$179%= " 1450 (142)

By Table on p. 362, the amount of \$1 for 34 payments at 3 per cent. = \$57.73018.

 $$57.73018 \times 260 = $15009.84.$

By Formula I, page 361,
$$A = \frac{a \{(1+r)^t - 1\}}{a \{(1+r)^t - 1\}}$$

$$= \frac{a}{r} \left\{ (1+r)^{2} - 1 \right\} = \frac{260}{03} \left\{ (1.03)^{34} - 1 \right\}$$

$$= \frac{26000}{3} \times (2.731855 - 1) = \frac{26000 \times 1.731855}{3} = $15009.41$$

th root.

(143)

By Formula IX, p. 333, $d = \frac{l-a}{n-1} = \frac{79-2}{6-1} = \frac{77}{5} = 183$.

Hence the series is 2, 17‡, 32‡, 48½, 63¾, and 79.

Formula I, p. 333. $l = a + (n-1) d = 3 + (9-1) \times 4$ = 3 + (8 × 4) = 3 + 32 = 35.

Formula VI, p. 333. $s = \left\{ 2a + (n-1)d \right\} \frac{n}{2}$ = $\left\{ 2 \times 3 + (207 - 1) \times 4 \right\} \frac{207}{2} = \left\{ 6 + (206 \times 4) \right\} \frac{207}{2}$ = $(6 + 824) \times \frac{207}{2} = \frac{830 \times 207}{2} = 85905$.

(144)

B-travels 4 miles per-day faster than A, and will therefore gain the circumference of the island in ⁷/₄ = 18½ days.

C-travels 10 miles per day faster than A, and will therefore gain the whole circumference of the island in $\frac{73}{10} = 7_{10}^3$ days.

Now B cannot be with A except at the end of 18½ days or twice 18½ days, or three times 18½ days, or some other multiple of 18½ days.

Similarly C cannot be with A except at the end of 7_{10}^3 days, or of some other multiple of 7_{10}^3 days.

Therefore C and B will both be with A for the first time after the lapse of a number of days expressed by the least common multiple of 18‡ and 7,3°.

The greatest common factor of 184 and 71% is 31%.

Hence the l. c. m. of $7\frac{3}{10}$ and $18\frac{1}{4}$ is $\frac{7\frac{3}{10} \times 18\frac{1}{4}}{3\frac{1}{20}} = 36\frac{1}{4} = \text{number}$ of days when A, B, and C will first be together.

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9 - 41

ARITHMETICAL RECREATIONS.

The third of 6 = 2, and the fourth of 20 = 5.
 Then if 2 becomes 3, what should 5 become? Evidently
 Ans.

or

$$\begin{cases} 6:20 \\ \frac{1}{2}:\frac{1}{4} \end{cases} :: 3:x = \frac{8 \times 20 \times \frac{1}{4}}{6 \times \frac{1}{4}} = 74.$$

2. The half of 5 = 21; then if 7 becomes 21, what will 11 become?

$$\frac{2\frac{1}{4} \times 11}{7} = \frac{1}{4}.$$
 Lastly, what part of 9 is \(\frac{1}{4}\)?

or

9: 5
7: 11
$$x = \frac{1 \times 5 \times 11}{9 \times 7} = \frac{44}{64} = \frac{55}{125}$$
. Ans.

3. 998.

- 4. 1 of 2d. = 3d. Then 3d. is what part of 3d.? Ans. 3.
 - 5. 11d. for a herring and a half is at the rate of 1d. per herring; hence 11 herrings will cost 11d.
- 6. 12 apples = 21 pears = 7 cents.

If 12 apples cost 7 cents, what will 100 apples cost?

12: 100::
$$7:\frac{100\times7}{12}=58\frac{1}{2}$$
 cents.

- 7. If 5 is $\frac{2}{3}$ of a certain number, $\frac{1}{3}$ will be $\frac{1}{3}$ of 5, which is $\frac{5}{3}$. If $\frac{5}{3}$ is $\frac{1}{7}$ of a certain number, the whole number will be $\frac{5}{3} \times 7 = \frac{3}{5} = 11\frac{3}{2}$. Ans.
- 8. The hurdles are arranged so as to form a rectangular enclosure having 49 hurdles on each side and one on each end. Two additional hurdles will give two hurdles to each end, and will thus double the size of the enclosure.
- The mode of dividing the plot may be learned from the following figure:—

vidently

will 11

- 10. 33}
- 11. XIII; rub out the lower half, and there remains the expression VIII = 8.
- 12. 1st Step: Fill the 3-gallon cask and empty it into the 5-gallon cask.
 - 2nd Step: Again fill the 3-gallon cask out of the 8-gallon cask.
 - ²rd Step: Fill up the 5-gallon cask out of the 3-gallon cask. This will leave one gallon in the latter.
 - 4th Step: Empty the 5-gallon cask into the 8-gallon cask. 5th Step: Pour the one gallon out of the 3-gallon cask
 - into the 5-gallon cask.

 6th Step: Fill the 3-gallon cask out of the 8-gallon cask, and empty it into the 5-gallon cask.

The following diagrams show this more clearly:

1st Step.

2nd Step.



Ans.

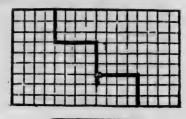
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13. The heavy line in the accompanying figure shows how the board is to be cut.



8	1	6
3	6	7
4	9	2

15. Weigh out 7 lbs. as often as possible and there will remain 2 lbs.; add two four pounds and one seven pounds to this, and the sum will be 17 lbs., the share of one.

Weigh 7 lbs. as often as possible out of the remaining 34 lbs. and there will remain 6 lbs., to which add 7 lbs. and 4 lbs., and the sum will be 17 lbs., the share of the second. The remaining 17 lbs. will be the share of the third.

- 16. The hurdles are, in the first case, placed 12 on a side and one on each end, and then they inclose a space represented by 12 squares whose area is, by the question, 40 square yards. If two hurdles be taken away there will remain 24, and if these be placed in the form of a square, each side containing 6 hurdles, they will enclose a space represented by 36 squares of the same size as the former. Hence they now inclose three times as much space as before, i. c. three times 40 square yards, or 120 square yards.
- 17. He takes the goose to the remote bank and leaves it there, returning, he next carries over the fox, which he leaves, but takes the goose back with him. He now leaves the goose on the first bank, and carries over the oats which he allows to remain on the remote bank with the fox, and returns for the goose.
- 18. The following diagrams exhibit the solution of this problem:

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I. III. IV

3	3	3	4	1	4	2	5	2	1	7	1		
3	3	3	4	1	4	2	5	2	5	2	1	7	1
3	3	3	4	1	4	2	5	2	5	2	1	7	1
24	20	28	20										
V. VI.													

| 0 | 9 | 0 | 5 | 0 | 4 |
| 0 | 9 | 0 | 4 | 0 | 5 |
| 36 | 18

19. XII; rab out the lower half, and VII remains,

20.

17	24	1	8	15
23	5	7	14	16
4	6	13	20	22
10	12	19	21	3
11	18	25	2	9

RULE FOR FILLING MAGIC SQUARES OF ODD NUMBER OF CELLS.

Begin in centre cell of top horizontal row by placing 1 in it; ascend diagonally to the right, and where this carries us beyond the square, transport the next number to the cell at the remote end of the vertical or horizontal band to which it belongs. When in ascending we come to a cell already filled, we place the number in the cell next below the cell last filled. The following is a square of 7 cells in a side filled after this method:

(Continued on next page.)

turns for problem:

000

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Ø

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28

30	39	48	1	10	19	28
38	47	7	9	18	27	29
46	6	8	17	26	35	37
5	14	16	25	34	86	45
13	15	24	33	42	44	4
21	23	32	41	43	3	12
22	31	40	49	2	11	20

- 21. Half-a-dozen d :en = $6 \times 12 = 72$. Six dozen dozen = $6 \times 12 \times 12 = 864$. 864 - 72 = 792. Ans.
- 22. The following shows the mode of performing this. It will be observed that the two side counters are merely moved one counter higher when the other two are taken away.
- 23. This problem admits of the following two solutions:

1ST SOLUTION.

Persons.	Full bottl	es. Hffull	bottles.	Empty	bottles.
1st	2		3	2	
2nd	2	8 8 5 1 1 P. C.	3 1 45.15		
3rd	3		1	3	
	_	-	_		
	7,	" (Jan 19	7	7	

Each person has 3½ bottles of wine and 7 bottles.

2ND SOLUTION.

1st	3	1	. 2
2nd		i	3
3rd	1	5	1
•	-	-	-
	7	7	7

Each person, as before, has 7 bottles and 31 bottles of wine.

- 24. There were in all 8 bottles of wine, of which each drank \(\frac{1}{2}\), which is 2\(\frac{1}{2}\). The third person, therefore, drank \(\frac{1}{2}\) of a bottle belonging to him who had but 3 bottles, and \(\frac{1}{2}\) of a bottle belonging to him who owned the 5 bottles. Hence the latter should have seven times as much of the money as the former, or, in other words, the latter gets 7 shillings, and the former 1 shilling.
- 25. This problem is merely to find some number between 50 and 100 which is exactly divisible by 2 and by 3, but which divided by 5 leaves a remainder 3.
 - The only numbers between 50 and 100 that are divisible by both 2 and 3, are 54, 60, 66, 72, 78, 84, 90, and 96, and by inspection the only one of these which gives a remainder 3 when divided by 5 is 78; therefore the basket contained 78 eggs.
- 26. Ans. 1 lb., 3 lbs., 9 lbs., and 27 lbs.
- For 1 lb. = 1 lb.; 2 lbs. = 3 lbs. -- 1 lb., i. e. 3 lbs. in one scale and 1 lb. in the other; 3 lbs. = 3 lbs.; 4 lbs. = 3 lbs. + 1 lb.; 5 lbs. = 9 lbs. -- (3 lbs. + 1 lb.); 6 lbs. = 9 lbs. -- 3 lbs.; 7 lbs. = 9 lbs. + 1 lb. -- 3 lbs.; 8 lbs. = 9 lbs. -- 1 lb.; 9 lbs. = 9 lbs.; 10 lbs. = 9 + 1 lb.; 11 lbs. = 9 lbs. + 3 lbs. -- 1 lb.; 12 lbs. = 9 lbs. + 3 lbs.; 13 lbs. = 9 lbs. + 3 lbs. + 1 lb.; 14 lbs. = 27 lbs. -- (9 lbs. + 3 lbs.); 15 lbs. = 27 lbs. -- (9 lbs. + 3 lbs.); 16 lbs. = 27 lbs. + 1 lb. -- (9 lbs. + 3 lbs.); 17 lbs. = 27 lbs. -- (9 lbs. + 1 lb.); 18 lbs. = 27 lbs. -- 9 lbs.; &c., &c.
- 27. In order to fill seven out of the eight points, it is merely requisite to remember that the second counter must be carried to the point from which the first started, the third to the point from which the second started, &c.
 - Thus if the first counter is carried from 1 to 4 and there de posited, the second must be taken from 6 to 1 and there deposited; the third from 3 to 6; the fourth from 8 to 3; the fifth from 5 to 8; the sixth from 2 to 5; and the seventn either from 7 to 2 or from 2 to 7.
- 28. The mouth fills the reservoir in 6 hours, therefore it fills in 1 hour; the right eye fills it in 38 hours, therefore it fills

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 $\frac{1}{48}$ in 1 hour; the left eye fills it in 72 hours, therefore it fills $\frac{1}{48}$ in 1 hour; the foot fills it in 96 hours, therefore it fills $\frac{1}{96}$ in 1 hour. Hence together they fill $\frac{1}{6} + \frac{1}{43} + \frac{1}{78} + \frac{1}{96} = \frac{6}{18}$ in 1 hour, and to fill the reservoir they require $1 \div \frac{6}{18} = \frac{6}{18} = \frac{8}{18} = \frac{8$

29. The person who thinks of the numbers must proceed as follows: He must multiply the 1st by 2 and add 5 to the poduct; he must next multiply this sum by 5 and add the record number to the product; he must next multiply this result by 10 and add the third number to the product; lastly, he must subtract 250 and name the remainder.

The three digits of the remainder will be the three numbers thought of, and will be in the order in which they were thought of.

The reason is obvious: let c = 1st, b = 2nd, and c = 3rd number thought of.

$$a \times 2 + 5 = 2a + 5$$
.

$$(2a+5) \times 5 + b = 10a+b+25.$$

$$(10a+b+25) \times 10+c=100a+10o+c+250.$$

$$(100 a + 10 b + c + 250) - 250 = 100 a + 10 b + c =$$
a in hundreds' place, b in tens' place, and c in units' place.

30. Since each man possesses 63 square rods of land more than his son, we must form three pairs of numbers, such that the difference of their squares shall be 63.

The difference of the squares of two numbers is equal to their sum multiplied by their difference, and hence 63 must be divided into two factors in three distinct ways, thus:

$$63 = 63 \times 1 = 21 \times 3 = 9 \times 7$$
.

If sum = 63 and difference = 1, the numbers are 32 and 31. If sum = 21 and difference = 3, the numbers are 12 and 9. If sum = 9 and difference = 7, the numbers are 8 and 1.

Hence the squares of Jones, Brown, and Smith, are respectively 32 rods, 12 rods, and 8 rods on the side, and the son's squares are respectively 31, 9, and 1 yards on the side.

Jones' piece was 23 rods longer on each side than Tom's, and since the difference between 32 and 9 is 23, we may conclude that Jones' square was 32 rods to the side, and Tom's 9 rods on a side.

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Brown'c piece was 11 rods longer on a side than Harry's, and since if the above numbers 12 and 1 have 11 for their difference, we may conclude that Brown's piece was 12 rods on a side, and Harry's piece 1 rod.

Hence Tom was Brown's son, Harry was Smith's son, and Ned was Jones' son

31. The mode of arranging the crew may be remembered by attention to the vowels in the following line:

Populeam virgam mater regina ferebat.

The vowels refer to the crew as follows, a = 1, e = 2, i = 3, o = 4, and u = 5.

We begin with 4 whites because the first vowel is o, next u = 5 blacks, next e = 2 whites, next a = 1 black, next i = 3 whites, next a = 1 black, next a = 1 white, next e = 2 blacks, next e = 2 whites, next e = 2 blacks, &c., as follows, o standing for a white and e = 2 black.

32. You select the multiplier or the multiplicand, such that the sum of its digits shall be exactly divisible by nine. Hence upon the principle of the proof by casting out the nines, the product has the sum of its digits exactly divisible by nine. By subtracting the sum of the digits of the remainder from the next higher multiple of 9 you determine the digit crossed out.

Thus suppose you select 117, and he takes for multiplicand 21613. Then 21613 × 117 = 2528721. Now, suppose he crosses out the 7; upon reading you the remaining digits 252821, you find that their sum = 20, which taken from 27 the next higher multiple of 9 leaves 7 the digit he crossed out.

If he crosses out a 0 or a 9, you cannot determine which, but in all other cases you can tell the exact figure.

33. You write the second, fourth, sixth, &c. lines in such a manner as to make the sum of the first pair, the sum of the second pair, &c. an exact number of 9's. Then having settled the number of pairs, you get the answer by multiplying by that number a row of 9's containing as many digits as there are to be figures in the line.

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and 31. and 9. d 1. espee-

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s, and y con-Tom's Thus suppose you agree to write 5 lines each, and that each line is to contain 5 digits, or not more than 5 digits. Then 99999 × 5 = 499995 will be the answer. This is shown as follows:

Suppose he writes You write	41113 } 58886 }	= 99999 }	
Suppose he writes You write	61451 ? 38548 \$	= 99999	
Suppose he writes You write	6500 }	= 99999	= 99999 × 5.
Suppose he writes You write	99998	= 99999	
Suppose he writes You write	99999 }	= 99999_	
Sum =			

THE END

ARITH

t each Then wn as

× 5.